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An Efficient Chameleon Swarm Algorithm for Economic Load Dispatch Problem

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Abstract: Economic Load Dispatch (ELD) is a complicated and demanding problem for power engineers. ELD relates to the minimization of the economic cost of production, thereby allocating the produced power by each unit in the most possible economic manner. In recent years, emphasis has been laid on minimization of emissions, in addition to cost, resulting in the Combined Economic and Emission Dispatch (CEED) problem. The solutions of the ELD and CEED problems are mostly dominated by metaheuristics. The performance of the Chameleon Swarm Algorithm (CSA) for solving the ELD problem was tested in this work. CSA mimics the hunting and food searching mechanism of chameleons. This algorithm takes into account the dynamics of food hunting of the chameleon on trees, deserts, and near swamps. The performance of the aforementioned algorithm was compared with a number of advanced algorithms in solving the ELD and CEED problems, such as Sine Cosine Algorithm (SCA), Grey Wolf Optimization (GWO), and Earth Worm Algorithm (EWA). The simulated results established the efficacy of the proposed CSA algorithm. The power mismatch factor is the main item in ELD problems. The best value of this factor must tend to nearly zero. The CSA algorithm achieves the best power mismatch values of 3.16×10^{-13} , 4.16×10^{-12} and 1.28×10^{-12} for demand loads of 700, 1000, and 1200 MW, respectively, of the ELD problem. The CSA algorithm achieves the best power mismatch values of 6.41×10^{-13} , 8.92×10^{-13} and 1.68×10^{-12} for demand loads of 700, 1000, and 1200 MW, respectively, of the CEED problem. Thus, the CSA algorithm was found to be superior to the algorithms compared in this work.

Keywords: chameleon swarm algorithm; optimization; economic load dispatch; combined emission; economic dispatch



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1. Introduction

The problem of economically allocating the power production of each generating unit and minimizing the emissions of these units is an ongoing challenge for engineers. This has led to the development of the Economic Load Dispatch (ELD) and Combined Economic and Emission Dispatch (CEED) problems. ELD and CEED are among the most complex power system optimization problems. The solution methodology of these complex problems is mostly dependent on metaheuristics [1]. In [2], Gradient-Based Optimizer (GBO) was used for solving ELD, with and without the valve point effect, in addition to CEED. In [3], the authors used a modified version of the Class Topper Optimizer (CTO) algorithm for solving different variants of ELD. In [4], the Turbulent Flow of Water Optimization (TFWO) algorithm was used for solving ELD and CEED. In [5], a hybrid algorithm comprising the Firefly Algorithm (FA) and Bat Algorithm (BA) was used for solving variants of the ELD problem. Simulation results showed that the hybrid algorithm performed better than

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the standalone algorithms. However, the computational cost of the hybrid algorithm is greater than that of the standalone algorithms. In [6], a memory-based Gravitational Search Algorithm (GSA) was used for solving the ELD problem in a micro-grid environment having renewable generation. In [7], authors used Moth Flame Optimization (MFO) for solving the ELD problem considering the valve point effect, wind power, and the load transit conditions. In [8], a novel algorithm considering amalgamation of quantum theory, the Gravitational Search Algorithm (GSA), and Particle Swarm Optimization (PSO) was used for solving the ELD of a power system having photovoltaic generation. When integrated into the algorithm, the quantum theory concepts enhanced the capability. This is due to the fact that, in quantum space, the movement of particles is not restricted and the optimal solution can be found with an even smaller population. In [9], authors proposed the Firefly Algorithm (FA) with a non-homogeneous population for solving different variants of the ELD problem. In [10], the authors proposed an improved version of the Firefly Algorithm (FA) for solving the reserve constrained dynamic ELD problem in multi-area power systems. In [11], a quantum-inspired Bat Algorithm (BA) was used for solving the ELD problem with the valve point effect. In [12], the authors used a Pareto-based PSO for solving CEED. In [13], the authors modelled the ELD problem in the presence of Electric Vehicles (EVs) as a storage medium and solved the problem by reinforcement learning. In [14], authors proposed a novel island-based Harmony Search (HS) algorithm for solving the non-convex ELD problem. In [15], authors proposed an improved directional Bat Algorithm (BA) for solving different variants of the ELD problem. In [16], authors used a modified version of the Krill Herd (MKH) algorithm for solving an ELD problem including nonlinear characteristics of generators. It was observed that the MKH performed relatively well compared to other metaheuristics and that tuning of parameters was also very easy in MKH. In [17], an improved version of symbiosis PSO was proposed for solving the ELD problem. In [18], the authors proposed an improved version of Teaching Learning Based Optimization (TLBO) for solving dynamic ELD considering wind resources and load demand uncertainty. In [19], the authors proposed an evolutionary adaptive Hooke Jeeves algorithm for solving ELD considering the valve point effect. A hybrid algorithm considering amalgamation of PSO with DE was proposed for solving ELD with and without the valve point effect in [20]. In [21], authors applied Ant Colony Optimization (ACO) for solving ELD in the case of an IEEE 26 bus test system considering the valve point effect. In [22], authors applied oscillatory PSO for solving ELD with multiple fuel options. A hybrid GA and fish swarm algorithm was used for solving ELD with multiple fuel and valve point effects in [23]. It was observed that the hybrid algorithm performed better than the standalone algorithms when applied to the ELD problem.

