

## Article

# A Wavelet Analysis of the Dynamic Connectedness among Oil Prices, Green Bonds, and CO<sub>2</sub> Emissions

Nini Johana Marín-Rodríguez <sup>1,\*</sup>, Juan David González-Ruiz <sup>2</sup> and Sergio Botero <sup>3</sup>

<sup>1</sup> Programa de Ingeniería Financiera, Facultad de Ingenierías, Universidad de Medellín, Medellín 050026, Colombia

<sup>2</sup> Departamento de Economía, Facultad de Ciencias Humanas y Económicas, Universidad Nacional de Colombia, Sede Medellín, Medellín 050034, Colombia

<sup>3</sup> Departamento de Ingeniería de la Organización, Facultad de Minas, Universidad Nacional de Colombia, Sede Medellín, Medellín 050034, Colombia

\* Correspondence: njmarin@udemedellin.edu.co

**Abstract:** Wavelet power spectrum (WPS) and wavelet coherence analyses (WCA) are used to examine the co-movements among oil prices, green bonds, and CO<sub>2</sub> emissions on daily data from January 2014 to October 2022. The WPS results show that oil returns exhibit significant volatility at low and medium frequencies, particularly in 2014, 2019–2020, and 2022. Also, the Green Bond Index presents significant volatility at the end of 2019–2020 and the beginning of 2022 at low, medium, and high frequencies. Additionally, CO<sub>2</sub> futures' returns present high volatility at low and medium frequencies, expressly in 2015–2016, 2018, the end of 2019–2020, and 2022. WCA's empirical findings reveal (i) that oil returns have a negative impact on the Green Bond Index in the medium term. (ii) There is a strong interdependence between oil prices and CO<sub>2</sub> futures' returns, in short, medium, and long terms, as inferred from the time–frequency analysis. (iii) There also is evidence of strong short, medium, and long terms co-movements between the Green Bond Index and CO<sub>2</sub> futures' returns, with the Green Bond Index leading.

**Keywords:** co-movements; dependence; wavelet analysis; oil prices; green bonds; CO<sub>2</sub> emissions; bibliometric analysis



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## 1. Introduction

The inclusion of oil prices in the analysis of the environmental context comes from the substitution and income effect caused by any change in the product price relative to its demand function (Barsky and Kilian 2004; Hamilton 1983; Kilian 2009). The substitution effect occurs when goods get cheaper, and this generates incentives to consume more of the cheaper goods and less of the expensive ones. On the other hand, the income effect occurs when the price of the goods falls and the purchasing power increase, causing a result similar to a rise in income. This theory is called the Slutsky-Hicks Theory (Allen 1950). In this way, oil price shocks can affect carbon emissions and green bond issuances through changes in fossil fuel consumption. For instance, the sharp decline in oil prices during 2014–2015 increased carbon emissions due to the relatively more expensive clean energy projects (Kassouri et al. 2022, 2021). In this context, a fall in oil prices obstructs carbon mitigation initiatives as green bonds promote them (Kassouri et al. 2022).

With the implementation of the European Union Emissions Trading System (EU ETS) in January 2005, EU Allowances (EUAs) became a tradeable asset that could be negotiated in organized spot, futures, and options markets (Reboredo 2013). Likewise, in January 2014, the International Capital Markets Association (ICMA) published the Green Bond Principles (GBP) to establish the rules for a bond to be labeled green. Since then, investors have at their disposal information to enable them to discern the environmental benefits of their

fixed-income investments against alternative investments (Mejía-Escobar et al. 2021; Reboredo 2018). Thus, green bonds are a well-established sustainable investment instrument that has been gaining popularity among (i) investors, especially environmentally-conscious investors, (ii) companies concerned about climate-related risk exposition and the opportunities of financing their eco-friendly projects, and (iii) governments for the potential influence of green bonds on their climate change policies (Reboredo 2018).

Numerous studies evidence the relationship between (i) oil prices and green bonds (Azhgaliyeva et al. 2022, 2021; Dutta et al. 2021; Lee et al. 2021; Reboredo and Ugolini 2020; Saeed et al. 2021; Su et al. 2022), (ii) oil prices and CO<sub>2</sub> emissions (Alhodiry et al. 2021; Ali et al. 2022; Habib et al. 2021; Maji et al. 2020; Mensah et al. 2019; Mujtaba and Jena 2021; Sadorsky 2009; Wen et al. 2017; Zhang and Zhou 2022; Zou 2018), and (iii) green bonds and CO<sub>2</sub> emissions (Jin et al. 2020; Lichtenberger et al. 2022; Nenonen et al. 2019; Rannou et al. 2021; Ren et al. 2022a; Tiwari et al. 2022; Wang et al. 2022).

However, a knowledge gap has been identified despite all the advances in studying the previously mentioned relationships with other financial assets; just a few recent studies in the current literature have provided an in-depth analysis of the co-movements among the green bonds, CO<sub>2</sub> emissions, and oil prices simultaneously (Li et al. 2022; Marín-Rodríguez et al. 2022b). These two studies provide an important foundation for our paper. Furthermore, by using wavelets, we contribute to the debate on the dependences among green bonds, CO<sub>2</sub> emissions, and oil prices simultaneously, conducting a time-frequency analysis of the dependence among these three variables. Moreover, we emphasize the economic and policy implications of the results obtained. Additionally, we make a novel extension to the existing literature focusing on clean energy stocks and other financial markets.

For example, Li et al. (2022) found that oil price has a negative effect on the Green Bond Index and that carbon prices positively influence the Carbon Efficiency Index in the short and medium term. Additionally, the Green Bond Index positively affects carbon prices in the short and medium term and negatively impacts the Carbon Efficiency Index. In addition, carbon price shocks positively affect the Carbon Efficiency Index in the short and medium term. Furthermore, Marín-Rodríguez et al. (2022b) using Granger Causality and DCC-GARCH methodologies, observed a unidirectional causality running from the Green Bond Index to the Brent oil returns and a unidirectional causality running from the Green Bond Index to the CO<sub>2</sub> futures' returns and a unidirectional causality running from the Brent oil returns to the CO<sub>2</sub> futures' returns. Also, their results for DCC-GARCH indicate a positive dynamic correlation between the Brent oil price return and the CO<sub>2</sub> futures' returns and a negative dynamic correlation between the Green Bond Index concerning the oil return and the CO<sub>2</sub> futures' returns, presenting a solid correlation in uncertainty periods. Thus, a deeper analysis of this concern will lead to a better comprehension of the evolution and co-movements of these three variables in a global decarbonization scenario.

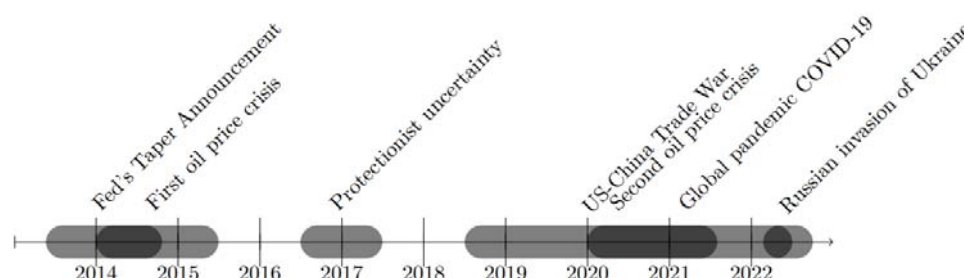
This research is aimed at quantifying such co-movements identifying their effects on different time periods, and how this relationship varies according to the economic conditions. Thus, this paper makes two substantial contributions to the existing body of knowledge and practice. First, this study is the first to incorporate a scientometric analysis of dynamic co-movements among oil prices, green bonds, and CO<sub>2</sub> emissions with particular emphasis on measuring different time period relationships, limiting the search equation to the existence of co-movements, contagion, or dependence among the variables. Second, it provides new evidence by examining the dynamic relationship among crude oil prices, CO<sub>2</sub> futures' price, and green bonds using a wavelet coherence approach to determine the effects of oil price shocks on CO<sub>2</sub> emissions and green bonds issuances over different time frequencies: short, middle, and long-term. In addition, this study analyzes whether the correlation changes over different scales in the period studied 2014–2022. Thus, this study's outcomes can help researchers, managers, policymakers, and decision-makers to understand the importance of the oil price shocks on the design of assets and policies that tend to improve sustainability practices.

The paper's outline is as follows: Section 2 studies the background and bibliometric analysis of asset market linkages among oil prices, green bonds, and CO<sub>2</sub> emissions. Section 3 presents the data, the descriptive statistics, and the methodologies used. Section 4 analyzes the results. Section 5 discusses the empirical results. Finally, in Section 6, some concluding remarks are offered.

