



# *Article* **A Spatial Agent-Based Model for Studying the Effect of Human Mobility Patterns on Epidemic Outbreaks in Urban Areas**

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**Abstract:** The epidemic outbreaks of the last two decades have led governments to rely more on computational tools for establishing protection policies. Computational approaches to modeling epidemics traditionally rely on compartmental models, network models, or agent-based models (ABMs); however, each approach has its limitations, ranging from reduced realism to lack of tractability. Furthermore, the recent literature emphasizes the importance of points of interest (POIs) as sources of population mixing and potential outbreak hotspots. In response, this study proposes a novel urban spatial ABM validated using our augmented SICARQD epidemic model. To replicate daily activities more accurately, the urban area is divided into a matrix of points of interest (POIs) with agents that have unique paths that only permit infectious transmission within POIs. Our results provide a qualitative assessment of how urban characteristics and individual mobility patterns impact the infected population during an outbreak. That is, we study how population density, the total number of POIs (where the population concentrates), the average number of POIs visited by an agent, the maximum travel distance from the home location, and the quarantine ratio impact the dynamics of an outbreak. Our ABM simulation framework offers a valuable tool for investigating and controlling infectious disease outbreaks in urban environments with direct applicability to global policy makers.

**Keywords:** computational epidemics; agent-based model; nonpharmaceutical interventions; urban population

**MSC:** 93A16; 92D30; 91D10; 62R07

## **1. Introduction**

The dynamics of recent epidemics such as H1N1, SARS, and COVID-19 have been a significant challenge and top public health priority for many governments around the world [\[1–](#page-17-0)[3\]](#page-17-1). Traditional epidemiological approaches employ compartmental models that categorize the population based on economic and demographic factors, among others. Despite the lack of complexity in individual behavior, these models have been shown to be effective in the formation and shaping of public health policies [\[4–](#page-17-2)[6\]](#page-18-0).

Most approaches in computational epidemics use compartmental models (analytical approach), complex network models, agent-based models (ABMs), or hybrid solutions. The sole usage of compartmental models offers reduced realism and tractability since all agents interact with other agents without any geo-spatial restrictions, omitting the complexity of human organization [\[6–](#page-18-0)[8\]](#page-18-1). Network models solve this problem, as nodes only interact with their neighbors, but it is the infection that must *spread* to static node locations, instead of allowing nodes to move as in the case of dense urban environments [\[9](#page-18-2)[,10\]](#page-18-3). More recently, agent-based models (ABMs) have become a powerful computational tool for the study of infectious disease outbreaks [\[11–](#page-18-4)[15\]](#page-18-5).

Unlike traditional approaches, such as compartmental models or network models, ABMs offer a high degree of realism by allowing agents to move freely and interact in a dynamic environment. This makes ABMs especially useful in modeling complex urban



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environments, where populations are dense and mobility patterns play a critical role in the spread of disease [\[16\]](#page-18-6). During the beginning of the COVID-19 pandemic, ABMs were successfully used in exchange for simpler compartmental models, such as the SIR and SIS [\[17](#page-18-7)[,18\]](#page-18-8).

Nevertheless, many ABMs also lack tractability, as agents are permitted to move *anywhere* and interact *anywhere* in the system. To this end, the recent literature has shown the increased importance of points of interest (POIs) as the main sources of population mixing and therefore outbreak hotspots [\[19](#page-18-9)[–21\]](#page-18-10). In other words, it turns out to be more realistic to track human interaction inside POIs only and control the epidemic by limiting access to, or entirely closing, POIs during outbreaks.

Authors Chang et al. [\[19\]](#page-18-9) showed that a fraction of POIs account for the majority of infections and that restricting POI occupancy is more effective than uniformly reducing mobility. By contrast, the authors use an SEIR epidemic model that cannot account for quarantine and patient recurrence as our SICARQD (*Susceptible* − *Incubating* − *Contagious* − *Aware* − *Recovered* − *Quarantined* − *Dead*) model [\[22\]](#page-18-11). The study in [\[11\]](#page-18-4) by Hackl et al. concentrated on the Zurich (CH) transport network and used a SIR model to explain the dynamics of influenza. Conversely, our ABM provides a general framework for testing customizable urban areas and makes use of a more detailed epidemic model. In [\[14\]](#page-18-12), authors Zhuge et al. created a hybrid ABM–social network model which establishes friendships between agents based on similarity and geographic information; their model is general purpose but lacks the mobility paradigm for agents. In [\[20\]](#page-18-13), authors Li et al. provided a statistical study on population flow for POIs for 16 US cities, and showed which categories of POIs were more affected by quarantine. Authors Nian et al. [\[21\]](#page-18-10) studied the relationship between residents' mobility, POIs, and social activities from the perspective of taxi travel during COVID-19; their conclusions focused on the recovery of public transport in megacities during the post-epidemic period. Finally, we mention the study by Mao et al. [\[23\]](#page-18-14), in which the authors employed the SLIR epidemic model for H1N1 and created an ABM for the Buffalo region (USA) with its local businesses (POIs); the authors concluded that certain POIs are critical in spreading the disease.

In light of these recent developments, we propose an urban spatial ABM that replicates the daily mobility of an average individual as much as possible. Specifically, the urban area is divided into a matrix of equidistant POIs, and all agents will have a unique random path of POIs to follow from and back to their home location. Agent interactions that trigger infectious transmission will only be possible inside a POI. In other words, two agents need to be at the *same time* and at the *same POI* to be able to transmit an airborne viral infection between each other.

The main motivation of this study is to define a general purpose, customizable, and computationally efficient *urban spatial agent-based model* which uses a points-of-interest (POIs) matrix as relevant interaction points for the spread of infectious diseases, opinion, innovation, rumors, etc. In terms of originality, agents move independently between a controlled number of POIs in their daily routine and may be restricted to move inside a variable area around their home location. Infection may only occur within POIs, reducing computational complexity from *O*(*A* 2 ) (*Agents*<sup>2</sup> ) to *O*(*AP*) (*Agents* · *POIs*). Moreover, in this study, we focus on epidemic outbreaks and how their dynamics can be influenced by population density, the number of urban POIs, the average number of POIs visited by an agent, the maximum travel distance from the home location, and the impact of the quarantine ratio. To this end, we incorporate our previously validated SICARQD epidemic model [\[22\]](#page-18-11), which allows patient quarantine and relapse, and supports three stages of infection.

In addition to detailing the urban spatial ABM, our study aims to answer the following questions relevant to epidemic outbreaks:

- 1. How does population (density) in an urban environment affect outbreak dynamics?
- 2. How does the number of population accumulation points (POIs) scale with the impact of an outbreak?
- 3. How do mobility restrictions (reducing the maximum travel distance and the number of visited POIs) reduce the outbreak intensity?
- 4. How does the quarantine policy for new cases reduce the impact of the outbreak?

By addressing these questions, we aim to prove the practicality of our ABM and implicitly define a set of qualitative directives to enhance effective epidemic control with both social and scientific impact in the ABM literature and in computational epidemics.

# **2. The Urban Spatial Agent-Based Model**

We further detail the reasoning and methodology for developing the urban spatial agent-based model used to simulate epidemic outbreaks in a target population.

