

*Article*



# **Experimental and Numerical Analysis on Mesoscale Mechanical Behavior of Coarse Aggregates in the Asphalt Mixture during Gyratory Compaction**

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**Abstract:** Compaction is a critical step in asphalt pavement construction. The objective of this study is to analyze the mesoscale mechanical behaviors of coarse aggregates in asphalt mixtures during gyratory compaction through experiments and numerical simulation using the Discrete Element Method (DEM). A novel granular sensor (SmartRock) was embedded in an asphalt mixture specimen to collect compaction response data, including acceleration, stress, rotation angle and temperature. Moreover, the irregularly shaped coarse aggregates were regenerated in the DEM model, and numerical simulations were conducted to analyze the evolution of aggregate interaction characteristics. The findings are as follows: (1) the measured contact stress between particles changes periodically during gyratory compaction, and the amplitude of stress tends to be stable with the increase of compaction cycles; (2) the contact stress of particles is influenced by the shape of aggregates: flat-shaped particles are subjected to greater stress than angular, fractured or elongated particles; (3) the proportion of strong contacts among particles is high in the initial gyratory compaction stage, then decreases as the number of gyratory compactions grows, the contacts among particles tending to homogenize; (4) during initial gyratory compactions, the normal contact forces form a vertical distribution due to the aggregates' gravity accumulation. The isotropic distribution of contact forces increases locally in the loading direction along the axis with a calibrated internal angle orientation (1.25°) in the earlier cyclic loading stage, then the local strong contacts decrease in the later stage, while the strength of the force chains in other directions increase. The anisotropy of aggregate contact force networks tends to weaken. In other words, kneading and shearing action during gyratory compaction have a positive impact on the homogenization and isotropy of asphalt mixture contact forces.

**Keywords:** gyratory compaction; granular sensor; Discrete Element Method; contact stress; homogenization; isotropy

# **1. Introduction**

Gyratory compaction is one of the main preferred methods to mold asphalt mixtures. With vertical pressure and horizontal shear simultaneously applied to the specimen, gyratory compaction can simulate the wheel kneading action during the asphalt pavement construction stage and the open traffic stage. Research has shown that the features of samples formed by gyratory compaction are closest to those of on-site core samples, and aggregate cracking can be alleviated during gyratory compaction [\[1](#page-14-0)[–3\]](#page-14-1). Led by the National Highway Cooperative Research Program (NCHRP), the Superpave Gyratory Compactor



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(SGC) has been widely used in the United States [\[4,](#page-14-2)[5\]](#page-14-3). At present, according to the densification curves recorded by SGC, volume indicators to characterize the compaction mechanism have been proposed, including the theoretical maximum relative density  $(G_{mm})$ , the initial number of gyrations  $(N_{\text{ini}})$  [\[6\]](#page-14-4), the compaction energy index (CEI) [\[7\]](#page-14-5), densification curve slopes, the locking point  $[8-10]$  $[8-10]$ , and the ratio of compaction cycles when the air void of asphalt mixture reaches 2% and 5% [\[11\]](#page-14-8). The criteria based on the above volume parameters has not been unified. For instance, there are several criteria for defining the locking point according to the specimen's height change during gyratory compaction [\[8,](#page-14-6)[12](#page-14-9)[–16\]](#page-14-10). Furthermore, to obtain a more reasonable and acceptable method to describe the compactability of the asphalt mixture, novel sensors and numerical methods [\[17\]](#page-15-0) are used to characterize the force framework evolution of coarse aggregates, and attempts have been made to establish the relationship between volume parameters and mechanical indexes for asphalt mixtures.