## 2. Context of the Analysis and Literature Review

### 2.1. Context of the Analysis

For the selected analysis period, 2014–2022, some different exogenous shocks or crises could have caused rupture or change among the linear relationships of financial assets considered in this study. As a starting point, the financial shocks definition by [Beirne and Gieck \(2014\)](#) will be used. This definition states that they are turbulences in asset markets in advanced and emerging economies that affect other international financial markets. Figure 1 presents the timeline of the main common financial shocks. The first event is the Federal Reserve's Rate reduction announcement (known as the FED's Taper Announcement), which caused a fall in the prices of financial assets, an increase in volatility, and a decrease in trade volumes and market liquidity, as well as a rise in a government bond, spreads between the end of May and August 2014 at the height of the market turmoil. Later, the first oil price crisis emerged in 2014 and then in 2016. Subsequently, focusing the analysis on a specific region such as Latin America, several events in the region were affected by protectionist uncertainty in its emerging markets, especially Mexico, due to its strong financial and commercial links with the rest of the world, particularly with the United States. Such uncertainty started with the presidential campaign in the United States when the financial markets reflected the tension during each presidential debate. For example, when investors thought the then-candidate Trump would win, the market would drop; and when candidate Clinton seemed most likely to win, markets rose. This was especially reflected in the fluctuation of the financial markets.



**Figure 1.** Timeline of principal common financial shocks, 2014–2022. Source: Author's own research.

In addition to that scheme, other events have caused imbalances in financial assets, not only in Latin America but also globally, such as the trade war between China and the United States that began in March 2018 after Donald Trump announced the tariff imposition of 50,000 million dollars on Chinese products. In response to those actions, the government of the People's Republic of China applied tariffs on numerous American products.

A dispute in which the World Trade Organization (WTO) had to intervene to reduce tensions arose. Afterward, the global crisis caused by the COVID-19 virus pandemic (an acronym for coronavirus disease, 2019) occurred. It originated in China in December 2019. After it spread to different countries, on 11 March 2020, it was declared a global pandemic by the World Health Organization (WHO). The virus's expansion has generated economic and social uncertainty, which has influenced the global financial and economic markets, generating losses. Those are difficult to quantify even today, given that the pandemic has not yet been overcome. Additionally, it is necessary to mention that during this global pandemic, there has been a second crisis in oil prices; The member countries of OPEC (Organization of Petroleum Exporting Countries) have decided to cut production due to the sharp drop in crude oil prices, the decline in demand and the substantial volatility. Finally,

the recent Russian invasion of Ukraine on 24 February 2022 is bringing consequences in a range of areas, mainly: (i) humanitarian crisis, (ii) food security crisis, and (iii) energy volatility crisis.

## 2.2. Literature Review

This research includes a scientometric review of the leading studies about the dynamic relationships among oil prices, green bonds, and CO<sub>2</sub> emissions. The documents reviewed were obtained from the Scopus and Web of Science (WoS) bibliographic databases. The research equation was: (TITLE-ABS-KEY (“oil prices\*” OR “oil-price\*” OR “crude oil” OR “crude-oil”) AND TITLE-ABS-KEY (CO<sub>2</sub> OR “CO<sub>2</sub> emission\*” OR “carbon dioxide emission\*” OR “carbon emission\*” OR “emission\* CO<sub>2</sub>” OR “green bond\*”) AND TITLE-ABS-KEY (“contagion” OR “interdependence\*” OR “comovement\*” OR “co-movement\*” OR “correlation\*”). All the research documents identified were downloaded and ed into the Mendeley Reference Manager for the scientometric analysis. After removing 29 duplicates, we utilized 86 research documents for the scientometric analysis using three tools: (i) the tree of science (Robledo et al. 2014), (ii) the VOSviewer version 1.6.18 (van Eck and Waltman 2017), and (iii) the Bibliometrix package for R (Aria and Cuccurullo 2017). Figure 2 shows the literature search strategy.

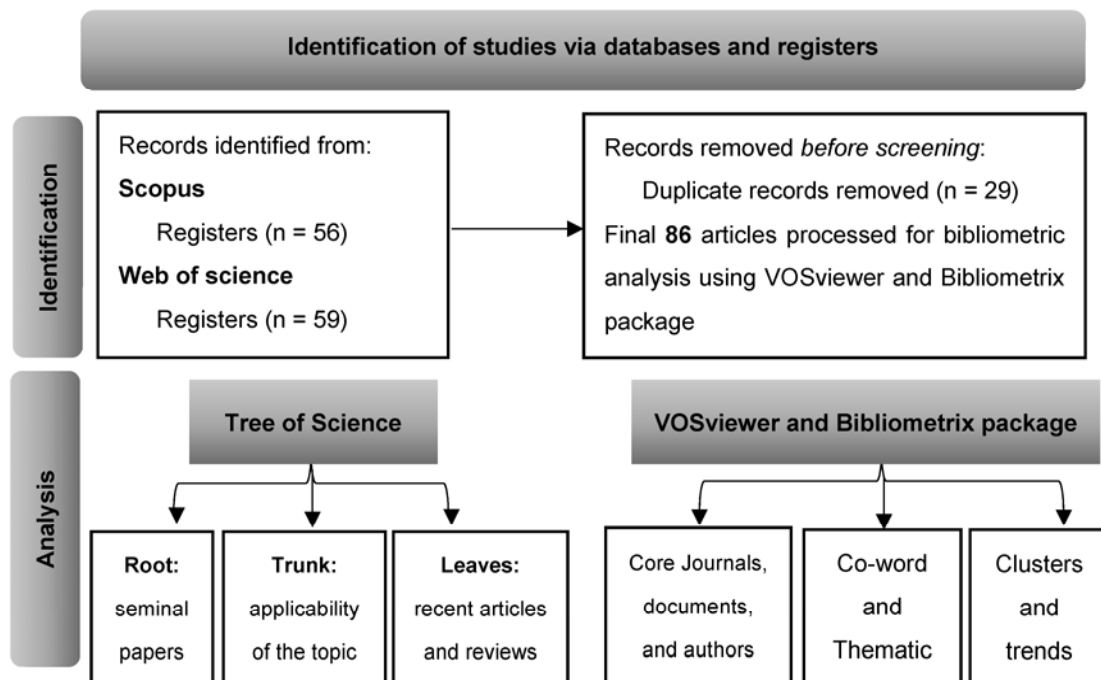


Figure 2. Literature search strategy.

As indicated by Robledo et al. (2014), the studies found at the root of the tree of science include seminal articles from the original ones about the dynamic associations among oil prices, green bonds, and CO<sub>2</sub> emissions. For example, studies conducted by (Henriques and Sadorsky 2008; Kumar et al. 2012; Reboredo 2015; Reboredo et al. 2017; Sadorsky 2012) were found in the root, and those papers are the identified seminal studies about the linkages among oil prices and assets related to sustainable finance, such as renewable energy or clean energy stock prices. Refs. (Kumar et al. 2012; Sadorsky 2012) analyze the correlations between clean energy stock prices and oil prices. The findings suggest, for daily data from 2001 to 2010, that stock prices of clean energy companies correlate more highly with technology stock prices than oil prices (Sadorsky 2012). Additionally, based on the weekly observations for the period 2005–2008, Kumar et al. (2012) found that past movements in oil prices explain the indexes of clean energy stocks, stock prices of high technology firms, and interest rates.

Conversely, [Robledo et al. \(2014\)](#) argue that documents in the trunk mainly include the first authors who discovered the applicability and have become references for dynamic associations between oil prices and the financial markets analyzed. Here, documents that study the relationship between energy markets and assets related to sustainable finance can be found, and those used the methodologies of Dynamic Conditional Correlation analysis (DCC-GARCH) or volatility linkages ([Dutta et al. 2018](#); [Lin and Chen 2019](#); [Marín-Rodríguez et al. 2022b](#); [Reboredo 2018](#)); and wavelet analysis ([Kassouri et al. 2022](#); [Maji et al. 2020](#)). According to [Dutta et al. \(2018\)](#), the results, using daily data from 2009 to 2017, indicate a volatility connection between the emissions and the European Clean Energy Price Indexes. However, this result does not hold for the United States market, suggesting that emissions' return and volatility shocks are country or region-specific. [Lin and Chen \(2019\)](#), using a daily dataset from 2013 to 2017, found that: (i) There are significant time-varying correlations and a long-run persistence between the Beijing Carbon Emissions Trading (CET) market, the coal market, the stock market of New Energy Companies (NEC), and the coal market; (ii) the new energy stock market has a higher volatility persistence. Additionally, (ii) there is a bi-directional spillover effect between the coal market and the stock market of New Energy Companies.