We set out to create an urban-like environment, where agents are distributed in a 2D space and move freely to various points of interest (POIs) in their daily business. Regardless of age and social status, these POIs represent common population accumulation points, such as shops, schools, university campus, office buildings, hospitals, churches, train/metro stations, hotels, administrative buildings, cinemas, etc.

As such, we start by defining a fixed rectangular area  $S = w \cdot h$ , given by a width w and a height *h*. This area is divided into a matrix of uniform square areas based on a fixed distance parameter *P<sup>d</sup>* between two adjacent POIs. Furthermore, urban POIs are placed at each intersection of matrix cells, including along the margins of the urban area (see illustration in Figure [1a](#page-3-0)). For simplicity, all POIs are treated the same; no distinction is made in terms of maximum occupancy or time spent inside by an agent. In fact, future developments of this model may include several distinct classes of POIs with specific characteristics.

Given the constant orthogonal distance  $P_d$  between adjacent POIs, we express the total number of POIs *P*, using the numbers  $P_x$  and  $P_y$ , and define the coordinate matrix POIs (sized  $P_x \times P_y$ ) based on area *S*:

$$
0 < P_d \le \min\{w, h\} P_x = \lfloor w / P_d \rfloor + 1 P_y = \lfloor h / P_d \rfloor + 1 P = P_x \cdot P_y
$$
\n
$$
(1)
$$

<span id="page-2-0"></span>
$$
POIs = \begin{bmatrix} (0,0) & (\frac{1}{P_x - 1}S,0) & (\frac{2}{P_x - 1}S,0) & \dots & (\frac{P_x - 1}{P_x - 1}S,0) \\ (0, \frac{1}{P_y - 1}S) & (\frac{1}{P_x - 1}S, \frac{1}{P_y - 1}S) & \dots & \dots & (S, \frac{1}{P_y - 1}S) \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ (0, \frac{P_y - 1}{P_y - 1}S) & (\frac{1}{P_x - 1}S, S) & \dots & \dots & (S, S) \end{bmatrix}
$$
(2)

Within the urban area *S* a number of *A* agents are randomly placed and constitute the fixed simulation population. All agents are considered equally and uniformly distributed within the area *S*. To simulate changes in population density, which is considered an important factor that influences the speed and impact of epidemics, we keep the urban area fixed and alter the agent population *A* (where population density  $\delta = A/S$ ).

Each agent  $a_i \in A$  receives a random home location  $(h_i(hx_i, hy_i))$ , and a maximum travel distance *T<sup>d</sup>* within the agent can move. Figure [1b](#page-3-0) exemplifies an agent *a<sup>i</sup>* (green dot) and its allowed travel area (gray square). In this area, an agent will receive a number of *N<sup>p</sup>* random POIs that the agent will visit repeatedly throughout the simulation process; each of these POIs matches a public urban POI. To determine a new POI for an agent, a random point  $(x, y)$  is generated, and the nearest urban POI—within the permitted area, i.e., closer than  $T_d$ —is chosen as the POI  $p_i^j$  $\mathbf{f}_i'$  that the agent will visit.

<span id="page-3-0"></span>

**Figure 1.** Schematic representation of the main defining properties of the urban ABM. (**a**) A rectangular (or square) space *S* is defined by width and height (*S* = *w* · *h*), which is divided as a matrix of uniform square areas based on the fixed distance  $P_d$  between POIs. An urban POI is placed in each intersection of the dotted lines, including along the margins of the area, e.g.,  $7 \times 7$  POIs are placed in the example model. The orange icons suggest possible urban POIs, such as shops, offices, train stations, churches, hospitals, etc. (**b**) For each agent (green dot), a number of *N p* POIs are assigned within the maximum travel distance *T<sup>d</sup>* . Each randomly placed POI (gray dot) is assigned as the *nearest* urban POI (orange dot) within the permitted gray square area. (**c**) An agent (green dot) will travel, independently of any other agent, along the designated green path through each POI (orange dots) and return to its home position; then, after a timeout, the process of visiting the same list of POIs repeats. Other agents (blue dot) have different paths to follow. The (infectious) interaction is only possible if two agents are at the same simulation time *t* at the same POI.

The last ABM specific phase is the agent mobility which implies any type of agent– agent interaction and transmission process (e.g., infection, opinion, rumor, innovation, and trade). Figure [1c](#page-3-0) exemplifies how an agent *a<sup>i</sup>* (green dot) continuously moves between its home and five POIs (numbered  $p_i^0$  to  $p_i^4$ ) along the green path. Once all POIs have been visited, the agent returns to its home position and waits for a short delay period; then, the same movement process repeats, i.e., the same agent POIs are visited in the order in which they were initially added to the list. Other agents (such as the blue dot in Figure [1c](#page-3-0)) have different POIs and thus different paths to follow. The interaction between two agents is only possible if the agents are at the same simulation time *t* at the same POI (e.g., like  $p_i^1$ coinciding with  $p_j^2$ ). The position of any agent  $a_i$  at any time *t* is given by the coordinates  $(x_i(t), y_i(t))$ . The first two described steps represent the urban initialization and the setup phase before the simulation can begin. The pseudocode for the setup of each agent and its POIs is described below.

Additional details on the speed, direction of movement, and interactions of each agent are explained with the help of Figure [2.](#page-4-0) All agents have the same constant speed limit  $A_v$ and move in a straight line to their next destination (i.e., a POI or their home location). The speed  $A_v$  is used to move the agent in any direction using a horizontal  $vx$  and a vertical *vy* speed. The two speeds are updated when an agent reaches a destination point and the next point is set as the new destination; then, the distances to the next destination (*dx*, *dy*) are measured along the Ox and Oy axes; the ratio *dx*/*dy* determines the new direction of movement. The ratio between the speeds satisfies  $vx/vy \propto dx/dy$  and  $vx^2 + vy^2 = A_v^2$  (see Figure [2a](#page-4-0)).

<span id="page-4-0"></span>

**Figure 2.** Overview of the agent movement characteristics. (**a**) An agent (green dot) moves in a straight line towards the next POI (orange dots), or returns home, with a constant speed of *Av*. Given the 2D space, two components of the speed are calculated, *vx*, *vy*, based on the ratio between the horizontal and vertical distances, *dx*, *dy*, towards the next POI; this ratio determines the direction of movement. The sum of the two squared speeds equals the square of the agent speed *Av*; thus, all agents move at the same speed, regardless of their direction. (**b**) Three agents (green, yellow, and blue) move towards the central POI (orange). The state of being *inside* a POI translates to being within  $\delta_{interact}/2 = 2 \cdot Av$  of the POI itself. Once an agent enters the target area (gray square), a new destination is immediately computed, and the agent changes its direction. In the example, all three agents move iteratively with speed *Av* towards the POI, step by step, as suggested by the short arrows and time steps  $(t_k)$ . Agents  $a_1$  and  $a_2$  enter the POI at time  $t_{k+3}$  and exit immediately at  $t_{k+4}$ ; agent *a*<sup>3</sup> enters the POI at *tk*+<sup>1</sup> , changes course, and exits at *tk*+<sup>4</sup> . In this sense, all three agents interact with each other only for one iteration  $(t_{k+3})$ , whereas agent  $a_3$  may interact with other agents for three iterations as shown in the upper right panel.