With the development of sensors, a new integrated granular sensor called SmartRock has been introduced [\[18](#page-15-1)[–22\]](#page-15-2) and embedded in asphalt mixture to record physical and mechanical behavior data during compaction. With a size close to the nominal maximal particle size, the SmartRock can collect compaction response data, including stress, rotation angle, acceleration and temperature, and transmit it wirelessly to a LabVIEW system. Wang [\[18\]](#page-15-1) obtained the variation of particle attitude (rotation angle) during gyratory compaction utilizing SmartRock, and a method for determining the locking point based on the relative rotation angle curves was preliminarily suggested. Subsequently, Wang and Shen [\[19\]](#page-15-3) conducted more field compaction tests using SmartRocks, and the results proved that the acceleration tested by SmartRock could better reflect the dynamic characteristics of asphalt mixture under the action of a vibratory roller. In addition, the rotation angle tested by SmartRock could also explain the impact of rubber-tired rollers on the rolling and rubbing action for asphalt mixture. Han et al. [\[20](#page-15-4)[,21\]](#page-15-5) used SmartRock to compare dynamic responses, such as stress, acceleration and rotation angle, during on-site and indoor vibratory compaction, and found that the average stress tested by SmartRock could indicate the compaction trend of the asphalt mixture. However, this work is limited by the high cost and discrete characteristics of SmartRock sensor testing. Recently, the Discrete Element Method (DEM) was employed as a numerical technology to simulate asphalt mixing [\[23–](#page-15-6)[25\]](#page-15-7) and the compaction process [\[26](#page-15-8)[–29\]](#page-15-9). Initially, 2D simulation models were built to analyze the dynamic modulus of mixtures and the law of particle motion, and to reveal the gyratory compaction mechanism of asphalt mixture [\[27\]](#page-15-10). Considering the influence of irregular particle shapes on the compaction process, scholars have combined 3D scanning technology and DEM to simulate real-shaped particles [\[28](#page-15-11)[–30\]](#page-15-12), and a more accurate representation of particle movement during compaction was achieved. However, there is still a lack of numerical analysis on the evolution of the interior force framework for aggregates during compaction.

The objective of this paper is to investigate the movement characteristics and mechanical behavior of coarse aggregates during gyratory compaction utilizing a granular sensor monitoring test and a numerical simulation. The main work includes: (1) obtaining the movement and contact stress of SmartRock during gyratory compaction; (2) preparing the compacted sample with a combination of differently shaped coarse aggregates through DEM simulation; (3) building the DEM model and simulating the gyratory compaction process to track the movements and contact forces of coarse aggregates; (4) comparing and analyzing the results between the test and numerical model and detecting the mesoscale force chain characteristics of aggregates.

#### **2. SGC Testing Based on SmartRock**

# *2.1. SmartRock*

SmartRock is a small-size sensor developed for monitoring granular forces, deformation, stability, etc., of railway ballasted bed [\[31\]](#page-15-13) and highway pavements. With the particle level size, all of the above studies have been extended from macroscale to mesoscale and have achieved meaningful results. The sensor system consists of three modules according

to their functions: a data module, a communication module and a power module. The data are collected and stored instantly in the data module, including global time, temperature, stress, Euler angles under quaternion or geodetic coordinates, and acceleration. The shell of the sensor can be made in a specified shape. The sensor used in this study was filled in a cube shell 23  $\times$  23  $\times$  23 mm [in](#page-2-0) size, as shown in Figure 1a, of which material strength and the bonding performance with the asphalt mixture are similar to the actual aggregate of the mixture. The test data were transmitted to a portable receiver [\(Fi](#page-2-0)gure 1b) using Bluetooth Low Energy technology in the communication and power module and can be displayed and recorded in real time. As the working temperature of the sensor should be within 120 °C, a thermal insulation [lay](#page-2-0)er (Figure 1c) is wrapped around the particle shell. Therefore, the sensor, embedded in hot mix asphalt mixture, can work normally under high temperatures over 120 °C during compaction.

<span id="page-2-0"></span>

Figure 1. The SmartRock sensor: (a) dimensions of the shell; (b) the portable signal receiver; (c) the thermal insulation layer. thermal insulation layer.