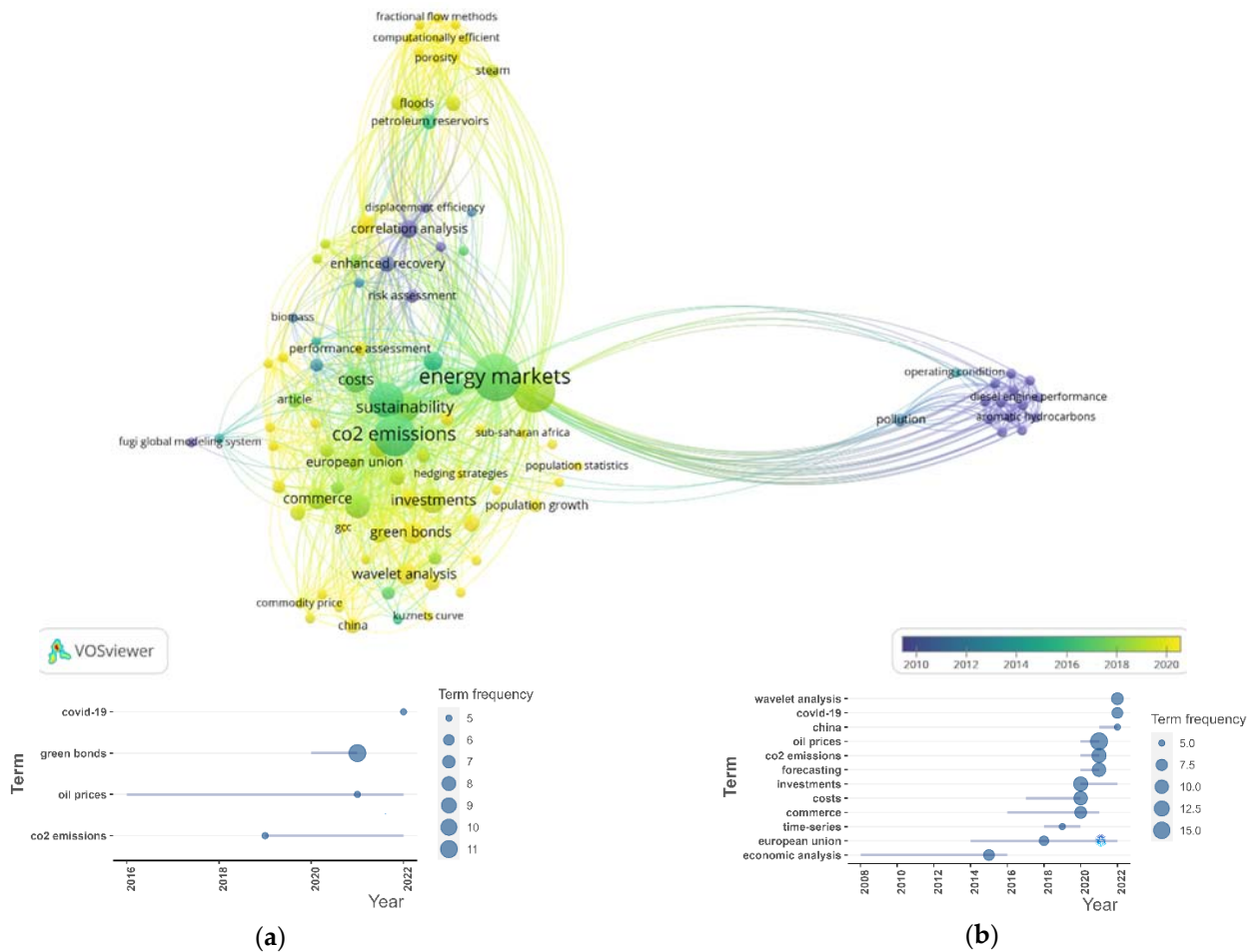
Finally, the documents in the leaves, according to [Robledo et al. \(2014\)](#), are recent articles and reviews that should condense the analysis of dynamic relationships among oil prices, green bonds, and CO<sub>2</sub> emissions. In the literature review, [Marín-Rodríguez et al. \(2022a\)](#) can be outlined. In the new trends, in the leaves, there are several methodologies identified which have studied the dynamic relationships among energy markets and assets related to sustainable finance, for example, using Time-Varying Parameter Vector Auto Regression (TVP-VAR) ([Li et al. 2022](#)), wavelet analysis ([Bouoiyour et al. 2023](#); [Kassouri et al. 2022](#); [Luo et al. 2022](#); [Maghyereh et al. 2019](#); [Shah et al. 2022](#); [Zhou et al. 2022](#)), DCC-GARCH and its extensions ([Dutta et al. 2021](#); [Marín-Rodríguez et al. 2022b](#)), Copula functions ([Elie et al. 2019](#); [Naeem et al. 2021a](#); [Wen et al. 2017](#)), time-varying conditional analysis comprising hedging effectiveness and optimal hedge ratios ([Gustafsson et al. 2022](#)), and quantile analysis ([Ren et al. 2022a, 2022c](#); [Saeed et al. 2021](#); [Zhang and Zhou 2022](#)).

On the other hand, when exploring the existing literature about the dynamic relationship among oil prices, green bonds, and CO<sub>2</sub> emissions using the VOSviewer, the research pointed out that the most used keywords for this type of analysis are: (1) energy markets, (2) oil prices, (3) CO<sub>2</sub> emissions, and (4) economic analysis. The results of the analyses are presented in Figure 3.

Furthermore, during the revision through the Bibliometrix package for R applying on author keyword analysis, which offers information about research trends from the researchers' points of view ([Garfield 1970](#)), the results indicate that the most prominent research areas are COVID-19 (2022), green bonds (2020–2021), oil prices (2016–2022), and CO<sub>2</sub> emissions (2019–2022). On the other hand, implementing the analysis on the keywords plus, which are terms extracted from titles or abstracts ([Aria and Cuccurullo 2017](#)), the findings reveal that the leading research areas are wavelet analysis and COVID-19 (2022), China (2020–2022), oil prices, CO<sub>2</sub> emissions, forecasting (2019–2021), and investments (2020–2022).

Thus, the relationships among oil prices, green bonds, and CO<sub>2</sub> emissions can be classified into these two major trends provided by (i) the authors' keywords and (ii) keywords plus. The first trend (Figure 3a) delves into the bonds among these three variables, including the effects of the COVID-19 disease ([Li et al. 2022](#); [Marín-Rodríguez et al. 2022b](#)). In this trend, the keywords COVID-19, green bonds, oil prices, and CO<sub>2</sub> emissions are precisely leading the trend topics. This result is according to the studies in the leaves of the Tree of Science. Additionally, in this first trend, the documents that study the impacts of the COVID-19 on the green bonds markets can be included ([Liu 2022](#); [Naeem et al. 2021b](#); [Rao et al. 2022](#); [Tiwari et al. 2022, 2021](#)), as well as CO<sub>2</sub> emissions ([Agboola et al. 2021](#); [Balsalobre-Lorente et al. 2020](#); [Dong et al. 2022](#); [Shah et al. 2022](#); [Tiwari et al. 2022](#)), and oil prices ([Alshdadi et al. 2022](#); [Ghorbali et al. 2022](#); [Habib et al. 2021](#); [Ozturk and Cavdar 2021](#); [Ren et al. 2021](#); [Zhou et al. 2022](#)). The findings suggest that the COVID-19 pandemic

shock caused huge fluctuations and negative returns in green bond markets (Liu 2022). Furthermore, the contraction of economic growth since the beginning of the COVID-19 pandemic produced a reduction in CO<sub>2</sub> emissions (Agboola et al. 2021). Finally, the results also indicate that COVID-19 negatively impacted crude oil prices, which contributed to the reduction of CO<sub>2</sub> emissions during the pandemic period (Habib et al. 2021).



**Figure 3.** Main keyword trends identified in the research topic are dynamic linkages among oil prices, green bonds, and CO<sub>2</sub> emissions. Source: Authors’ research using VOSviewer, Bibliometrix tools, Scopus, and WoS databases. (a) Author’s keywords trend topics; (b) Keywords plus trend topics.