Each agent updates its position  $(x_i, y_i)$  with  $(vx, vy)$  in every simulation iteration *t*, and thus,

$$
(x_i(t+1), y_i(t+1)) = (x_i(t), y_i(t)) + (vx_i(t), vy_i(t))
$$
\n(3)

where each agent has its own movement speeds (*vx*, *vy*) updated after reaching a new POI.

The example in Figure [2b](#page-4-0) details the movement update of three agents (green, yellow, and blue) that move to the same POI (orange). An agent is considered to have reached the POI when its position is within *δinteract*/2 of the POI position. Consequently, when an agent enters the target area (gray square), a new destination is automatically calculated, and the agent updates its speed  $(vx, vy)$ . The movement speed of all agents is  $A_v$  as they move iteratively along the suggested arrows at each iteration (from  $t_k$  to  $t_{k+6}$ ). In Figure [2b](#page-4-0), agents  $a_1$  and  $a_2$  enter the POI at time  $t_{k+3}$  and exit the next iteration at  $t_{k+4}$ ; agent  $a_3$  enters the POI at *tk*+<sup>1</sup> , updates course, and exits at *tk*+<sup>4</sup> . In this example, all three agents interact with each other only for one iteration ( $t_{k+3}$ ), whereas agent  $a_3$  can interact with other agents for three iterations as shown in the upper right panel.

Given the current position of an agent  $a_i$  at a destination, say,  $p_i^k$ , the movement parameters towards the next destination, say,  $p_i^{k+1}$ , are updated as follows:

$$
(dx, dy) = p_i^{k+1}(x, y) - p_i^k(x, y)
$$
  
\n
$$
d = |dx/dy|
$$
  
\n
$$
vx = sgn(dx) \cdot \frac{d \cdot A_v}{\sqrt{d^2 + 1}}
$$
  
\n
$$
vy = sgn(dy) \cdot \frac{A_v}{\sqrt{d^2 + 1}}
$$
  
\n
$$
vx^2 + vy^2 = \frac{sgn^2(dx) \cdot d^2 \cdot A_v^2 + sgn^2(dy) \cdot A_v^2}{d^2 + 1} = \frac{A_v^2(d^2 + 1)}{d^2 + 1} = A_v^2
$$
 (5)

<span id="page-5-0"></span>where *sgn* is the sign function and is used to define the correct direction of each speed. Equation [\(5\)](#page-5-0) confirms that the two agent speed vectors add up to the  $A_v$  vector.

The full movement algorithm—through all POIs back home, and repeated for each agent—is detailed by the following pseudocode.

As a note on Algorithm [1,](#page-5-1) during the setup phase, each agent has their list of POIs (*ai* .*pois*) initialized (see Algorithm [2\)](#page-6-0), their next POI index initialized to *poi*\_*index* = 0, and destination to *destination* = *pois*[0].

<span id="page-5-1"></span>

**Require:**  $A > 0$ ,  $\delta_{interact} > 0$ ,  $N_p > 0$ ,  $A_v > 0$ <br> **if**  $stayHome > 0$  **then**  $\triangleright$  1 **▷ Random timeout to stay home before leaving** *stayHome* ← *stayHome* − 1 **else if**  $dist((x_i, y_i),$  *destination*)  $< \delta_{interact}$  **then**  $\triangleright$  Agent is within destination **if** *destination* ==  $h_i(hx_i, hy_i)$  **then ▷ Agent has returned home**  $(x_i, y_i) \leftarrow (hx_i)$ , *hyi*) ▷ Reset position and path  $stayHome \leftarrow rand(5, 100)$  $poi\_index \leftarrow 0$ *destination* ← *a<sup>i</sup>* .*pois*[*poi*\_*index*] updateAgentDestination(*destination*(*x*, *y*), *ai*(*x<sup>i</sup>* , *yi*), *Av*) **else Ⅰ else b b Agent has reached another POI**  $poi\_index \leftarrow poi\_index + 1$ **if**  $poi$ *\_index*  $\geq a_i$ *.pois.length* **then** .*pois*.*length* **then** ▷ All POIs have been visited  $\mathcal{A}$  *destination*  $\leftarrow h_i(hx_i, hy_i)$ **else ▷ The next POI on the path will be visited** *destination* ← *a<sup>i</sup>* .*pois*[*poi*\_*index*] **end if** updateAgentDestination(*destination*(*x*, *y*), *ai*(*x<sup>i</sup>* , *yi*), *Av*) **end if else else b** Update agent position  $(x_i, y_i) \leftarrow (x_i, y_i) + (vx, vy)$ **end if end if procedure** UPDATEAGENTDESTINATION(*destination*(*x*, *y*),  $a_i(x_i, y_i)$ ,  $A_v$ )  $dx =$  *destination* $(x) - x_i$  $dy = destination(y) - y_i$  $d = abs(dx/dy)$  $vx = sgn(dx) * d * A_v/sqrt(d*d + 1)$  $v\psi = sgn(dy) * A_v/sqrt(d*d + 1)$ **end procedure**

<span id="page-6-0"></span>**Algorithm 2** ABM setup phase.

**Require:**  $S > 0, 0 < P_d \leq S, A > 0, P_d \leq T_d \leq w, 0 < N_p \leq P$  $POS[$ [ $] \leftarrow int[P_x + 1][P_y + 1]$   $\triangleright$  According to Equation [\(2\)](#page-2-0) **for** ∀*a<sup>i</sup>* ∈ *A* **do**  $h_i(x_i, y_i) \leftarrow (rand[0, S], rand[0, S])$ , *yi*) ← (*rand*[0, *S*],*rand*[0, *S*]) ▷ Random placement of agents inside *S* **end for for** ∀*a<sup>i</sup>* ∈ *A* **do for**  $j = 0$  *to*  $N_p - 1$  **do** Generate  $(x, y) \leftarrow (h_i(x_i, y_i) \pm rand[-T_d/2, T_d/2]) \Rightarrow$  Random points inside  $T_d$ *p*<sup>*j*</sup> ← closest POIs to  $(x, y)$  inside  $(h_i ± [−T_d/2, T_d/2])$ add  $(p_i^j)$  $\binom{J}{i}$  to  $a_i$ .*pois*() ▷ Save to agent's POI list **end for end for**

# *Theoretical and Practical Performance Analysis*

The originality of this urban spatial ABM was motivated by the fact that agent interactions do not happen *everywhere* all the time but are restricted to the areas inside urban POIs. To this end, our simulator reduces the computational complexity and enables a speedup of large simulations.