From references [2–23], it can be concluded that researchers have used a number of metaheuristics, such as BA, FA, PSO, CTO, GSA, and MFO, for solving the complex and demanding problem of ELD. Regardless of the application of various metaheuristics for addressing the ELD problem, researchers continue to seek and develop new and novel methods for its solution. The superb inspiration driving this is the No Free Lunch (NFL) hypothesis [24–28]. The NFL hypothesis expresses that a single algorithm does not perform equally well when applied to all enhancement issues. Henceforth, it is a legitimate goal to propose new, more proficient methods and improve the existing techniques. Thus, the current study proposes a novel Chameleon Swarm Algorithm (CSA) for solving the ELD problem. CSA is a novel algorithm proposed by Braik in 2021 that mimics the hunting and food searching mechanism of chameleons [29].

The main items of this work are as follows:

- Discussion of the problems of economic load dispatch (ELD) and the combined emission and economic dispatch (CEED) for a six-unit network system.
- The Chameleon Swarm Algorithm (CSA) is used as a new metaheuristic technique for the two case studies.
- Minimizing the fuel cost is the main item in the objective function in the ELD problem.

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• Minimizing the fuel cost and emission cost are the main items in the objective function in the CEED problem.

- A comparison between the proposed CSA method and other algorithms, such as the Sine Cosine Algorithm (SCA), Grey Wolf Optimization (GWO), and Earth Worm Algorithm (EWA), is undertaken for the two case studies.
- The performance of all algorithms is measured according to the power mismatch factor in the ELD and CEED problems.
- The maximum, mean, minimum, and standard deviation values of 30 independent runs were examined as statistical analyses for all applied algorithms.

The paper is organized as follows: the ELD and CEED problems are analyzed in Section 2. Section 3 discusses the chameleon swarm algorithm. The numerical analysis of the results is discussed in Section 4. Section 5 presents the conclusion and discusses future work.

2. Economic Load Dispatch Problem

Power system operation is subject to a number of problems; one of these is the ELD problem. Minimizing fuel consumption cost is the main issue in the optimization of the ELD problem to maximize the benefit economic of the power system. The main variable in the ELD problem is the allocating vector of each unit that specifies the optimal production for each unit in the system. Section 2.1 discusses ELD with losses and Section 2.2 discusses combined economic and emission dispatch (CEED).

2.1. ELD

The mathematical modeling of ELD with losses is clarified in this section. The operating cost of fuel consumption of *n* generators is:

$$Min(F) = F_1(P_1) + \cdots + F_n(P_n) \tag{1}$$

where F is the total fuel cost, F_1 is the cost of fuel for the 1st generator, and F_n is the cost of fuel for the nth generator. The fuel consumption cost function is estimated in quadratic form as:

$$Min(F) = \sum_{k=1}^{n} F_i(P_i) = \sum_{k=1}^{n} a_k P_k^2 + b_k P_k + c_k$$
 (2)

where *c*, *b*, *a* are the fuel cost weight constants.