The second trend (Figure 3b) analyzes the interlinkages between oil prices and CO<sub>2</sub> emissions. For example, (Ali et al. 2022; Alkathery and Chaudhuri 2021; Apergis and Payne 2015; Royal et al. 2022; Sadorsky 2009; Zaghoudi 2017) analyze the co-movements among oil prices, CO<sub>2</sub> emissions, and renewable energy. The findings suggest that renewable energy improves environmental quality in both the short and long run; an increase in oil prices causes a decrease in CO<sub>2</sub> emissions and has an important effect on economic growth. Additionally, other documents within this trend study the effects of oil price shocks on CO<sub>2</sub> emissions (Bassey 2015; Habib et al. 2021; Husaini et al. 2021; Maji et al. 2020; Ren et al. 2022b; Wei et al. 2022). Their results indicate that there is a negative relationship between oil price shocks and CO<sub>2</sub> emissions; higher oil prices can mitigate CO<sub>2</sub> emissions, while lower oil prices can increase sectoral CO<sub>2</sub> emissions. Besides, COVID-19 affects crude oil prices, the major contributor to the reduction of CO<sub>2</sub> emissions during the pandemic period. In this trend, the keywords COVID-19, wavelets, China, oil prices, CO<sub>2</sub> emissions, and forecasting are the foremost trend topics.

Finally, based on the scientometric analysis of the main studies on the dynamic co-movements among oil prices, CO<sub>2</sub> emissions, and green bonds conducted by Marín-

Rodríguez et al. (2022a) on the dynamic co-movements among oil prices and financial markets (including energy markets and assets related to sustainable finance), the findings indicate that the most promising areas for further research in this field are represented by co-movement, copula, wavelet, dynamic correlation, and volatility analysis. Furthermore, the authors indicate that energy markets and assets related to sustainable finance emerge as crucial trends in exploring dynamic co-movements of oil prices. Additionally, as we mentioned before, Marín-Rodríguez et al. (2022b) make a previous application to the analysis of the dynamic co-movements among oil prices, CO<sub>2</sub> emissions, and green bonds using Granger causality and DCC-GARCH methodologies. Thus, in line with these two documents and the results of the present literature review, this study attempts to make a deeper analysis considering a time-frequency analysis (using wavelets methodology) that searches for the connection among the three variables studied in the short, medium, and long term.

### 3. Methodology

#### 3.1. The Dataset

The dataset consists of daily closing prices of Brent oil prices, green bonds, and CO<sub>2</sub> emissions (Table 1). Our sampling period spans from 1 January 2014 to 3 October 2022, including 2290 daily observations. The starting date of the sample is determined by the availability of the Green Bond Index data. All data were gathered from Bloomberg. Futures' prices of CO<sub>2</sub> emissions (MO1 Comdty), according to Reboredo (2013) and Rittler (2012) were used. They indicate that the futures market leads the price training process by first locating information and then transferring it to the spot market. Furthermore, the Bloomberg MSCI Green Bond Index (GBEUTREU Index) is a Euro fixed-income benchmark to fund projects with direct environmental benefits. This index incorporates Euro-denominated fixed-income securities, such as treasury, corporate, government-related, and securitized debt. Additionally, the index reflects the performance of Euro-denominated fixed-income securities, including treasury, corporate, government-related, and securitized debt. Furthermore, the Brent oil price (CO1 Comdty) is included as a fundamental component of energy prices.

**Table 1.** List of variables.

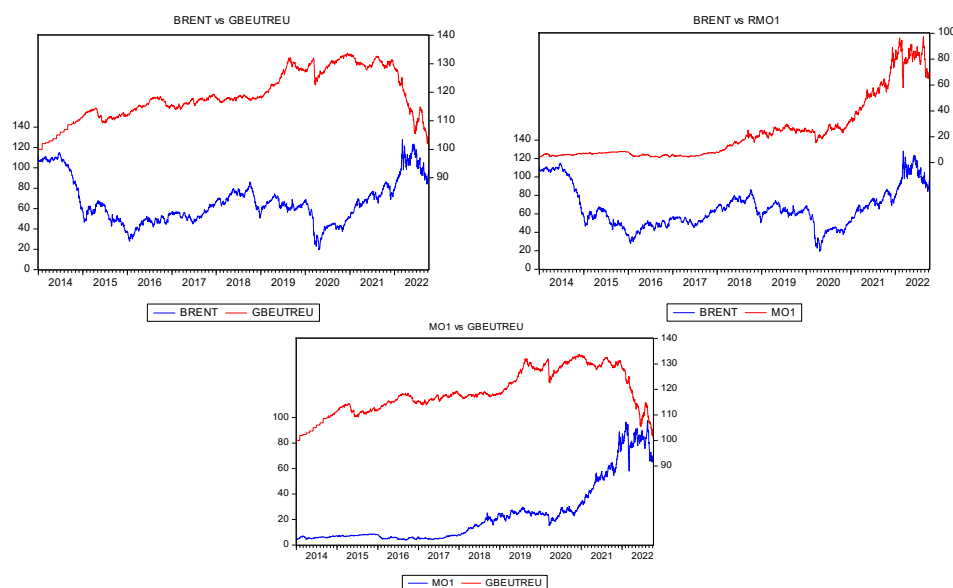
Variable	Ticker	Description
Oil Brent price	CO1 Comdty	Generic 1st Crude Oil, Brent
Green Bond Index	GBEUTREU Index	Bloomberg MSCI Euro Green Bond Index Total Return Index Value Unhedged
CO <sub>2</sub> futures price	MO1 Comdty	CO <sub>2</sub> futures price, Euros per ton

Source: Authors' own research using Bloomberg.

Figure 4 illustrates the temporal dynamics of Brent oil prices, green bonds, and CO<sub>2</sub> emissions by pairs, evidencing that oil prices positively depend on CO<sub>2</sub> futures prices (MO1 Comdty). Still, the dependence is negative with the Green Bond Index (GBEUTREU Index). Furthermore, in recent times the co-movements are increasing between the Green Bond Index (GBEUTREU Index) and CO<sub>2</sub> futures prices (MO1 Comdty), indicating clear graphical evidence of dependence, particularly in 2022.

Table 2 depicts descriptive statistics of daily returns of the considered series computed as the first difference of the natural log of the prices or indexes. The average daily returns are close to zero for all series. The standard deviations reveal that green bonds are less volatile than Brent oil prices and CO<sub>2</sub> futures' prices. All daily returns are negatively biased and exhibit high values for the Kurtosis statistics consistent with heavy-tailed distortions. The Jarque–Bera (JB) test strongly rejects the normality of the unconditional distribution of the return series and the non-stationarity tests [via Augmented Dickey–Fuller (ADF)] (Dickey and Fuller 1979) evidence that all return series are stationary. Finally, the Ljung–Box Q-statistics (LBQ) indicate the presence of a serial correlation in both the

return series and the squared return series; it is consistent with the existence of conditional heteroskedasticity effects.



**Figure 4.** Daily prices and returns of Brent oil prices (RBRENT), Green Bond Index (RGBEUTREU), and CO<sub>2</sub> futures' returns (RMO1). Source: Author's own research using data from Bloomberg.

**Table 2.** Summary statistics of daily returns.

Index	Mean	Max	Min	Std. Dev.	Skew.	Kurt.	JB	ADF	LBQ (25)	LBQ2 (25)
RBRENT	−0.000063	0.1908	−0.2798	0.0256	−0.982	19.46	26198.4 *	−47.16 *	48.36 [0.003]	836.81 [0]
RGBEUTREU	0.000004	0.0196	−0.0196	0.0027	−0.164	11.13	6315.4 *	−44.18 *	61.73 [0]	1655.0 [0]
RMO1	0.001145	0.162	−0.1944	0.0292	−0.527	7.61	2133.5 *	−50.34 *	38.42 [0.042]	306.21 [0]

Source: Authors' own research using data from Bloomberg. Notes: This table presents summary statistics of daily returns of Brent oil prices (RBRENT), Green Bond Index (RGBEUTREU), and CO<sub>2</sub> futures' returns (RMO1). The 1 January 2014—3 October 2022 sample yielded 2290 observations. (\*) indicates the rejection of the null hypothesis at the 5% level for both the normality test (via Jarque-Bera) and unit root test [via Augmented Dickey-Fuller (ADF)], the ADF test is conducted with an intercept. LBQ (25) and LBQ2 (25) denote the Ljung–Box Q-statistics for serial correlation in the returns and squared returns series, respectively, computed using 25 lags, with p values reported in square brackets.

### 3.2. Wavelet Analysis

The wavelets methodology is one of the mathematical applications that has recently been applied to modeling in several fields, including economics and finance. It allows for the analysis of the time series frequency and time domain simultaneously. This methodology is based on the Fourier Analysis, which focuses on studying frequency domain signals. In this way, wavelets are functions that oscillate as a wave and present fades; that is, they decay. Due to these particularities, this methodology is considered an ideal filter that allows the fragmenting of a signal into different levels of resolution, capturing large and small particularities of the analyzed series. This is known as multi-resolution decomposition using wavelets, which facilitates the decomposition of the original signal into different levels of resolution where each level will necessarily be associated with a specific time scale. The existence of non-stationary phenomena, that is, those presenting variations over time and which do not have a constant mean and/or variance in various disciplines such as geophysics, medicine, statistics, economics, and finance, among others, has expanded the use of wavelets to be ideal for the treatment of this type of series.