The pressure measuring principle of SmartRock is to test and convert voltage to stress The pressure measuring principle of SmartRock is to test and convert voltage to stress value. During compaction, the compressed sensitive film in SmartRock generates a slight deformation and a change in the resistance value of the strain gauge. Furthermore, the deformation and a change in the resistance value of the strain gauge. Furthermore, the stress on the particle can be determined based on the voltage value, and the stress value stress on the particle can be determined based on the voltage value, and the stress value can be determined by Equation (1): can be determined by Equation (1):

$$
f = \frac{U - U_0 - b \cdot lnT - c}{aA} \tag{1}
$$

where f (kPa) is the stress value;  $U$  (V) is the voltage signal recorded;  $U_0$  is the basic voltage signal before compaction;  $T({}^{\circ}C)$  is the temperature;  $\overrightarrow{A}$  (m<sup>2</sup>) is the area of the strain gauge; a,  $\overline{b}$  and *c* are calculation coefficients. Three sensors (R1, R2, R3) were employed in this study and the calculation parameters of each sensor are listed in Table [1.](#page-2-1)

<b>Sensor</b>	Direction	a	b	c	$U_0$
	X	$-0.04771$	0.09367	$-0.7178$	2.28
R1	v	$-0.05377$	0.127	$-1.137$	2.3
	z	$-0.06123$	0.06668	$-0.6924$	2.38
R <sub>2</sub>	X	$-0.044$	$-0.06509$	0.04185	2.32
	v	$-0.05006$	$-0.06509$	$-0.08448$	1.86
	z	$-0.05262$	$-0.02223$	$-0.3959$	2.04
R3	X	$-0.05348$	0.09208	$-0.6609$	2.3
	v	$-0.06735$	$-0.02064$	$-0.4156$	2.44
	Z	$-0.05227$	0.003175	$-0.4239$	2

<span id="page-2-1"></span>**Table 1.** Parameters of the SmartRock for stress conversion. **Table 1.** Parameters of the SmartRock for stress conversion.

#### *2.2. Preparation of SGC Testing Materials and Equipment*

In order to reduce the influence of SmartRock's size on the compactability of the asphalt mixture, AC-20C mixture (the maximum particle size is close to the SmartRock's size) was selected for gyratory compaction. Moreover, the technical indicators of coarse aggregate, filler and bituminous binder are listed in Tables [2–](#page-3-0)[4,](#page-3-1) respectively.

<span id="page-3-0"></span>**Table 2.** Technical indicators of coarse aggregate.



**Table 3.** Technical indicators of filler.



<span id="page-3-1"></span>**Table 4.** Technical indicators of bituminous binder.



According to the inspection results listed in Table [2](#page-3-0) through to Table [4,](#page-3-1) all materials meet the requirements of the Technical Specification for Highway Asphalt Pavement Construction (JTG F40-2004) [\[32\]](#page-15-14). The gradation curve of the AC-20C mixture is shown in Figure [2.](#page-3-2)

<span id="page-3-2"></span>

**Figure 2.** Gradation curve of the AC-20C mixture. **Figure 2.** Gradation curve of the AC-20C mixture.

The gradation of the AC-20C mixture is listed in Table [5,](#page-4-0) and the optimal asphalt content is 4.2%. The volumetric and mechanical characteristics of the mixture are shown in Table [6,](#page-4-1) and both meet the specification requirements.

<span id="page-4-0"></span>

$0 - 3$	$3 - 5$	$5 - 10$	$10 - 15$	$15 - 25$	Mineral Powder	<b>Bituminous</b> <b>Binder</b>
27(%)	10(%)	19(%)	15(%)	26(%)	3(%)	4.2 $(%)$

<span id="page-4-1"></span>**Table 6.** Summary of the volumetric and mechanical parameters of the AC-20 asphalt mixture.



The Superpave gyratory compactor manufactured by the PINE instrument company was adopted in this test, as shown in Figure [3a](#page-4-2). The operation parameters used in the study consisted of the rotation speed at 30 r/min with a calibrated internal angle of 1.25◦ and a stress of 600 kPa. The diameter of the molding specimen is 150 mm. During gyratory compaction, the top plate remains fixed, and the bottom plate under upward pressure rotates with the mold.

<span id="page-4-2"></span>

**Figure 3.** Superpave gyratory compactor: (**a**) the compactor; (**b**) the compaction process. **Figure 3.** Superpave gyratory compactor: (**a**) the compactor; (**b**) the compaction process.

# *2.3. Layout and Application of SmartRocks 2.3. Layout and Application of SmartRocks*

Several indoor experiments with SmartRock were carried out to investigate the compaction response characteristics from a mesoscale perspective. The application of SmartRocks in gyratory compaction is illustrated as follows. tRocks in gyratory compaction is illustrated as follows.