The generator constraints of each unit are given by Equations (3) and (5):

$$\sum_{k=1}^{n} P_k - P_D - P_L = 0 \tag{3}$$

where P_D signifies total network demand and P_L represents the network transmission losses.

$$P_L = \sum_{i=1}^{n} \sum_{j=1}^{n} P_i B_{ij} P_j \tag{4}$$

where B_{ij} is the loss factor, P_i is the power generated by the *i*th generator, and P_j is the power generated by the *j*th generator.

$$P_k^{min} \le P_k \le P_k^{max} \tag{5}$$

2.2. CEED

The ELD problem is further developed by taking the reduction of emissions into consideration with the production cost; this is then called the CEED problem. Minimizing fuel cost is aligned with minimizing the emissions. Similarly, minimizing the emissions is aligned with minimizing the fuel cost.

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The CEED problem is concerned with the minimization of the gases from power plants. The factor of emission is specified by:

$$Min(E) = \sum_{k=1}^{n} E_i(P_i) = \sum_{k=1}^{n} \alpha_k P_k^2 + \beta_k P_k$$
 (6)

The CEED problem fitness function is:

objective function =
$$Min\left(\sum_{k=1}^{n} E_i(P_i) + h_e \sum_{k=1}^{n} F_i(P_i)\right)$$
 (7)

where h_e is the penalty factor of price, as shown in Equation (8):

$$h_e = \frac{F_i(P_{imax})}{E_i(P_{imax})} \tag{8}$$

The generator constraints of each unit are given by Equations (3) and (5).

3. Chameleon Swarm Algorithm (CSA)

CSA is one of the most recent metaheuristics and was proposed by Braik in 2021. This algorithm mimics the hunting and food searching mechanism of chameleons [29]. Chameleons are a highly specialized class of species, having the ability to change color to mix in with their surrounding environment [29]. Chameleons have the capacity to live and survive in lowlands, mountains, deserts, and semi-desert areas, and generally eat insects [29]. Their food hunting process involves a number of steps, such as tracking the prey, pursuing the prey using their sight, and attacking the prey, as shown in Figure 1. The mathematical models and steps of this algorithm are explained in the subsequent sub-sections.



Figure 1. Steps of CSA.

3.1. Initialization and Function Evaluation

CSA is a population-based metaheuristic that randomly generates an initial population to start the process of optimization. The chameleon population with size n is generated in a d dimensional search area, where each individual of the population is a possible solution

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to the optimization problem. The chameleon position at any iteration in the search area is characterized by Equation (9):

$$y_t^i = \left[y_{t,1}^i, y_{t,2}^i, \dots, y_{t,d}^i \right] \tag{9}$$

where $i = 1, 2 \dots$ t represents the count of iteration, $y_{t,d}^i$ represents the position of chameleon. The initial population is generated based on the problem dimension and the number of chameleons in the search space as shown in Equation (10):

$$y^i = l_j + r(u_j - l_j) \tag{10}$$

where y^i is the initial vector of the ith chameleon, u_j and l_j refer to the upper and lower limits of the search space, respectively, and r is a random uniformly number ranging from 0 to 1. The solution quality in each step is measured for each new position on the basis of the evaluation of the objective function.

3.2. Search of Prey

The chameleons' movement behavior during searching can be characterized based on the updating strategy of position, as in Equation (11):

$$y_{t+1}^{i,j} = \begin{cases} y_t^{i,j} + P_1 \left(P_t^{i,j} - G_t^j \right) r_2 + P_2 \left(G_t^j - y_t^{i,j} \right) r_1 \\ y_t^{i,j} + \mu \left(u^j - l^j \right) r_3 + l_b^j sgn(rand - 0.5) r_1 < P_p \end{cases} r_1 \ge P_p$$
 (11)

where t and (t+1) indicate the tth and (t+1)th iteration step, respectively. i and j represent the ith chameleon in the jth dimension. $y_t^{i,j}$ and $y_{t+1}^{i,j}$ are the current and new positions, respectively, of the chameleon. $P_t^{i,j}$ and G_t^j imply the best and global best positions of the chameleon, respectively.