Ftiti et al. (2016) indicate that among their advantages, the following stand out: (i) wavelets are a process that breaks down data into different frequency components. This decomposition of different scales facilitates to distinguish of seasonality, structural changes, volatility clusters, and the identification of the local and global dynamic properties of



the variables; (ii) Wavelets provide a better alternative for exploring the interconnection between oil and stock markets, as they do not impose parametric constraints on stock market dynamics and oil price fluctuations and (iii) The wavelet process adapts to different characteristics of the time series in general (such as the stock market and oil price series), where the variance is variable over time, and the covariance matrix presents possible structural breaks. This feature helps discriminate between interdependence (long-term co-movement) and contagion (short-term co-movement) in the relationship between oil and financial markets, which will be the subject of the application in this study. However, [Dibal et al. \(2018\)](#) identify weaknesses in the methodology, such as its excessive redundancy, its computational intensity, and the fact that an original signal cannot be perfectly reconstructed from the coefficients estimated by the process.

This research studies the co-movement among oil prices, green bonds, and CO<sub>2</sub> emissions, leading to knowing the linkage across different horizons (i.e., short-medium-and long-term). The wavelet coherency approach by [Grinsted et al. \(2004\)](#) offers this possibility by decomposing the economic relationship into time-frequency components. Furthermore, the wavelet coherency can be applied to bivariate and multivariate contexts, where patterns of covariation and causal relationships among variables across different scales are examined over time ([Ahmed 2022](#)). This methodology is similar to the Pearson Bivariate Correlation Coefficient. It measures the degree of co-movement in the time-frequency (location–scale) domain between a pair of time series variables  $x(t)$  and  $y(t)$  ([Singh et al. 2022](#)).

### 3.2.1. The Continuous Wavelet Transform (CWT)

Thus, the wavelet technique (i) decomposes the return series into time-scale components, and (ii) represents the variability and structure of the stochastic processes on a scale-by-scale basis. The wavelet function is a small wave and can be manipulated (stretched or squeezed over time) to extract the frequency components from a complex signal ([Bouri et al. 2020](#)).

The mother wavelet is used to produce small waves. It is expressed as a function of time and scale  $s$  as:

$$\psi_{\tau,s}(t) = \frac{1}{\sqrt{s}} \psi\left(\frac{t - \tau}{s}\right) \quad (1)$$

where  $\tau$ ,  $s$ , and  $\frac{1}{\sqrt{s}}$  represent the time position (translation parameter), scale (dilation parameter related to frequency) and normalization factor, respectively. The normalization factor ensures that the transformation remains comparable across scales and over time.

The literature provides various wavelets for the time series decomposition depending on the research topic. To examine the wavelet coherence among oil prices, green bonds, and CO<sub>2</sub> emissions, the Morlet Wavelet is used ([Morlet et al. 1982](#)). This wavelet provides the best balance between time and frequency localization ([Addison 2017](#)). [Grinsted et al. \(2004\)](#) show that the Fourier period for the Morlet wavelet is almost equal to the scale used:

$$\psi^M(t) = \frac{1}{\pi^{1/4}} e^{i\omega_0 t} e^{-t^2/2} \quad (2)$$

where  $\omega_0$  indicates the central wavelet frequency. Like [Bouri et al. \(2020\)](#), this research used  $\omega_0 = 6$ , as the Morlet wavelet; this central frequency provides good localization between time and frequency.

### 3.2.2. Wavelet Power Spectrum

The wavelet analysis can be performed using either the continuous wavelet transforms (CWT), or the discrete wavelet transform (DWT). The CWT has several advantages over the DWT. For example, the CWT provides independence to select wavelets according to the length of data, and the redundancy in the CWT makes the interpretation and discovery of patterns or hidden information easier ([Aguar-Conraria and Soares 2011](#)). A continuous

wavelet transform  $W_x$  of a discrete-time series  $(x(t), t = 0, 1, \dots, n)$  with respect to  $\psi(t)$  can be represented as:

$$W_x(\tau, s) = \int_{-\infty}^{+\infty} x(t)\psi_{\tau,s}^*(t)dt = \frac{1}{\sqrt{s}} \int_{-\infty}^{+\infty} x(t)\psi^*\left(\frac{t-\tau}{s}\right)dt \tag{3}$$

where  $*$  denotes the complex conjugate. Notably, the wavelet transform preserves the energy of a time series that can be used to analyze the power spectra. Accordingly, the variance is given by:

$$\|x\|^2 = \frac{1}{C_\psi} \int_0^\infty \left[ \int_{-\infty}^{+\infty} |W_x(\tau, s)|^2 d\tau \right] \frac{ds}{s^2} \tag{4}$$

To obtain information about the time series behavior, the wavelet power spectrum (WPS) was used in the present paper,

$$WPS_x(\tau, s) = |W_x(\tau, s)|^2 \tag{5}$$

Refs. [Hudgins et al. \(1993\)](#) and [Torrence and Compo \(1998\)](#) define the cross-wavelet power  $|W_{xy}(\tau, s)|$  of two time series  $x(t)$  and  $y(t)$  with the continuous transforms  $W_x(\tau, s)$  and  $W_y(\tau, s)$  as:

$$W_{xy}(\tau, s) = W_x(\tau, s) \cdot W_y^*(\tau, s) \tag{6}$$

### 3.2.3. Wavelet Coherence

The cross-wavelet power shows the areas of high common power between two time series in the time-frequency space. The wavelet squared coherence between the two times series is given by:

$$R_{xy}^2(\tau, s) = \frac{|S(s^{-1}W_{xy}(\tau, s))|^2}{S(s^{-1}|W_x(\tau, s)|^2) \cdot S(s^{-1}|W_y(\tau, s)|^2)} \tag{7}$$

where  $R_{xy}^2(\tau, s)$  represent the wavelet squared coherency between  $x(t)$  and  $y(t)$ , in other words  $R_{xy}^2(\tau, s)$  is a direct measure of the contemporaneous correlations between  $x(t)$  and  $y(t)$  at each point in time and for each frequency.  $S(\cdot)$  is a smoothing parameter in scale and time. The value of the wavelet squared coherence  $R_{xy}^2(\tau, s)$  ranges between zero (no co-movement) and one (high co-movement) can be seen as a scale-specific squared correlation between series. In addition, the wavelet coherence framework allows studying the lead-lag relationship between series while avoiding the squared coherence’s inability to distinguish between the positive and negative relationship between series. [Torrence and Webster \(1999\)](#) and [Bloomfield \(2013\)](#) show that the phase difference depicting the phase relationship between  $x(t)$  and  $y(t)$  is given by:

$$\phi_{xy}(\tau, s) = \tan^{-1} \frac{\Im\{W_{xy}(\tau, s)\}}{\Re\{W_{xy}(\tau, s)\}}, \phi_{x,y} \in [-\pi, \pi] \tag{8}$$

where the parameters  $\Im$  and  $\Re$  give the imaginary and real parts of the smooth power spectrum, respectively. A zero-degree phase difference reveals the synchronization of  $x(t)$  with  $y(t)$  at a particular time-frequency. On the wavelet coherence plots,  $\phi_{xy}(\tau, s)$  is symbolized as black rightward, leftward, upward, and downward arrow signs within areas of statistical significance. When the arrow points to the right (left) suggests that  $x(t)$  and  $y(t)$  are in phase (out of phase); it means that  $x(t)$  and  $y(t)$  are positively (negatively) associated, with negligible or no time lag. If the arrow points upwards, the first series leads the other by  $\pi/2$  (the actual period is based on the specific frequency/scale of the wavelet coherence chart), and the opposite for a downward-pointing arrow. Additionally, for the interpretation of the arrows, following [Kirikkaleli and Güngör \(2021\)](#) arrows pointing up, right-up, or left-down denote that the second variable causes the first variable, while

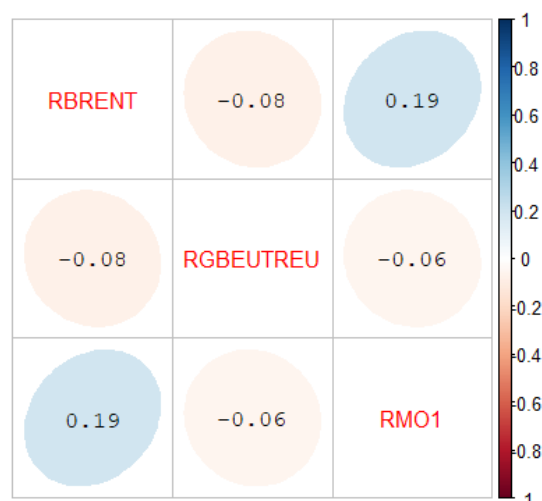
arrows pointing down, right-down, or left-up indicate that the first variable causes the second variable.