A standard ABM approach, in which any two agents  $a_i, a_j \in A$  can interact at every iteration, would require the constant checking of all pairs of agents to determine whether they are within the interaction distance  $\delta_{interact}$ , leading to a time complexity of  $O(A^2)$ . We consider using only urban POIs as places of interaction also to improve the time complexity of the simulation. In this sense, at each iteration *t*, each agent checks its proximity to each urban POI; an agent may be outside of all POIs, or inside one at maximum (because POIs are spatially nonoverlapping). If proximity to one POI is detected, the iteration suspends and jumps to the next agent, reducing the check time for each agent. Furthermore, once proximity to an agent *a<sup>i</sup>* is detected, a POI *poi<sup>k</sup>* updates its list of currently visiting agents  $\textit{poi}_k(\textit{agents}) \leftarrow \textit{a}_i$ . The final interaction step is the actual iteration over all POIs, and checking all pairs of agents for the relevant properties (e.g., infection status and opinion).

The number of agents inside POIs, at a given time, is estimated using the ratio between the area occupied by all POIs *S<sup>p</sup>* and the total urban area *S*. Given that the interaction range of a POI with an agent is  $\delta_{interact} = 4 \cdot A_v$  (see Figure [2b](#page-4-0)), the area occupied by all POIs is  $S_p = (4 \cdot A_v)^2 \cdot P$ , and the ratio between the two area is

$$
\frac{S_p}{S} = \frac{(4 \cdot A_v)^2 \cdot P}{w \cdot h} \tag{6}
$$

To estimate the ratio between the areas in a real example, we exemplify two extreme simulation settings:  $\{S = 1000^2, A_v = 2, P = 1\}$  (small village) and  $\{S = 1000^2, A_v = 2,$ *P* = 1000} (large city). The difference between the two settings is the number of POIs *P* being  $\times$ 1000 greater. In the first setting, we obtain  $S_p/S = 0.0064\%$ ; in the second setting, we obtain  $S_p/S = 6.4\%$ . This means that around 6% (or less) agents will be inside POIs at a certain time *t*. Therefore, we estimate the number of interacting agents per iteration, in all urban POIs, as  $A \cdot S_p/S \approx (0.006 - 6)\% \cdot A$  (6% worst case). The pseudocode for the full interaction algorithm (Algorithm [3\)](#page-7-0) is given below.

The function *updateAgentsStatus*() is given as an example for any placeholder function which checks the status between two agents (e.g., infection and opinion) and updates one or both of the agents in *O*(1) time.

In conclusion, the time complexity for the agent interaction is summarized as follows:

- Reset agent lists in all urban  $POIs O(P)$ .
- Check the proximity of all agents in all POIs  $O(A \cdot P \cdot (1 0.06)) = O(A \cdot P \cdot 0.94)$ (approximated as worst case).

• Interaction between all pairs of agents in each POI –  $O(P \cdot (A/P \cdot S_p/S)^2) \approx O(A^2/P \cdot S_p/S)$  $(0.06<sup>2</sup>)$  (worst case).

The full complexity is approximated as  $O(P + 0.96 \cdot A \cdot P + 0.0036 \cdot A^2/P) \approx O(AP +$  $0.0036 \cdot A^2/P)$ , which, given the real-world values of  $A \leq 10^6$  inhabitants and  $P \leq 1000$ POIs, can be further approximated to *O*(*AP*). Overall, we consider our model's time complexity an important improvement over the standard  $O(A^2)$ , where, in most realworld scenarios, the number of individuals is much higher than the number of population accumulation points ( $P \ll A$ ) in an urban area.

The underlying simulation software is written in Java entirely by the authors. Currently, the code—without a GUI—is available on GitHub at [https://github.com/deltaalex/](https://github.com/deltaalex/Urban_ABM_SICARQD) [Urban\\_ABM\\_SICARQD](https://github.com/deltaalex/Urban_ABM_SICARQD) (accessed on 1 September 2024).

<span id="page-7-0"></span>

### **3. Materials and Methods**

Given the multitude of possible parameters in an epidemic model, as well as an ABM, we consider incorporating a straightforward and intuitive epidemic process on top of the presented urban spatial ABM. Specifically, we employ the previously developed SICARQD epidemic model [\[22\]](#page-18-11) to showcase the practical utility of our ABM in the context of evaluating tracking and control strategies for an infectious outbreak.

In particular, SICARQD (*Susceptible* − *Incubating* − *Contagious* − *Aware* − *Recovered* − *Quarantined*− *Dead*) is an upgrade of our previous SICARS model [\[24\]](#page-18-15) that was custom tailored for the COVID-19 pandemic and is a generalization of the popular SIR/SEIR model [\[25,](#page-18-16)[26\]](#page-18-17), explicitly aimed at the analysis of isolation strategies that were relevant to the early COVID-19 outbreak.

In this study, we employ discrete event simulation, a widely acknowledged approach in the field of computational epidemiology, to model intricate systems characterized by the interplay of multiple stochastic processes and the inherent structure of the system [\[27\]](#page-18-18).

#### *3.1. The SICARQD Epidemic Model*

For the purpose of this study, we employ the complex epidemic model named SICARQD [\[22\]](#page-18-11), summarized in Figure [3,](#page-8-0) and which defines the seven possible infectious states and particular transition rates. As such, an agent can be in one of the following states: *susceptible SUS*, *incubating INC*, *contagious CTG*, *aware AWR*, *quarantined QRT*, *recovered REC*, or *dead DED*. The transition from  $SUS \rightarrow REC \rightarrow SUS$  is determined by several infection rates, the quarantine ratio, the quarantine policy, and the recurrence scenario. We summarize the main epidemic parameters as follows:

- *rINC*: The rate of *susceptible* agents becoming infected in the vicinity of an infectious agent (which is in either of the two *infectious* states *CTG* or *AWR*). An agent in the *INC* state will not infect other agents.
- *rCTG*: The rate of *incubating* agents becoming contagious *CTG* after a specific period (depending on the modeled virus). In this state, an agent does not know that it is infected (has no symptoms yet), but it infects others.
- *rAWR*: The rate of *contagious* agents becoming aware after a specific period. In this state, an agent knows that it is infected (has symptoms) and infects other agents in its vicinity.
- *rREC*: The rate of *aware* (or *quarantined*) agents recovering after an infectious period. The transition determines whether an agent has fully recovered, becoming temporarily immune (*REC*), or if the agent has died (*DED*) based on the death ratio *rDED*. Recovered agents *REC* may not be infected.
- <span id="page-8-0"></span>• *rRCR*: The recurrence rate of *recovered* agents to become *susceptible* again after a specific period of recovery from infection.



**Figure 3.** Schematic of the SICARQD epidemic model with its seven states and transmission dynamics based on the infection ratios. The characteristic two-stage infectious process (*CTG* and *AWR*) enables our model to differentiate between and early (proact-Q) and a late (react-Q) quarantine policies. The ratio *rQRT* of agents moved to quarantine *QRT* will no longer infect other agents and will transit directly to the recovered *REC* or dead *DED* states. Moreover, recovered *REC* agents may become susceptible *SUS* again, in time, based on the imposed recurrence scenario.

In addition to the classical transition between susceptible, infected, and recovered states (SIR), SICARQD offers several transitions that increase the realism of epidemic modeling. First, a quarantine policy and a quarantine ratio *rQRT* will define *when* and *how many* agents transition to the *QRT* state; in this state, agents are not be able to infect others and will transition directly to the *REC* state (or, alternatively, to the *DED* state). Second, our epidemic model adds a recurrence scenario, which determines *whether* or *how fast* agents transition back to *SUS*.