Where, P_1 and P_2 are two positive numbers that control exploration ability. r_1 , r_2 , and r_3 are random uniformly numbers created and ranging from 0 to 1. r_i is a random uniformly number created at index i ranging from 0 to 1. P_p indicates the probability of the chameleon perceiving prey. sgn(rand - 0.5) has an effect on the direction of exploitation and exploration, and can be either -1 or 1. μ is a function of iterations parameter that reduces with the number of iterations.

3.3. Chameleon's Eyes Rotation

Chameleons possess the capacity to identify the position of the prey by rotating their eyes. This rotational feature assists them to spot the prey through 360 degrees [21]. The accompanying steps happen in the following manner:

- The first position of the chameleon is the focal point of gravity (i.e., the beginning);
- The rotation matrix is discovered that recognizes the position of the prey;
- The situation of the chameleon is refreshed utilizing the rotation matrix at the focal point of gravity;
- Finally, the chameleons are returned to the first position

3.4. Hunting Prey

Chameleons assault their prey when it comes excessively close. The chameleon that is nearest to the prey is the optimal chameleon, and is viewed as the best result. This chameleon assaults the prey by utilizing its tongue. The situation of the chameleon is improved because it can extend its tongue by twice its length. This helps the chameleon to take advantage of the pursuit space, and allows it to adequately snatch prey [21]. The speed of a chameleon's tongue when it is extended toward prey can be numerically demonstrated by Equation (12):

$$v_{t+1}^{i,j} = wv_t^{i,j} + c_1 \left(G_t^j - y_t^{i,j} \right) + c_2 \left(P_t^{i,j} - y_t^{i,j} \right) r_2 \tag{12}$$

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where $v_{t+1}^{i,j}$ indicates the new velocity of the *i*th chameleon in the *j*th dimension of iteration t+1, and $v_t^{i,j}$ indicates the current velocity of the *i*th chameleon in the *j*th dimension.

4. Numerical Analysis of Results

The performance of CSA for two scenarios of ELD was examined. The proposed CSA algorithm was compared with Grey Wolf Optimization (GWO), Sine Cosine Algorithm (SCA), and Earth Worm Algorithm (EWA) for the same two case studies. Table 1 describes the two case studies used to compare the proposed CSA with the other algorithms. The general and private settings for all algorithms are reported in Table 2. The independent runs were performed on MATLAB R2015b software and Intel(R) Core(TM) i7-4600U CPU @ 2.10 GHz–2.70 GHz hardware with Windows User 10 Pro and 8 GB RAM.

Table 1. Cases of the tested networks.

Item	Problem	Test Network	Load (MW)
			1200
1	ELD	6	1000
		-	700
			1200
2	CEED	6	1000
		-	700

Table 2. Algorithms' specific parameter settings.

Algorithms	Parameter Values
Common parameters	Size of population: $N = 30$ Number of iterations is 1000
CSA	p_1 , p_2 , ρ , c_1 , c_2 are equal to 0.25, 1.50, 1.0 1.75, 1.75, respectively.
GWO	a decreases linearly from 2 to 0
SCA	A = 2
EWA	$A = 0.98$, $\beta_0 = 1$, and $\gamma = 0.9$

4.1. Results of the ELD Problem

The network system of six generator units with several demand loads, as shown in Table 1, was used to solve the ELD problem based on several optimization algorithms, namely, the CSA, SCA, GWO, and EWA algorithms. The comparison between all algorithms was performed based on 30 independent runs. Table 3 presents the statistical analysis, showing the standard deviation, minimum, mean, and maximum of the objective function for all algorithms based on the 30 independent runs for all demand loads. Based on this table, the proposed CSA algorithm achieved the best objective function and standard deviation for all cases. Thus, CSA is more reliable and has higher accuracy than the other competitor algorithms. The best fuel consumption cost for all demand loads and the best objective function for all algorithms is reported in Table 4. The allocation vector of each unit in the network system based on the best fitness function is reported in Tables 5–7, for demand loads of 700, 1000, and 1200 MW, respectively. Based on these results, the proposed CSA algorithm achieved the best fuel consumption cost for all demand cases. The order of algorithms based on the best cost is CSA, GWO, SCA, and EWA for all demand cases. The convergence and robustness curves for all algorithms over 30 independent runs are shown in Figures 2-4, for demand levels of 700, 1000, and 1200 MW, respectively. Based on these figures, the CSA reached the optimal solution faster than the other algorithms. The convergence and robustness curves indicate the solution achieved by the proposed CSA algorithm was the global optimal solution for ELD problem.