Each testing specimen weighed 4.8 kg. The mixing temperature of the asphalt mixtures was set to 180 °C, and the compaction temperature ranged from 160–170 °C. To distinguish the possible impact on the compaction process caused by the SmartRock's embedded  $\rm{locations, three\ groups\ of\ tests\ were\ carried\ out\ with\ SmartRock\ up-located\ (Test\ 1), mid-$ located (Test 2), and bottom-located (Test 3) in the sample, respectively (see Figure [4a](#page-5-0)). After compaction and testing, the sensor was taken out at a high temperature from the demolding specimen (as shown in Figure [4b](#page-5-0)). the demolding specimen (as shown in Figure 4b).

<span id="page-5-0"></span>

**Figure 4.** SmartRocks in SCG specimen: (**a**) test loaction; (**b**) after compaction. **Figure 4.** SmartRocks in SCG specimen: (**a**) test loaction; (**b**) after compaction.

During the test, the sampling frequency for stress, acceleration and rotation angle During the test, the sampling frequency for stress, acceleration and rotation angle acquisition was set to 100 Hz. The quaternion could be transformed into an Euler angle, acquisition was set to 100 Hz. The quaternion could be transformed into an Euler angle, and all gathered signals should be filtered to reduce noise interference. and all gathered signals should be filtered to reduce noise interference.

# **3. Discrete Element Simulation for Gyratory Compaction 3. Discrete Element Simulation for Gyratory Compaction**

*3.1. Model Construction with Irregularly Shaped Aggregates 3.1. Model Construction with Irregularly Shaped Aggregates*

of asphalt mixture compaction behavior [\[33\]](#page-15-15). Therefore, Gong obtained point cloud data tion of asphalt mixture compaction behavior [33]. Therefore, Gong obtained point cloud of particle profiles with 3D laser scanning [\[26\]](#page-15-8) and divided the overall morphological Previous studies reported that particle shape had a significant impact on the simulation characteristics of aggregates into five categories (rounded, fractured, angular, elongated and flat) according to ASTM D 4791 and 5821 [\[34,](#page-15-16)[35\]](#page-15-17). Based on the statistical results, most particles were fractured and angular, and only a small number of particles were elongated and flat [\[33\]](#page-15-15). In this study, an open-source discrete element simulation program (YADE) was used to simulate the gyratory compaction process. Considering the particle morphology distribution characteristics [\[33\]](#page-15-15), a reconstruction method for polyhedral particles based on Voronoi tessellation [\[36–](#page-15-18)[38\]](#page-15-19) was employed to set up a sample library for irregularly shaped particles. For each particle, the reconstruction method is illustrated as follows:

- 1. In 3D space, seed nuclei with random coordinates are firstly arranged around the center nuclei C. The 3D space is divided into multiple polyhedrons by the vertical bisector of adjacent seed nuclei, and the polyhedron containing the center nuclei C is obtained as the basic particle shape.
- 2. Figure [5a](#page-6-0) shows the schematic diagram in 2D. Each particle shape is further adjusted to make the grading curve of the particle sample library satisfy the gradation requirement of the asphalt mixture. As shown in Figure [5b](#page-6-0), spindle tension and rotation are mainly utilized to adjust particle size. The final particle shape for 3D simulation is shown in Figure [5c](#page-6-0).

3. After generating the polyhedrons, including three shape categories—angular particles, fractured/elongated particles and flat particles—each polyhedron is filled with densely arranged spheres to form a clump, as shown in Figure 6. In addition, asphalt binder and aggregates with sizes less than 3 mm are directly simulated by spherical particles.  $\blacksquare$ 

<span id="page-6-0"></span>

**Figure 5.** Particle reconstruction based on Voronoi tessellation: (**a**) basic particle shape generation; (**b**) spindle tension and rotation for shape adjustment; (**c**) 3D particle shape for simulation.