Since the epidemic model is not the main focus of this study, we briefly explain the quarantine and recurrence scenarios for agents. The quarantine policy is of three types:

- 1. Proactive quarantine (**proact-Q**)—agents may be quarantined immediately as they become contagious *CTG* and require real-time contact tracing and detection before symptoms appear).
- 2. Reactive quarantine (**react-Q**)—agents may be quarantined as they become aware *AWR*, and require home isolation as symptoms appear.
- 3. No quarantine (**no-Q**)—all infected agents remain active in the population.

In this study, we maintain the react-Q policy in most simulation scenarios, except when stated otherwise. We choose the reactive policy as the default because it is the most realistic in terms of large-scale real-world applicability when human and financial resources are limited, and quarantining is based largely on visible symptoms [\[28\]](#page-18-19).

The recurrence scenario is of three types:

- 1. Quick recurrence (**quick-R**)—short immunity duration of 3 months on average.
- 2. Slow recurrence (**slow-R**)—longer immunity duration of 12 months on average.
- 3. No recurrence (**no-R**)—meaning the rate  $r_{RCR} = 0$  and all recovered agents remain permanently immune.

In addition, in this study, we adopt the slow-R scenario in all cases since a 'yearly' recurrence is highly realistic for many ongoing/seasonal airborne viral infections (influenza [\[29\]](#page-18-20) and COVID-19 [\[30\]](#page-18-21)).

For additional details on the epidemic model, please refer to our previous study in [\[22\]](#page-18-11).

#### *3.2. Real-World Epidemic Parameters for SICARQD*

The SICARQD allows customization for airborne infections, similar in complexity to influenza and coronaviruses. Therefore, given the ongoing relevance of the COVID-19 pandemic, in this study, we choose to parameterize our SICARQD model to the SARS-CoV-2 virus.

Table [1](#page-9-0) details the values for each of the model's parameters as found in the recent COVID-19 literature; we enumerate all the parameters illustrated in Figure [3,](#page-8-0) whose values are chosen based on an extensive literature review. In the situations where we find multiple parameter estimations, we choose either the worst case scenario (marked with ∗∗) or the average value (unmarked).

The impact of the last three parameters in Table [1](#page-9-0) has been extensively studied in [\[22\]](#page-18-11), being outside the scope of this paper. Relevant studies identify various recurrence rates for the SARS-CoV-2 virus, such as 3 months [\[31\]](#page-18-22), 4–5 months [\[32\]](#page-18-23), 6 months [\[33\]](#page-18-24), and 1 year [\[34\]](#page-19-0). In this study, we adopt a slow-R scenario which translates to a fixed recurrence rate *rRCR* that causes agents to relapse back to *SUS*, on average, in 12 months' simulation time. In terms of quarantine policy, we adopt a react-Q policy which means that agents may be quarantined—with a rate  $r_{ORT}$ —only once after in the  $AWR$  state, when symptoms become visible. For all experiments, except one scenario, we assign the quarantine ratio to a fixed value.

<span id="page-9-0"></span>**Table 1.** Parameterization of the SICARQD epidemic model detailing the values reported in the literature, the values selected in our model, and the relevant references. \*\* Assumed worst-case scenario based on the literature.



All epidemic parameters are kept fixed (except for the *Qpolicy* in one simulation scenario) because the focus of this study is not to analyze the SICARQD model but rather to explore the realism and effectiveness of our urban spatial ABM. We note that in order to adjust the SICARQD model to another virus, it suffices to redefine the seven ratios in Table [1](#page-9-0) according to the available epidemiological data.

#### *3.3. Experimental Setup*

In Table [2,](#page-11-0) we enumerate the input and output parameters which are investigated during the simulation phase. The focus of this paper is to understand the influence of all the ABM parameters on the dynamics of an epidemic outbreak. Note that in order to reduce the complexity of the experiments, some of the parameters are kept fixed at all times, such as the urban area size  $S = 1000 \times 1000$ , the number of infectious seeds  $N_s = 1\%$ A, the agent movement speed  $A_v = 2$ , and the interaction radius with POIs  $\delta_{interact} = 4 \cdot A_v = 8$ .

We define the peak infection ratio  $0 \leq \rho \leq 1$  as the maximum number of daily cases, and it is expressed as a ratio of the total population *A*. To obtain  $\rho$ , we measure  $\rho(t)$  at every time step *t* and keep the maximal value

$$
\rho(t) = \frac{Infected(t)}{A} = \frac{INC(t) + CTG(t) + AWR(t) + QRT(t)}{A}
$$
\n
$$
\rho = max{\rho(t)}
$$
\n(7)

While  $\rho$  quantifies the magnitude of the epidemic, we also measure the total number of cases *τ*, for all simulation times, to obtain a perspective on the ratio between the peak and the duration of an outbreak. We define the ratio *τ* as the total number of susceptible *SUS* agents who become incubating *INC* over all agents in the population:

$$
\tau = \frac{\sum_{t} \{new \ cases\}}{A} = \frac{\sum_{t} \{a_{i} | state(a_{i}(t)) = INC \ & state(a_{i}(t-1)) = SUS\}}{A}
$$
(8)

In some cases where high population mixing allows for rapid contagion, the total cases ratio  $\tau$  may be greater than 1; this means that agents are, on average, infected more than once during the simulation.

<span id="page-10-0"></span>Figure [4](#page-10-0) summarizes the ABM and SICARQD model input parameters, the agent setup phase, and the simulation steps with the end condition.



**Figure 4.** Flow diagram of the experimental setup, from *Start* to *End*. The specific input parameters are fixed for the urban area, the ABM, and the epidemic model. Next, the ABM is created by designating the urban POIs inside the area *S*, placing all *A* agents and assigning their own POIs to visit within the distance *T<sup>d</sup>* ; also, all agents are set as susceptible, except a number of *Ns* agents who are infected to trigger the epidemic outbreak. The simulation phase (gray area) consists of three repeated steps: updating the epidemic state of each agent, updating the position of each agent, and checking the agent interaction (whether inside POI, and transmitting infection to other agents). The process repeats as long as the simulation time *t* ≤ *SIM*\_*T IME*.



<span id="page-11-0"></span>**Table 2.** Input (upper panel) and output (lower panel) parameters for the ABM-SICARQD experimental setup, alongside the model symbols, default value in the model, and range of investigated values through simulation.

#### **4. Simulation Results**

In this section, we present the simulation results according to the experimental flow described in Figure [4](#page-10-0) using the variable ABM input parameters from Table [2](#page-11-0) and the epidemic parameters from Table [1.](#page-9-0) To this end, we investigate 6 values for the agent population *A* ∈ {100, . . . 10,000}, 6 values for the number of urban POIs *P* ∈ {1.. . 1000}, 6 values for the number of agent POIs  $N_p \in \{1...50\}$ , 6 values of maximum travel distances  $T_d \in \{100 \dots 1000\}$ , and 11 values for the quarantine ratio  $r_{ORT} \in \{0, 0.1 \dots 1\}$ . The pairs of simulations are  $(A, P, r_{QRT} = 0.5)$ ,  $(A, N_p, r_{QRT} = 0.5)$ ,  $(A, r_{QRT})$ ,  $(A, T_d, r_{QRT} = 0.5)$ , leading to 174 different scenarios. Each scenario is repeated 100 times and averaged, resulting in 17,400 simulations.