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 $\textbf{Table 3.} \ \textbf{Statistical analysis of objective function for case 1}.$

Load (MW)	Technique	Min	Mean	Max	SD
	CSA	8528.091975	8922.841673	9093.525189	133.4072202
700	GWO	554,192.147	8,523,819.629	29,793,196.04	7,437,182.379
700	SCA	7,680,621.197	69,654,953.61	203,722,478.8	42,769,492.03
	EWA	14,863.57446	46,501,446.523	196,465,481.6	57,752,646.53
	CSA	12,120.08172	12,311.32929	12,695.87285	115.7916315
1000	GWO	495,091.3593	12,418,496.27	39,059,487.38	9,946,760.603
1000	SCA	1,836,263.786	126,730,461.9	620,534,587.7	122,987,260.2
	EWA	44,518.42105	25,701,303.152	156,109,230.1	37,277,321.51
	CSA	14,846.46878	14,964.33727	16,640.51747	319.5243805
1200	GWO	3,089,864.26	15,978,305.46	119,976,210.6	21,625,976.95
1200	SCA	15,376,807.46	199,191,415.2	608,076,225.3	157,173,566.8
	EWA	14,915.7328	71,604,765.525	564,214,908.2	121,880,902.4

 $\textbf{Table 4.} \ \ \text{Best fuel cost in \$ per hour for various load settings of case 1.}$

Technique	700 MW	1000 MW	1200 MW
CSA	8528.091869	12,120.04448	14,846.46878
GWO	8602.008494	12,363.08738	14,865.77008
SCA	8717.700902	12,370.84528	14,962.38136
EWA	9540.807338	14,612.63001	17,447.40468

Table 5. Vector of allocation for the best objective function for all techniques of case 1 at demand of 700 MW.

CSA	GWO	SCA	EWA
201.2535201	165.20543	163.4754609	57.01527783
129.4000937	126.7615129	94.97953739	75.0047139
154.2857039	200.0201434	151.0967108	91.00020071
71.30891756	69.4678662	150	116.0167198
98.34085361	101.459958	84.37601099	124.0000002
57.66734009	50	69.14598368	248.4968272

Table 6. Vector of allocation for the best objective function for all techniques of case 1 at demand of 1000 MW.

CSA	GWO	SCA	EWA
403.4372818	500	273.3437231	56.00029022
142.9644621	151.23974	112.4433126	84.00042386
244.1627946	80.9641118	300	102.0006046
66.55584622	97.7893247	79.70060918	143.6741356
116.3668887	139.896394	141.6622318	149.0010695
50.00013166	52.367134	120	486.9954158

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Table 7. Vector of allocation for the best objective function for all techniques of case 1 at demand of 1200 MW.

CSA	GWO	SCA	EWA
467.1166529	456.069504	500	51.02070233
192.0406171	160.473756	169.2380267	105.9965483
231.0401614	264.875181	300	132.0054405
126.9090868	138.920676	139.6603993	180.963024
147.2057156	109.351234	50	276.8977415
69.81050052	104.7556989	74.15460988	486.8740064

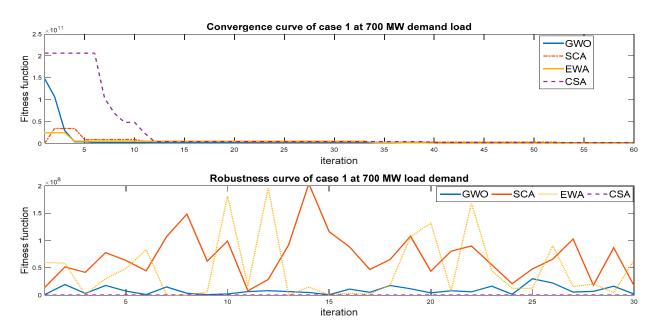


Figure 2. Convergence and robustness behavior using all techniques for case 1 at demand load of 700 MW.