#### *3.2. Gyratory Compaction Process Simulation*

For the DEM model, aggregates were randomly generated according to the method described in the previous section and initially stacked by gravity (see Figure [7a](#page-7-1)). Then, the top plate was fixed, while the mold was rotated around the central point of the top plate until the rotation angle reached 1.25°. During gyratory compaction, the bottom plate was under a pressure of 600 kPa. The mold rotated around the central axis at a speed of 0.5 r/s, and the final compacted model is shown in Figure [7b](#page-7-1). The process data for the bottom plate position and the aggregate movement were recorded. In addition, asphalt binder was considered to play a lubricating role with respect to fast movement and large displacement [\[39\]](#page-15-20), so that the linear contact model was adopted to simulate the gyratory compaction behavior, with the meso-parameters listed in Table [7.](#page-8-0) The computer used for calculation was configured with a dual core CPU with model Intel Core I7-9700 and 3.1 GHz using the Ubuntu 16.04 operating system. The total simulation time lasted about 44 h.





**Figure 6.** Clump models. **Figure 6.** Clump models.

<span id="page-7-0"></span>Angular

<span id="page-7-1"></span>

Figure 7. DEM simulation process: (a) stacked states by gravity; (b) compacted states after gyratory compaction.



(**a**) (**b**)

<span id="page-8-0"></span>Table 7. Meso-parameters of DEM model.

#### **4. Results and Discussion**  $T$  and  $T$  change change compact compact  $\alpha$  or compact  $\alpha$  three tests were recorded specific were recorded specific were recorded specific weak and  $T$

# 4.1. Specimen Height Change **and compared with the DEM simulation result**, as shown in Figure 8. The compared 8. The compaction results are all the compaction results as shown in Figure 8. The compaction results are all th

The height change curves for compacted specimens from three tests were recorded and compared with the DEM simulation result, as shown in Figure 8. The compaction efficiency (height change) of the DEM model was greater than the test results in the several einciency (neight change) of the DEM model was greater than the test results in the several initial rotations (before 10 cycles). In addition, the reduction rate of specimen height in the DEM model became slower in the subsequent gyratory compaction stage. Unlike Burger's contact model with a damping pot, the linear contact model used in this paper ignored the viscosity of the asphalt binder, which might explain the height change rule distinction between the DEM simulation and the test results. between the DEM simulation and the test results.

<span id="page-8-1"></span>

**Figure 8.** Specimen height change comparison between tests and the DEM model.

#### *4.2. Contact Stress of Aggregates*

Figure [9](#page-9-0) shows the contact stress results of particles measured by SmartRock at different locations in three testing groups. It can be seen that the measured stress changes periodically during gyratory compaction, and the stress amplitude tends to be stable asgyrations increase. The stress value range fluctuates from 350 kPa to 750 kPa. Each particle's contact stress is also tracked in the simulation model. The result indicates that the particles' contact stress evolution in the DEM model is similar to the test result. However, the particles' contact stress is discrete due to the particles' shapes. Figure [10](#page-10-0) shows the particles' contact stress obtained in the simulation model; particles with three different shapes (angular, fractured/elongated and flat) are located in the middle layer of the specimen. As can be seen in Figure [10,](#page-10-0) the contact stress range for the angular particle (300 kPa~800 kPa) is close to that for the fractured/elongated particle (300 kPa~700 kPa).

Nevertheless, the flat particles' contact stress (1200 kPa~1600 kPa) is significantly higher<br>than the other particles'. Similarly, sep elusions, sep ha dresse for other particles with than the other particles'. Similarly, conclusions can be drawn for other particles with different shapes according to the simulation results. It can be inferred that the flat particles are easy to trap in stress concentration, resulting in their being crushed during gyratory compaction. Therefore, the proportion of flat particles in the mixture should be reduced as much as possible. for the fractured/elongated particle (300 kPa~700 kPa). Nevertheless, the flat particles' con-

 $\mathcal{F}_{\mathcal{A}}$  figure 10, the contact stress range for the angular particle (300 kPa $^2$ 00 kPa $^2$ 00 kPa) is close to that

<span id="page-9-0"></span>

**Figure 9.** Particles' contact stress tested by SmartRock located in (**a**) upper, (**b**) middle and (**c**) bottom positions of the specimen.