Since the number of numerical results is very high, we summarize all experiments by presenting only the peak infection ratio *ρ* and the total cases ratio *τ* using intuitive plots instead of long tables. An example simulation using our SICARQD epidemic model, with slow-R and a quarantine ratio of  $r_{ORT} = 0.2$ , is depicted in Figure [5.](#page-12-0)

The specific SICARQD infection recurrence is visible in Figure [5a](#page-12-0) as the number of susceptible *SUS* agents increases slowly in time after the initial infection wave; similarly, the number of recovered *REC* agents decreases after having reached a maximum right after the first wave. Furthermore, the three SICARQD specific infectious states and the quarantine state are visible in Figure [5b](#page-12-0). Here, the total number of infected agents (red line) is the sum of all agents in either infected state, including *QRT*. The peak infection ratio *ρ* is the maximum number of infected, namely, the peak of the infection wave; if more waves follow in time, then *ρ* could be updated with a higher value. The three states *INC*, *CTG*, and *AWR* follow quickly one after another as suggested by the vertical dotted lines through the peaks of each wave. Agents in the *QRT* state become visible at the same time with *AWR* because, due to the react-Q policy, an agent may only be quarantined after reaching the *AWR* state and not sooner. Finally, the relatively small quarantine ratio  $r_{ORT} = 0.2$ determines the ratio between  $AWR/QRT = (1 - r_{QRT})/r_{QRT} = 0.8/0.2 = 4$ .

We start by measuring the two output epidemic measures defined in Table [2,](#page-11-0) namely, the peak infection ratio  $\rho$  and the total cases ratio  $\tau$  for an increasing agent population *A*. To put the results into perspective, Figure [6](#page-12-1) plots the epidemic measures for different number of urban POIs *P*. In Figure [6a](#page-12-1), we notice a linear increase from *ρ* ≈ 0–0.6 as the population increases, and are able to differentiate the impact of the total urban POIs *P*. Namely, for very few POIs  $P = 1-25$  the epidemic reaches a higher peak sooner. As the population (density) increases, the results pinpoint towards a strong initial wave (i.e., a peak of *ρ* = 0.5–0.6). In Figure [6b](#page-12-1), we observe an accelerated increase in *τ* up to *A* = 500–1000, then a slower increase towards 100% of the population becoming infected. In the case of very few POIs, we report more than one new case per person on average due to the slow recurrence scenario.

In Figure [7,](#page-13-0) we highlight the importance of POIs in the urban area. Namely, both *ρ* and *τ* drop abruptly as the number of urban POIs increases from *P* = 1–100 and then remain approximately constant regardless of the fact the *P* increases up to 1000 POIs. The initial <span id="page-12-0"></span>drops are plotted in Figure [7a](#page-13-0) as percentages, and increase in magnitude, from 6% to 65%, as the population *A* decreases. This means that for a larger population density, the number of POIs is less impactful on the epidemic intensity. Here, we highlight the results only for a maximum population up to  $A = 2500$  (instead of  $A = 10,000$ ) because the differences above  $A = 2500$  are insignificant in this plot. In panel Figure [7b](#page-13-0), the total cases ratio  $\tau$  follows a very similar trajectory. We note that for  $P = 1000$  POIs, the larger population results in  $\times 21$ more cases than the lowest population.



<span id="page-12-1"></span>of the dynamics of the infected states, highlighting the maximum of the total *infected* as the peak **Figure 5.** The dynamics of an epidemic outbreak using the SICARQD model with slow infection recurrence (slow-R) and a reactive quarantine policy (react-Q). (**a**) The total cases ratio *τ* increases steadily and becomes  $> 1$ , meaning that agents become infected more than once, on average; the similar drop in *REC* and increase in *SUS* is caused by the recurrent infection scenario. (**b**) Detail infection rate *ρ*. A quarantine ratio of  $r_{ORT} = 0.2$  is used, which means that 20% of agents who become *AWR* will be quarantined (i.e., the ratio *AWR*/*QRT* = 4).



**Figure 6.** Impact of the agent population *A* in terms of (a) peak infection ratio  $\rho$  and (b) total cases ratio *τ* for different values of number of urban POIs *P*. In several points, we highlight the percentage difference (%) between the highest and lowest *ρ*. Both plotted epidemic measures show particular linear increases. The highest infection rate is achieved for one single POI per system (blue line), suggesting that very high population concentration favors faster epidemic spreading.

<span id="page-13-0"></span>

**Figure 7.** Impact of the number of urban POIs *P* on the (a) peak infection ratio  $\rho$  and the (b) total cases ratio  $\tau$ , for increasing population sizes  $A = 100...2500$ . The drops from  $P = 1$  to  $P = 100$  are expressed as percentages from the maximum value *ρ*.

<span id="page-13-1"></span>Next, we provide a summary of how the epidemic measures are impacted by the 20% maximum travel distance *T<sup>d</sup>* . In Figure [8,](#page-13-1) we express the distance traveled *Td*%*S* relative to the area *S* (in our case width  $w =$  height *h*). The results prove that  $T_d$  has a significant impact on the increase in both *ρ* and *τ*. In Figure [8a](#page-13-1), the increase in *ρ* starts with *T<sup>d</sup>* = 200, or  $T_d$ %S = 0.2 for the larger population densities, and with 0.4 for the smaller ones. Afterwards, the increase in the peak infection ratio remains linear up to  $T_d$ %  $=$  1. In Figure [8b](#page-13-1), the increase in *τ* is more specific, with an accelerated increase between  $T_d$ % = 0.2–0.4 followed by a stabilization around  $\tau$  = 0.8–1 for higher values of  $T_d$ .



**Figure 8.** Impact of the maximum travel distance *T<sup>d</sup>* (expressed relative to the urban area size *S*) on the (**a**) peak infection ratio *ρ* and the (**b**) total cases ratio *τ*, for different population sizes *A*. Both epidemic measures increase linearly after  $T_d \geq 0.2$  (for larger populations), or after  $T_d \geq 0.4$  (for smaller populations). The highest differences in terms of epidemic measures are calculated around  $T_d = 0.4$ , where higher populations achieve an  $\approx \times 4$ –5 higher infection count.