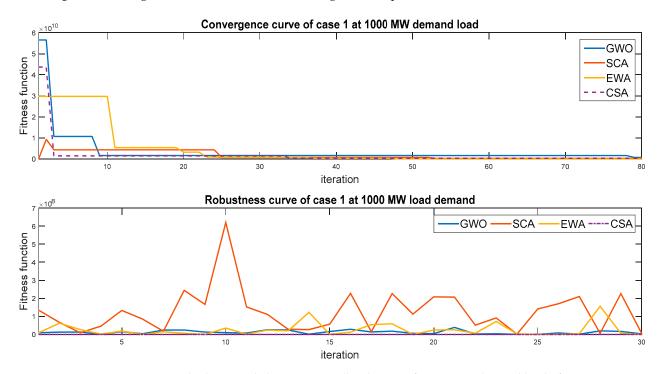


Figure 3. Convergence and robustness behavior using all techniques for case 1 at demand load of 1000 MW.

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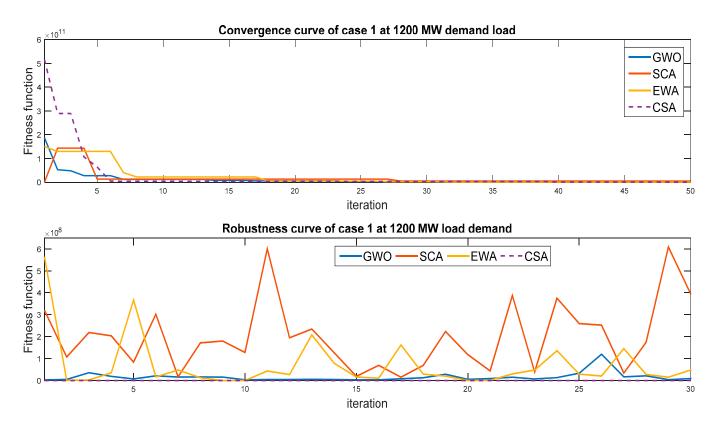


Figure 4. Convergence and robustness behavior using all techniques for case 1 at demand load of 1200 MW.

4.2. Results of CEED Problem

The network system of six generator units with several demand loads, as shown in Table 1, was used to solve the CEED problem based on several optimization algorithms, namely, the CSA, SCA, GWO, and EWA algorithms. The comparison between all algorithms was performed based on 30 independent runs. Table 8 presents the statistical analysis and shows the standard deviation, minimum, mean and maximum of the objective function for all algorithms based on the 30 independent runs for all demand loads. Based on this table, the proposed CSA algorithm achieved the best objective function and standard deviation for all cases. Thus, CSA is more reliable and has higher accuracy than the other competitor algorithms. The best fuel consumption cost for all demand loads and the best objective function for all algorithms is reported in Table 9. The allocation vector of each unit in the network system based on the best fitness function is reported in Tables 10–12, for demand levels of 700, 1000, and 1200 MW, respectively. Based on these results, the proposed CSA algorithm achieved the best fuel consumption cost for all demand cases. The order of algorithms based on the best cost is CSA, GWO, SCA, and EWA for all demand cases. The convergence and robustness curves for all algorithms over 30 independent runs are explained in Figures 5-7, for demand levels of 700, 1000, and 1200 MW, respectively. Based on these figures, the CSA reached the optimal solution faster than the other algorithms. The convergence and robustness curves indicate the solution achieved by the proposed CSA algorithm is the global optimal solution for the CEED problem.

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Table 8. Statistical analysis of the objective function for case 2.