The wavelet coherence results are standardly shown on a chart with time and scale (or frequency) on the respective axes and the coherences are represented by a color scale. The color spectrum shows the intensity of the association (co-movement) between the pair of the analyzed series. The warmer colors (red) indicate significant co-movements, while colder colors (blues) signify weak co-movements between the series. In regions beyond the black line cone or the cone of influence, the estimates of wavelet coefficients are statistically insignificant at 5% significance and are not considered.

#### 4. Application and Results

##### 4.1. Unconditional Correlation Analysis

Pairwise correlations across the returns of the variables considered are presented in Figure 5. The correlation of oil price return (RBRENT) with the CO<sub>2</sub> futures' returns (RMO1) is positive (19%), and the Green Bond Index (GBEUTREU) is negative (−6%). Additionally, the correlation between the CO<sub>2</sub> futures' returns (RMO1) and the Green Bond Index return (GBEUTREU) is negative too (−8%).

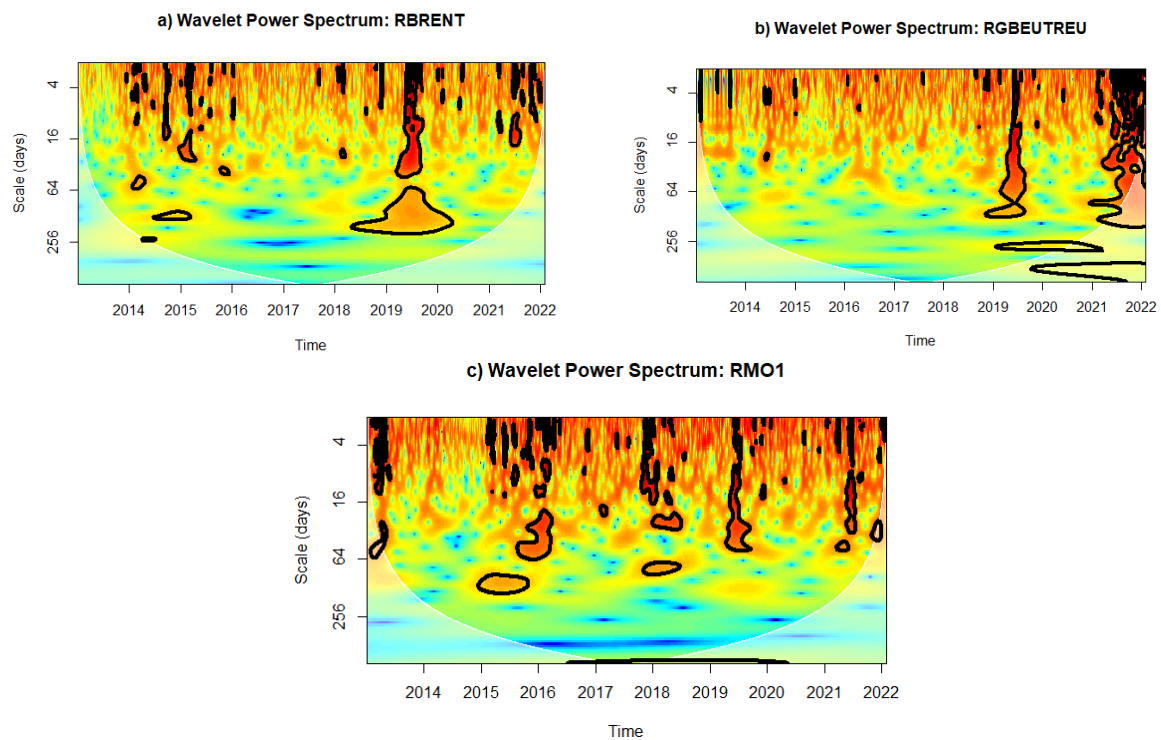


**Figure 5.** Unconditional correlation for Brent oil returns (RBRENT), Green Bond Index (RGBEUTREU), and CO<sub>2</sub> futures' returns (RMO1). Source: Authors' own research using data from Bloomberg.

According to the existing literature, it is expected that oil prices and CO<sub>2</sub> emissions have a positive relationship, and their co-movement against the Green Bond Index is in the same sense because an increase in oil prices tends to increase CO<sub>2</sub> emissions (Mahmood et al. 2022; Mahmood and Furqan 2021; Sadorsky 2009; Zheng et al. 2021). Additionally, increasing green bond issuances tends to reduce CO<sub>2</sub> emissions (al Mamun et al. 2022; Fatica and Panzica 2021). For example, the study conducted by al Mamun et al. (2022) shows that green finance significantly reduces carbon emissions in the short and long run by supporting waste and pollution control and improving energy efficiency.

##### 4.2. Wavelet Power Spectrum

Figure 6 presents the wavelet power spectrum for the Brent oil returns (RBRENT), Green Bond Index (RGBEUTREU), and CO<sub>2</sub> futures' returns (RMO1) variables, respectively. The Brent oil returns (RBRENT), Figure 6a, appear to show significant volatility at low and medium frequencies, particularly in 2014, the end of 2019–2020, and 2022. This phenomenon is according to the high volatility observed in these periods due to the FED's Taper Announcement and the first oil prices crisis in 2014, the global COVID-19 pandemic at the end of 2019–2020, and the Russian invasion of Ukraine in February 2022.



**Figure 6.** Wavelet power spectrum for Brent oil returns (RBRENT), Green Bond Index (RGBEUTREU), and CO<sub>2</sub> futures' returns (RMO1). Source: Authors' own research using data from Bloomberg.

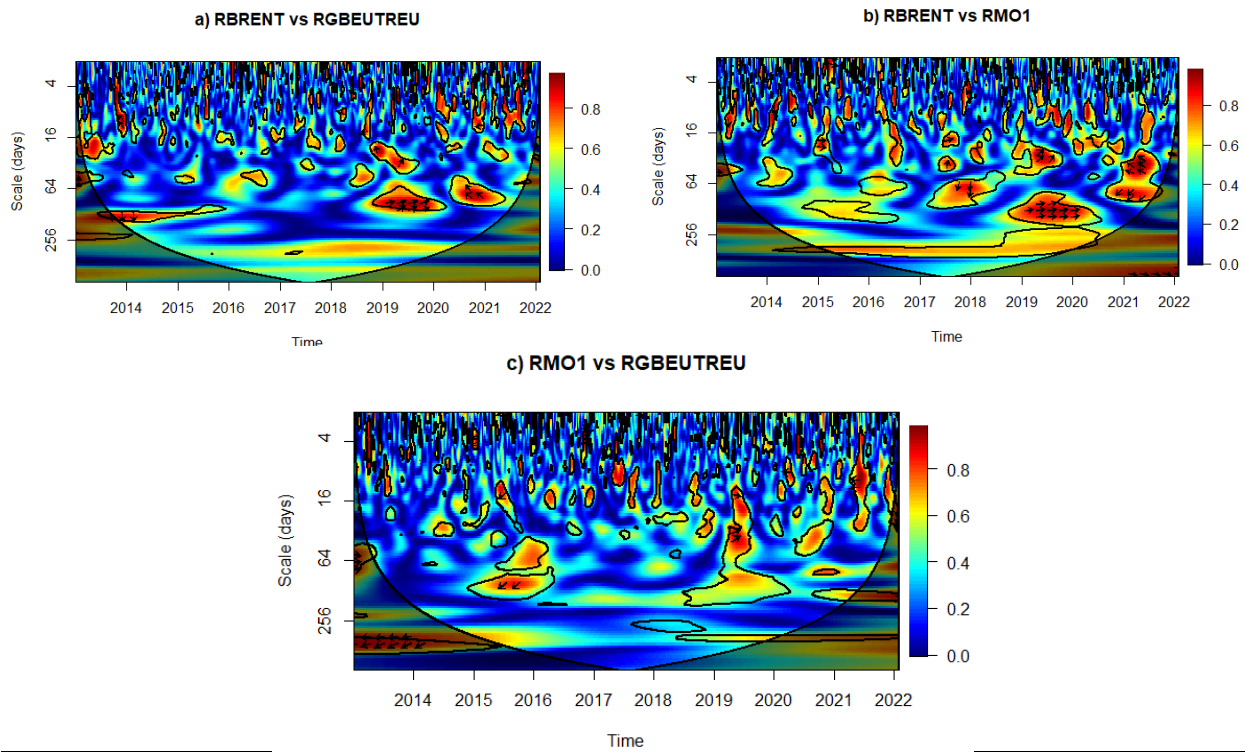
The Green Bond Index (RGBEUTREU) behavior, Figure 6b, exhibits significant volatility at the end of 2019–2020 and the beginning of 2022 at low, medium, and high frequencies, which is consistent with the two last events identified previously. For example, in 2019–2020, the issuances of green bonds were extended worldwide. However, in February 2022, the Russian invasion of Ukraine and the subsequent European energy crisis exacerbated post-COVID-19 inflation and impacted the bond market dynamics by increasing interest rates. As a result, high volatility resulted in decreased bond issuance. It is important to note that the Green Bond Principles (GBP) were launched in 2014, its first update occurred in 2015, and the development of this market is constantly changing.