We further analyze how the number of agent POIs  $N_p$  influences the epidemic outbreak measures (Figure [9\)](#page-14-0). To this end, we find a significant increase in both epidemic measures but especially in the peak  $\rho$  as the number of POIs increases from  $N_p = 1-5$ . The results in Figure [9](#page-14-0) can be corroborated by the results in Figure [7,](#page-13-0) where the epidemic intensity correlates with how well the population is distributed in multiple POIs. Here, when agents have a single POI on their path, the population mixing is highly reduced compared to when agents have five or more POIs to travel to. The increases in *ρ* as *N<sup>p</sup>* increases are depicted



<span id="page-14-0"></span>in Figure [9a](#page-14-0) and range from 157% to 165% (depending on *A*). The total cases ratio *τ* also increases rapidly with the number of agent POIs, as shown in Figure [9b](#page-14-0), and ranges from 97% to 105%.

travel routine, thus rapidly increasing the population mixing. The peak infection ratio *ρ* increases by **Figure 9.** Impact of the number of agent POIs  $N_p$  of each agent  $T_d$  on the (a) peak infection ratio *ρ* and the (**b**) total cases ratio *τ*, for different population sizes *A*. In both panels, we notice a rapid increase from  $N_p = 1$  to  $N_p = 5$ , which translates to an agent visiting more than one place on its over 150% from the initial increase in *N<sub>p</sub>*, while the total cases ratio *τ* increases by ≈100%.

<span id="page-14-1"></span>Since we use the react-Q quarantine policy and the slow-R recurrence scenario in all presented results so far, we further explain the impact of the *Qpolicy* and the quarantine rate  $r_{ORT}$  on the experimental setup. Figure [10](#page-14-1) compares the epidemic dynamics from the perspective of react-Q and proact-Q policies. In Figure [10a](#page-14-1), we show the drop in *ρ* as the quarantine ratio increases and highlight the area  $r_{ORT} = 0.6$ –1, where a rapid drop is noticeable. The measured drop in  $\rho$  is more significant for a higher population (53%) than for a smaller population (8%).



in each panel represent relative decreases in  $r_{QRT}$  between the vertical bars. The decrease in peak **Figure 10.** Impact of the (**a**) proactive and (**b**) reactive quarantine policies given an increasing quarantine ratio *rQRT* on the agent populations *A*. The red vertical bars delimit a visible phase transition area between  $r_{ORT} = 0.6$ –1 (react-Q), respectively  $r_{ORT} = 0.4$ –0.8 (proact-Q). The percentages infection ratio *ρ* is significantly more abrupt, as *rQRT* increases, for the proact-Q policy (79–92%).

In Figure [10b](#page-14-1), the proact-Q underlines the importance of early quarantine, as the peak infection ratio drops sooner and more abruptly than for react-Q. We measure drops in *ρ* of 79–92% for all populations starting with  $r_{QRT} = 0.4$ . Nevertheless, while proact-Q is a more effective epidemic control policy, the real-world effort and costs are much higher than for adopting react-Q. For a full analysis aimed at the impact of patient quarantine and recurrence, please consult our previous study [\[22\]](#page-18-11).

Please note that we do not plot the 95% CI for Figures [6–](#page-12-1)[10](#page-14-1) (or similar statistic) in the results section because it would overload the already detailed plots, and make near lines hard to discern. Nevertheless, all results in Figures [6–](#page-12-1)[10](#page-14-1) present the averages over 100 repeated simulations.

## **5. Discussion and Conclusions**

Agent-based modeling is a powerful tool in computational epidemics for monitoring and managing infectious outbreaks. Unlike similar approaches, such as compartmental models or complex network-based approaches, ABMs can take into account the stochastic nature of human behavior and mobility, producing highly realistic computer-based simulations in dense urban environments [\[12](#page-18-25)[–14](#page-18-12)[,43\]](#page-19-7).

Classic analytical modeling approaches employed in epidemics [\[5,](#page-17-3)[44,](#page-19-8)[45\]](#page-19-9) include a time-dependent transmission rate to model changes in the infection rate caused by viral strain evolution, seasonality, social interactions, or governmental policies. By contrast to the differential equations of the compartmental models applied on the recent COVID-19 pandemic [\[5,](#page-17-3)[44](#page-19-8)[,45\]](#page-19-9), ABMs study models of global mobility mechanisms based on emergent transmission dynamics. In this study, instead of a variable transmission rate, we use simulation on the ABM, resulting in a complex emergent population mixing instead of the compartmental models based on random uniform contact networks that are typically used to study epidemics spreading. Thus, modeling and quantifying human mobility is critical for studying the large-scale spatial transmission of infectious diseases [\[11,](#page-18-4)[13,](#page-18-26)[14\]](#page-18-12).

In this study, we introduce a novel urban spatial agent-based model (ABM) based on the idea that urban points-of-interest (POIs) are hotspots for agent interaction (e.g., transmission of infection, opinion, and innovation) [\[19](#page-18-9)[–21\]](#page-18-10). Therefore, we implement an agent's travel routine as an independent random path from its home location through a number of *N<sup>p</sup>* POIs and back home. To this end, we only verify interaction within POIs and are able to reduce computational complexity considerably, from  $O(A^2)$  to approximately  $O(AP + 0.0036A^2) \approx O(AP).$ 

In addition, we incorporate the SICARQD epidemic model [\[22\]](#page-18-11) to reproduce, analyze, and explain the parameters that affect the dynamics of an infectious outbreak in an urban setting. To showcase the efficiency of our ABM, we employ numerical simulation to measure the influence of urban-demographic parameters on the epidemic spreading based on complex and realistic agent mobility patterns.

We find that the agent population *A* (also interpreted as the population density given the fixed area  $S = 1000 \times 1000[m]$  plays a crucial role in the development of an outbreak. Both the peak infection ratio *ρ* and the total cases ratio *τ* increase linearly with *A*. Moreover, the number of total cases increases more rapidly up to  $A = 500-1000$  then converges linearly towards  $\tau \rightarrow 1$ . If we relate to the real-world context, most metropolises have population densities between 4500 and 8000 inhabitants per  $km^2$  [\[46\]](#page-19-10). By correlation, the density in our ABM is  $A/S^2 = A/(1000[m]x \times 1000[m]) = A[/\text{km}^2]$ . Therefore, for large and dense cities, we notice that the impact of the number of urban POIs *P* is less important than the population *A* (see Figure [6\)](#page-12-1).

A city having a very small number of urban POIs  $(P \leq 25)$  can considerably increase the infection ratio (by 5–65%) as supported by the results in Figure [7.](#page-13-0) Nevertheless, most real-world mid- to large-size cities will have hundreds of POIs [\[19](#page-18-9)[,20\]](#page-18-13) so that the population concentration is more evenly distributed.

The maximum travel distance  $T_d$  determines a delayed linear increase of the infec-tion ratio, as shown in Figure [8.](#page-13-1) For very reduced mobility ( $T_d < 0.2$  of the available city area), the outbreak is mostly inhibited; as the permitted travel distance increases to  $T_d$  = 0.2–0.4, we notice a rapid increase in the outbreak, proportional to the agent population *A*. Moreover, the total cases ratio  $\tau$  presents a phase transition increase between  $T_d$  = 0.2–0.6, earlier for the larger populations and later for the smaller ones.

The number of agent POIs  $N_p$  are used to describe the number and *diversity* of the agent's path. In this sense, we find that if agents are restricted to only one POI (except their home location), the outbreak is significantly reduced, compared to when agents may travel to  $N_p \geq 5$  POIs (see Figure [9\)](#page-14-0). We believe that more agent POIs translate to proportionally higher population mixing, which, in turn, increases the infection ratio. The increases in the peak infection ratio *ρ*, when increasing *N<sup>p</sup>* from 1 to 5, are between 149 and 165%; for the total cases ratio  $\tau$ , the increases are  $\approx$ 100% (i.e., double the number of infections).