Load (MW)	Technique	Min	Mean	Max	SD
	CSA	13,740.19426	15,341.954	16,374.91585	673.5762317
700	GWO	99,263.42118	8,823,549.782	32,618,509.3	8,180,728.243
700	SCA	1,299,372.036	58,806,922.34	268,245,016.9	70,125,512.69
	EWA	94,898.9244	36,933,381.1603	132,342,809.9	34,411,120.3
	CSA	21,612.42374	22,386.89567	23,771.54396	526.6885085
1000	GWO	491,868.4754	10,247,754.87	43,428,023.49	9,546,163.002
1000	SCA	12,621,456.9	87,188,746.09	305,519,608.7	64,964,750.28
	EWA	70,176.0552	12,601,434.865	46,743,568.71	14,550,469.21
	CSA	27,972.52315	28,378.16957	30,238.11598	430.7763349
1200	GWO	3,103,205.769	15,991,735.76	119,989,397.5	21,625,919.36
1200	SCA	15,390,677.52	199,205,138	608,090,433.9	157,173,553.9
	EWA	33,465.88848	78,645,451.7863	448,031,794.3	113,944,006.1

Table 9. Best fuel and emission costs in \$ per hour for various load settings of case 2.

Tashmiana	700 I	MW	1000	MW	1200	MW
Technique	Fuel	Emission	Fuel	Emission	Fuel	Emission
CSA	8462.268917	6792.11394	12,139.60382	10,527.9799	14,856.97546	15,211.91134
GWO	8907.148297	12,152.50578	12,260.97086	8748.43968	14,865.77008	16,562.15696
SCA	9066.659657	4136.630696	12,237.98949	9363.736686	14,962.38136	18,113.98812
EWA	9368.5485	10,248.42837	13,633.57578	22,746.5453	16,837.91299	42,558.60192

Table 10. Vector of allocation for the best objective function for all techniques of case 2 at demand of 700 MW.

CSA	GWO	SCA	EWA
258.0083211	115.216131	117.2751813	53
50.00000869	75.731398	200	84
167.3337086	300	80	109
106.613021	103.905314	50	135
73.44096019	67.6531736	200	158
56.5684972	52.354702	67.13006412	175

Table 11. Vector of allocation for the best objective function for all techniques of case 2 at demand of 1000 MW.

CSA	GWO	SCA	EWA
400.4399359	376.513695	394.8204572	78.0000557
140.5499372	200	157.0376964	94.17467563
195.0348613	137.696695	131.0117043	133.9999977
119.3390882	74.5127265	140.4159948	164.4652813
98.24778751	135.028378	119.2275839	265.4122572
69.56091425	100.274265	81.11261153	290.2872253

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Table 12. Vector of allocation for the best objective function for all techniques of case 2 at demand of
1200 MW.

CSA	GWO	SCA	EWA
480.1323819	456.069504	500	87.99845176
171.3582298	160.473756	169.2380267	138.4838263
266.9421588	264.875181	300	154.9963726
78.28987273	138.920676	139.6603993	170.9819546
152.5502456	109.351234	50	249.9359313
85.07538079	104.7556989	74.15460988	432.8298403

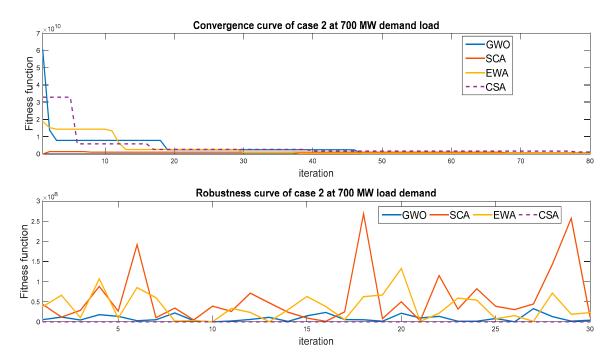


Figure 5. Convergence and robustness behavior using all techniques for case 2 at demand load of 700 MW.