Finally, CO<sub>2</sub> futures' returns (RMO1), Figure 6c, present high volatility at low and medium frequencies, particularly in 2015–2016, 2018, the end of 2019–2020, and 2022.

#### 4.3. Wavelet Coherence Approach

The wavelet coherence approach is applied to capture the causal relationship between the Brent oil returns (RBRENT), the Green Bond Index (RGBEUTREU), and the CO<sub>2</sub> futures' returns (RMO1). Figure 7 presents the results from the wavelet coherence. It captures the co-movement of these three variables in the time-frequency space.

Figure 7 and its table depict the wavelet coherence and phase difference and principal results between each pair of times series considered. In the figure, the horizontal axis ( $x$ -axis) represents the research period in days, while the vertical axis ( $y$ -axis) represents the frequency domain. This study considered five frequency cycles: 1–4, 4–16, 16–64, 64–256, and 256–512 daily bands. The shortest band, which considers 2–4 days, denotes the highest frequency band, and the most extended band includes 256–512 days, the lowest frequency band. For a better comprehension of the results, they include in the short-term (ST), the signals between the 2–4 days and 4–16 bands; medium-term (MT), the signals between the 16–64 days and 64–256 bands; and long-term (LT) the signals in 256–512 days band (see Figure 7 and its table). Located on the right-hand side of each plot, there is the color gradient code of power, where dark blue indicates low power (close to zero), and dark red implies high power (close to one).



Causality/Period	2014	2015–2016	2018	2019–2020	2021	2022
RBRENT significantly caused RGBEUTREU	Negative MT				Negative MT	
RGBEUTREU significantly caused RBRENT				Positive MT, LT		
RBRENT significantly caused RMO1			Positive ST, MT	Negative MT		Positive LT
RMO1 significantly caused RBRENT	Negative ST			Positive MT	Negative MT	
RMO1 significantly caused GBEUTREU						Negative MT
RGBEUTREU significantly caused RMO1	Positive, MT Negative, LT	Negative ST, MT, LT		Positive MT	Negative ST	

**Figure 7.** Wavelet coherence among Brent oil returns (RBRENT), CO<sub>2</sub> futures’ returns (RMO1), and Green Bond Index (RGBEUTREU). Source: Authors’ own research using data from Bloomberg. Note: The value of squared wavelet coherence is depicted in color, and the value of relative phase by arrows. The color code for the coherence ranges from blue (low coherence—close to zero) to red (high coherence—close to one). The area affected by edge effects is the semi-transparent region at the left and right boundary separated by the black U-shaped curve, which is the cone of influence (CoI). The thick black contours within CoI are the regions of significant coherence (at 5% level). The direction of the arrows reveals the phase relationship between each moment pair of times series returns in the time-frequency space. Notes: ST: short-term, MT: medium-term, LT: long-term.

Figure 7a shows that wavelet coherence between the Brent oil returns (RBRENT) and the Green Bond Index (RGBEUTREU) from scales 64 to 256 days, down arrows are obtained in 2014, indicating that in the medium-term, the Brent oil returns (RBRENT) significantly affected the Green Bond Index (RGBEUTREU) negatively. However, the direction of the causality changes between 2019–2020 at different frequencies (16–64 and

64–256 days, medium-term and long-term, respectively) since the arrows mostly point right-up, implying a positive relationship and that the Green Bond Index (RBEUTREU) is an important predictor of the Brent oil returns (RBRENT) in the medium-term and long term for the period between 2019–2020. Finally, in 2021, the Brent oil returns (RBRENT) significantly affected the Green Bond Index (RBEUTREU) for scales 16–64, and the arrows mostly point left-up, indicating a negative relationship in the medium-term. The summary of the results in the table supports a bi-directional causality relationship between the Brent oil returns (RBRENT) and the Green Bond Index (RBEUTREU).

Additionally, Figure 7b depicts that wavelet coherence between the Brent oil returns (RBRENT) and CO<sub>2</sub> futures' returns (RMO1) presents, from scales 4 to 16 days, arrows that point down and left-down in 2014, indicating that in the short term, the CO<sub>2</sub> futures' returns (RMO1) affected Brent oil returns (RBRENT) significantly with a negative relationship. In 2018, Figure 7b indicates that from scales 4–16 and 64–256, the arrows point right, implying that in the short-term and medium-term, Brent oil returns (RBRENT) influenced the CO<sub>2</sub> futures' returns (RMO1) with a positive relationship. From 2019 to 2020, Figure 7b shows a change in the direction of the causality for the frequencies 16–64, indicating that in the medium-term CO<sub>2</sub> futures' returns (RMO1) significantly influenced the Brent oil prices (RBRENT) with a positive relationship. However, for the period between 2019–2020, left-up arrows are obtained for a scale of 16–64, indicating that in the medium-term, the Brent oil returns (RBRENT) significantly affected the CO<sub>2</sub> futures' returns (RMO1) with a negative relationship. Additionally, for the frequency 64–256 days in the period 2021, the presence of left-down arrows indicates that in the medium-term CO<sub>2</sub> futures' returns (RMO1) significantly caused the Brent oil prices (RBRENT) with a negative relationship. Finally, for scales 256–512 days, the arrows point right-down, indicating that in the long-term, Brent oil returns (RBRENT) significantly caused the CO<sub>2</sub> futures' returns (RMO1) with a positive relationship. The summary of the findings in the table validates a bi-directional causality relationship between the Brent oil returns (RBRENT) and CO<sub>2</sub> futures' returns (RMO1).

Finally, Figure 7c presents the wavelet coherence between CO<sub>2</sub> futures' returns (RMO1) and Green Bond Index (RBEUTREU). In 2014, from scales 64 to 256 days, arrows pointed right, denoting that the Green Bond Index (RBEUTREU) and CO<sub>2</sub> futures' returns (RMO1) have a positive relationship in the medium-term. But, in 2014, from scales 256–512, arrows point left-down, which indicates that the Green Bond Index (RBEUTREU) affects the CO<sub>2</sub> futures' returns (RMO1) in the long-term, having a negative relationship. In 2015–2016 arrows point left-down at different frequencies (4–16, 16–64, and 64–256 days), denoting that the Green Bond Index (RBEUTREU) causes the CO<sub>2</sub> futures' returns (RMO1) for 2015–2016 in short-term, medium-term, and long-term with a negative relationship. For the period 2019–2020, for the frequency 16–64 days, arrows point right-up, indicating that the Green Bond Index (RBEUTREU) causes CO<sub>2</sub> futures' returns (RMO1) in the medium-term with a positive relationship. In 2021, for a scale of 4–16, the arrows pointed left-down, denoting that the Green Bond Index (RBEUTREU) causes the short-term CO<sub>2</sub> futures' returns (RMO1) with a negative relationship. Finally, in 2022 the direction of the causality changes, and for the frequency of 16–64 days, the arrows pointing down indicate that the CO<sub>2</sub> futures' returns (RMO1) variable affect the Green Bond Index (RBEUTREU) in the medium-term with a negative relationship. The summary of the results in the table supports a unidirectional causality relationship from the Green Bond Index (RBEUTREU) to CO<sub>2</sub> futures' returns (RMO1), with an exception in 2022 when the direction of the causality changes.

## 5. Discussion

The findings from the wavelet power spectrum reveal that (i) there was significant volatility in the Brent oil returns at low and medium frequencies, particularly in 2014, the end of 2019–2020, and 2022 at low and medium frequencies; (ii) the Green Bond Index exhibit significant volatility at the end of 2019–2020 and at the beginning of 2022 at low, medium, and high frequencies; and (iii) the CO<sub>2</sub> futures' returns present high volatility at

low and medium frequencies, specifically in 2015–2016, 2018, the end of 2019–2020, and 2022. This phenomenon is according to the high volatility observed in these periods due to the FED's Taper Announcement and the first oil prices crisis in 2014, the global COVID-19 pandemic at the end of 2019–2020, and the Russian invasion of Ukraine in February 2022. These results are in line with [Jin et al. \(2020\)](#), who argues that carbon emissions and energy markets (including oil prices) are due to the similar nature of the markets. We can include the green bond issuances for their relationship with these two markets, which is increasing due to the transition of energy to a decarbonized economy. Thus, the three considered markets are sensitive to the same macroeconomic variables, such as climate change, market conditions, and geopolitical situations, such as those reported in recent empirical facts.