Our last analyzed scenario is supported by the mechanics of the SICARQD epidemic model, namely, a comparison between the impact of a reactive (react-Q) and a proactive (proact-Q) quarantine policy. In this sense, Figure [10](#page-14-1) pinpoints that late quarantine react-Q (i.e., based on quarantining patients *after* they become aware of their symptoms) is much less effective than early quarantine proact-Q (i.e., based on quarantining patients preemptively, using contact tracing, and before their symptoms may appear). For react-Q, we measure a slow drop in the infection ratio, more pronounced between  $r_{ORT} = 0.6{\text{-}}1$ , of 8–53%. Conversely, for proact-Q, we measure an abrupt drop in the infection ratio between  $r_{ORT}$  = 0.4–0.8 of 79–92%. Thus, proact-Q can be  $1.7$ –10 $\times$  more effective (depending on population density) in reducing the peak infection ratio *ρ*. Nevertheless, the proact-Q scenario, with a high quarantine ratio, is very difficult to implement in a real context due to the high resource cost.

Overall, we summarize the findings validated through the usage of our urban spatial ABM and the SICARQD epidemic model as follows.

Urban/policy factors which increase the peak infection ratio *ρ* and the total cases ratio *τ*:

- Agent population (*A*)/density (*A*/*S*)—linear increase.
- Maximum permitted travel distance for agents  $(T_d)$ —linear increase but only above  $T_d > 0.2\%S$ .
- Number of agent POIs  $(N_p)$ —logarithmic increase for  $N_p = 1-5$ , then negligible increase after  $N_p > 5$ .

Urban/policy factors which decrease the peak infection ratio *ρ* and the total cases ratio *τ*:

- Number of urban POIs  $(P)$ —logarithmic decrease for  $P = 1$ –100, then negligible decrease after  $P \geq 100$ .
- Ratio of quarantined infected individuals (*rQRT*)—logarithmic decrease, pronounced after  $r_{ORT} > 0.4$ .

Additionally, the nature of the virus will determine the immunization period, modeled as the recurrence scenario in our SICARQD model. A quick-R scenario will increase the infected ratio in time compared to a no-R or slow-R scenario. Also, a proactive quarantine policy will significantly decrease the infection count compared to a reactive policy, for quarantine ratios of  $r_{ORT} > 0.4$ , by 1.7–10 $\times$ , depending on the agent density.

Compared to other classic ABM approaches, such as [\[11,](#page-18-4)[12\]](#page-18-25), which do not employ POIs, our study is able to point out two important aspects of infectious dynamics:

- 1. The epidemic recurrence phenomenon is induced by the emergent agent mobility modeled in our system. More specifically, recovered agents lose their immunity in time (based on either *slow-R* or *quick-R*) and may travel to infected POIs again, and thus, infectious hotspots will be maintained for a very long duration, replicating the residual waves seen after the COVID-19 pandemic started.
- 2. The proactive quarantine (*proact-Q*) in correlation to a higher quarantine ratio (*rQRT*) triggers a phase transition, reducing the total infected population by over 90% (Figure [10b](#page-14-1)) compared to the reactive quarantine (Figure [10a](#page-14-1)). Therefore, a proactive quarantine associated with a strict quarantine ratio can almost completely inhibit infectious spread.

Several limitations of this study are enumerated below. First, the agent model presented is confined to a closed area  $S = w \cdot h$  in order to replicate an urban setting. However,

we plan to extend the ABM so that it can represent multiple *independent* cities, by running parallel simulations, or *interdependent* cities, by allowing a fraction of agents to travel between cities [\[47\]](#page-19-11). Second, all POIs are considered equal and are placed equidistant. The present agent redirection algorithm can use any mapping of POIs, so one can initialize POIs using any spatial distribution. In terms of equal POIs, our model can be augmented by defining specific classes of POIs, with their own maximum occupancy and time spent per agent. Third, we consider all agents identical: they have the same speed, the same number of POIs  $(N_p)$ , and they do not belong to demographic groups (e.g., age and gender). However, our study maintains a generic focus on POIs rather than specific demographic aspects. Nevertheless, the ABM can be further improved to incorporate different individual traits, with different types of POI requirements.

An underestimated element in the adoption of quarantine policies during epidemics is the psychological human factor. We note as possible development directions in our methodology the consideration of the harmful mental effects caused by quarantine protocols [\[48\]](#page-19-12), as well as the natural intervention fatigue of maintaining quarantine strictness over a longer period [\[49\]](#page-19-13).

In addition to the scientific potential of our proposed general purpose, customizable, and computationally efficient ABM framework, our observations find immediate applicability in the ongoing COVID-19 pandemic, as well as foreseeable epidemics with similar airborne transmission. We validate our ABM in the context of epidemic outbreaks, but this model can be further adopted in social physics, or political and environmental sciences. For instance, our ABM can be used to analyze opinion injection strategies and competing influence dynamics [\[50–](#page-19-14)[52\]](#page-19-15), additional vaccination/immunization strategies for viral outbreaks [\[53,](#page-19-16)[54\]](#page-19-17), or political polarization and fake-news dynamics [\[55](#page-19-18)[,56\]](#page-19-19).

We believe that this study has great potential to have a consistent impact in the fields of computational epidemics, mathematical modeling, computer science, and public health by addressing major social and scientific challenges [\[2,](#page-17-4)[3,](#page-17-1)[57,](#page-19-20)[58\]](#page-19-21).

Future research directions may include (i) extending the ABM to a multi-urban model with interdependent cities, (ii) defining POI classes with unique characteristics and requirements, (iii) introducing multiple agent categories with unique mobility patterns and needs, and (iv) updating SICARQD to also model vaccination and tuning the epidemic parameters to custom regions and viruses of scientific interest.

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**Data Availability Statement:** All real-world data used in this study are summarized in Table [1](#page-9-0) and are represented by epidemiological data for the SARS-CoV-2 virus responsible for the COVID-19 pandemic. The parameters were used to tune the introduced SICARQD epidemic model for the experimental setup presented; these parameters were taken from cited resources as follows: incubation rate *rINC* [\[26](#page-18-17)[,35\]](#page-19-1), contagious rate *rCTG* [\[36–](#page-19-2)[38\]](#page-19-3), contagion to symptoms onset *rAWR* [\[35](#page-19-1)[,36\]](#page-19-2), symptoms onset to recovery *rREC* [\[39–](#page-19-4)[41\]](#page-19-5), death ratio *rDED* [\[39](#page-19-4)[,42\]](#page-19-6), quarantine policy *Qpolicy* [\[22](#page-18-11)[,28\]](#page-18-19), quarantine ratio  $r_{ORT}$  [\[22\]](#page-18-11), and recurrence scenario/rate  $r_{RCR}$  [\[31,](#page-18-22)[34\]](#page-19-0).

**Conflicts of Interest:** The authors declare no conflicts of interest.

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