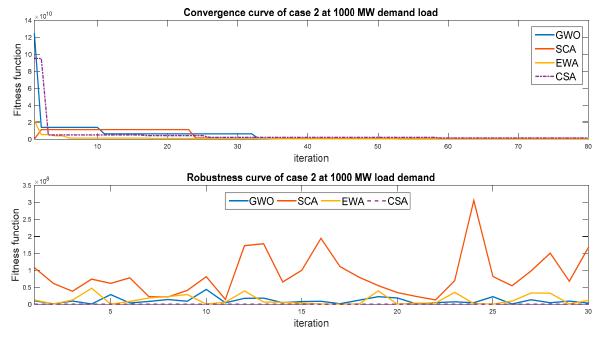


Figure 6. Convergence and robustness behavior using all techniques for case 2 at demand load of 1000 MW.

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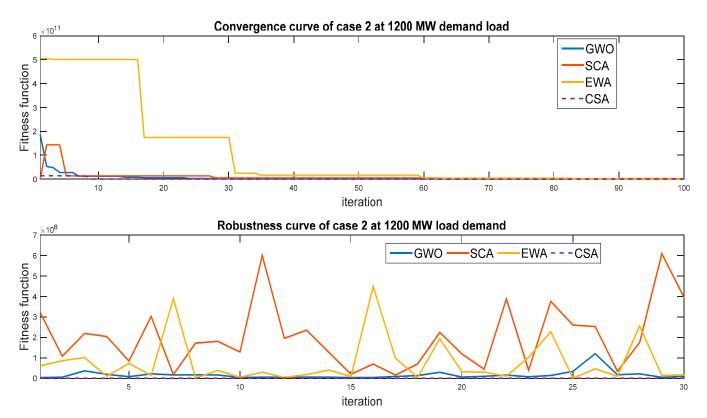


Figure 7. Convergence and robustness behavior using all techniques for case 2 at demand load of 1200 MW.

4.3. Discussion of Results

The power mismatch factor is the main factor in the ELD problems. This can be expressed by the absolute error between two terms; the first term is the sum of transmission losses and the load demand, and the second term is the sum of power generated by each unit in the system. The best value of this factor must tend to nearly zero. Based on the data identified from all algorithms, the power mismatch factor was calculated. The value of this factor is illustrated in Table 13 for the two cases used in this work. Based on this recorded data, the CSA technique achieved the best power mismatch factor compared to the GWO, SCA, and EWA algorithms.

Table 13. The power mismatch value for all cases

Cases	Algorithm	700 MW	1000 MW	1200 MW
Case 1 -	CSA	3.16×10^{-13}	4.16×10^{-12}	1.28×10^{-12}
	GWO	5.46×10^{-5}	4.83×10^{-5}	3.07×10^{-4}
	SCA	0.00076719	1.82×10^{-4}	1.54×10^{-3}
	EWA	5.71	20.1	23.4
Case 2 —	CSA	6.41×10^{-13}	8.92×10^{-13}	1.68×10^{-12}
	GWO	8.38×10^{-6}	4.7×10^{-5}	3.07×10^{-4}
	SCA	0.000128351	0.001259941	0.001536185
	EWA	2.164245	9.051048781	17.36856684

5. Conclusions

ELD is a complicated problem in the optimization of power systems. This work validates the performance of the Chameleon Swarm Algorithm (CSA) in solving different

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cases of ELD. CSA is one of the most recently developed metaheuristics, and mimics the food hunting process of chameleons. CSA has an excellent balance between exploration and exploitation, and favors faster convergence. In the current study, the performance of CSA was compared with that of several metaheuristic algorithms, namely, GWO, SCA, and EWA, in solving CEED and ELD for a six unit system. It was found that CSA performed well compared to other state-of-the-art metaheuristics and favored a faster convergence. The proposed CSA algorithm achieved the best objective function and standard deviation for all cases of CEED and ELD for a six unit system. Thus, CSA is more reliable and has higher accuracy than the other competitor algorithms. The CSA technique achieved the best power mismatch factor in solving CEED and ELD for a six unit system compared to the GWO, SCA, and EWA algorithms.

Future research will focus on the following aspects:

- Improvement and hybridization of CSA;
- Using CSA for solving other complex power system optimization problems; for example, unit commitment and hydro-thermal scheduling.

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