Additionally, wavelet coherence results indicate that (i) the Brent oil returns have a negative impact on the Green Bond Index in the medium term for 2015 and 2021, respectively. Still, the Green Bond Index positively impacts the Brent oil returns in the period 2019–2020 in the medium-term and long-term, which indicates a feedback relationship, suggesting that oil prices and green bond prices are interdependent when these markets are in a bearish state. This result is in line with [Lee et al. \(2021\)](#). Also, the wavelet coherence analysis indicates a negative relationship between oil prices and CO<sub>2</sub> futures' returns in 2019–2020. However, the relationship becomes positive during 2018 (short-term and medium-term) and 2022 (long-term). This paper's findings support [Li et al. \(2022\)](#), since oil price has a negative effect on the Green Bond Index and carbon price due to higher oil prices may lead to higher consumption of non-fossil energy, and then reducing the demand and willingness of companies to raise green financing. These research findings are also in line with [Mensah et al. \(2019\)](#), which provide evidence of causality that runs from the oil returns to the CO<sub>2</sub> futures' returns. For example, [Mensah et al. \(2019\)](#) determined a unilateral effect from oil prices to carbon emissions both in the long and short run. In contrast, [Marín-Rodríguez et al. \(2022b\)](#) found a unidirectional causality running from the Green Bond Index to the Brent oil returns, a unidirectional causality running from the Green Bond Index to the CO<sub>2</sub> futures' returns, and a unidirectional causality running from the Brent oil returns to the CO<sub>2</sub> futures' returns.

(ii) The wavelet coherence analysis results also show that there is a causal relationship between CO<sub>2</sub> futures' returns and oil prices, which was negative in 2014 (short-term) and 2021 (medium-term); however, this relationship becomes positive in 2019–2020 (medium-term). This paper's finding is in line with [Li et al. \(2022\)](#), who showed that carbon emissions trading is negatively affected by oil price shocks, and the impact is negative in both the short and medium term. A possible explanation for this is that an increase in oil prices may lead to a rise in the use of low-carbon energy and then diminish firms' demand for carbon credits.

(iii) Finally, other results from wavelet coherence suggest that the Green Bonds Index negatively affects the CO<sub>2</sub> futures' returns in the medium-term in 2022. Additionally, the Green Bond Index significantly affected CO<sub>2</sub> futures' returns positively (2014 and 2019–2020) and negatively (2015–2016 and 2021) in the short-term, medium-term, and long-term. In contrast, [Li et al. \(2022\)](#) using time-varying impulse response analysis found that carbon emission trading price is mainly positively affected by the impact of the Green Bond Index in the short and medium-term and tends to 0 in the long term.

The findings in this study extend several implications for researchers, managers, policymakers, and decision-makers. Thus, (i) The negative relationship between oil prices and green bonds causes the financial markets to generate incentives to raise green financing in the context of higher oil prices. Additionally, the positive linkage between oil prices and CO<sub>2</sub> emissions generates that policy decisions on the transition of energy to a decarbonized economy should consider the incentives for generating green bond issuances, which are an essential instrument for the transition to a climate-resilient economy. These results are in line with [Jin et al. \(2020\)](#).

Our findings are also relevant in the contribution to formulating green finance policies and supporting renewable investments. This is due to the negative relation found between

green bonds and CO<sub>2</sub> emissions. This topic acquires a particular interest in emerging countries where more outstanding efforts are required to expand the offer of these eco-friendly instruments. The preceding is because, for example, in Latin American and the Caribbean markets there is a strong demand for this type of instrument by investors in the local markets. Additionally, the support from policymakers towards the generation of energy transition policies could facilitate and encourage the generation of renewable energies procuring the criteria of climate bond initiatives.

The findings are also according to [Jin et al. \(2020\)](#), who suggests that investors in green bond markets are sensitive to fluctuations in energy and carbon markets because the carbon market can reflect climate change, uncertainty in green public policies, and changes in geopolitical situations. Additionally, we can admit that the search for sustainable investments promoted for the climate change risk has increased the popularity of green bonds, contributing to the enhanced correlation among the green bond market, oil prices, and the carbon market. This phenomenon can explain that during the outbreak of COVID-19 and the recent Russian invasion of Ukraine in February 2022, a greater percentage of co-movement among green bonds was driven by linkage connections among the markets ([Tiwari et al. 2022](#)).

Finally, for market players and decision-makers, our results can help to improve portfolio composition since we present the diversification potential of green bonds to CO<sub>2</sub> emissions and oil prices. Furthermore, based on the principal findings, several co-movements patterns in different frequency bands suggest that investors should determine the corresponding risk prevention strategies based on their investment time horizons. The above results can assist investors in making portfolio selection decisions within Brent oil price, green bond markets, and carbon markets, as well as scale-conscious (or investment horizons-conscious) traders making trading decisions, as [Omane-Adjepong et al. \(2019\)](#) and [Qureshi et al. \(2020\)](#) mentioned.

## 6. Conclusions

The present study explores the time-dependency among the Brent oil returns, the Green Bond Index, and the CO<sub>2</sub> futures' returns using the wavelet power spectrum and wavelet coherence for measuring the co-movements and causality test over the period 2014 to 2022 over different time frequencies: short, middle, and long term. The use of the wavelet approach permits the present research to (i) capture the volatility periods of the Brent oil returns, the Green Bond Index, and the CO<sub>2</sub> futures' returns; and (ii) to study the short-term, medium-term and long-term causal relationships among the Brent oil returns, the Green Bond Index, and the CO<sub>2</sub> futures' returns since the approach combines both time and frequency domain causalities.

Understanding the co-movements among the Brent oil returns, the Green Bond Index, and the CO<sub>2</sub> futures' returns are essential in assessing macroeconomic performance in the global decarbonization scenario. These three instruments are fundamental in implementing Sustainable Development Goals (SDGs) and the three traditional pillars of sustainable development based on the environmental, social, and economic domains. The SDGs represent the efforts to guide humanity toward long-term prosperity, and the variables used in this study are essential in the analysis of the global goals about affordable and clean energy, sustainable cities and communities, responsible consumption and production, and climate action. However, their implementation represents significant challenges due to the tensions and trade-offs among the three pillars of sustainability ([Giuliodori et al. 2022](#)). In this context, knowing the relationships among these variables can help researchers, managers, policymakers, and decision-makers to understand the importance of the oil price shocks on the design of assets and policies that tend to improve sustainability practices. For example, [Rodriguez-Fernandez \(2016\)](#) found a positive bidirectional relationship between Corporate Social Responsibility and Financial Performance, originating a positive feedback virtuous circle in Spanish-listed companies.



On the other hand, based on Kirikkaleli and Güngör (2021), climate change risk and its direct and indirect impacts on the price formation of energy markets and assets related to sustainable finance seem to be one of the main areas of further research due to the pressures of climate change over production technologies, investment practices, and regulations. In this point, green bonds have a pivotal role in being an essential instrument for financing energy transition reinforcing the importance it should have for policymakers to improve the legal framework relating to their issuance. Thus, there is great potential for further research on exploring the relationships among the Brent oil returns, the Green Bond Index, and the CO<sub>2</sub> futures' returns, for example, using artificial intelligence techniques such as machine learning models that have been used for predicting the direction of markets. In particular, deep learning strategies that use neural networks can be helpful for measuring the co-movements among the variables considered; for example, Deep Neural Networks (DNN); Convolutional Neural Networks (CNN); Autoencoders; and Recurrent Neural Networks (RNN) like Long Short-Term Memory (LSTM), Bidirectional LSTM (BiLSTM), stacked LSTM (SLSTM) or Gated Recurrent Unit (GRU) networks. These studies could also be extended to Latin American and Caribbean markets, where the lack of data makes this kind of research scarce.

Although this study enlarges the discussion around the dynamic association among oil prices, green bonds, and CO<sub>2</sub> emissions and addresses the diversification potential of green bonds to CO<sub>2</sub> emissions prices and oil prices in different frequency bands, a possible limitation of our study can be related to the data time-frequency. For example, some investors in energy markets and sustainable assets can prefer to make decisions over longer investment horizons, which is in line with Saeed et al. (2021). Therefore, future research can address this limitation by using lower frequency data (i.e., weekly or monthly data) and considering the heterogeneity of investors over different investment horizons.

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