<span id="page-10-0"></span>

**Figure 10.** Particles' contact stress (with angular, fractured/elongated and flat shapes) located in the **Figure 10.** Particles' contact stress (with angular, fractured/elongated and flat shapes) located in the mid-layer, tracked by DEM. mid-layer, tracked by DEM.

#### *4.3. Contact Force Network Characteristics*

Previous studies have proved that the normal contact force inside granular materials plays a major role in bearing external loads [\[40\]](#page-15-21). In this paper, the average normal contact place  $\leq n$  is defined as the average value of the hormal contact forces. In addition, strong and weak contacts among particles construct a contact force network to resist external loads. Strong contacts bear the major eccentric load, while almost all friction dissipation occurs at force  $\langle f_n \rangle$  is defined as the average value of the normal contact forces. In addition, strong

weak contacts [\[41\]](#page-15-22). In this paper, normal contact force less than the average normal contact force is recorded as weak contact, with the converse holding for strong contact.

Figure [11](#page-11-0) shows the evolution of a normal contact force (force chain) network under different compaction cycles (2, 50, 80 and 110 cycles). The distribution of normal contacts between particles becomes denser as the compaction cycle increases. Moreover, the strong contacts in the upper and middle parts of the specimen gradually increase in the compaction process. The proportions of strong contacts in the upper, middle and lower parts of the specimen vary from 21.9%, 18.3% and 19.1% to 27.8%, 20.1% and 20.5%, respectively. The  $\,$ maximum normal contact force of particles reaches 450 N in 110 cycle, which is located in the middle of the specimen. The probability distribution function (PDF) of contact force is often used to quantitatively study the non-uniformity of contact force networks [\[42\]](#page-15-23). The average normal contact force is normalized by the contact force *fn* in each normal direction, and the normalized  $f_n/\langle f_n \rangle$  is obtained. The PDF of  $f_n/\langle f_n \rangle$  under different compaction cycles (2 and 110 cycles) is shown in Figure [12.](#page-12-0) The strong contact proportion is high in the initial gyratory compaction stage. With the increase of cycles, the strong contact proportion decreases, and the contacts among particles tend to homogenize in the compaction process.

<span id="page-11-0"></span>

Figure 11. Normal contact force distribution under different compaction cycles: (a) 2 cycles; cycles; (**c**) 80 cycles; (**d**) 110 cycles. (**b**) 50 cycles; (**c**) 80 cycles; (**d**) 110 cycles.

<span id="page-12-0"></span>

cycles; (**c**) 80 cycles; (**d**) 110 cycles.

**Figure 12.** The evolution of the probability distribution function (PDF) for normalized normal contact force  $f_n$  /  $\leq f_n$  > with 2 and 110 compaction cycles.

The three-dimensional spherical histogram can be used to visually describe the spatial distribution of the normal contact force, in which each column bar (in each discrete direction) represents the normalized local average normal contact force  $f_n/f_0$  in this direction. The local average normal contact force  $\overline{f_n}$  is defined as the average value of the normal contact force falling in a solid angle interval. It should be noted that the term "local" is used to distinguish it from the average value  $\langle f_n \rangle$  ("global") of all contact forces. Besides  $\langle f_n \rangle$ , another global average value  $\overline{f_0}$  is introduced.  $\overline{f_0}$  equals the average of  $\overline{f_n}$  in all discrete directions. Therefore,  $\langle f_n \rangle$  is equal to  $f_0$  for a uniformly distributed normal contact force direction. Moreover, for the isotropic normal contact force, the spherical histogram is an exact sphere with radius 1. The non-spherical histogram means the anisotropic distribution of normal contact force. Figure [13](#page-13-0) shows the spatial distribution of the local average contact forces of the specimen under different numbers of gyrations (2, 50, 80 and 110 cycles). In the initial gyratory compaction (at two cycles), the normal contact forces form a close to vertical distribution, which is caused by the initial vertical gravity accumulation of the aggregates. In the process of gyratory compaction, the spherical histogram increases locally in the loading direction (along the axis with a calibrated internal angle of 1.25°), which means that strong contacts form and grow at 50 cycles. However, at 110 cycles, the local strong contacts along the axis with a calibrated internal angle of  $1.25^\circ$  decrease. While the strength of the force chains in other directions increase, the anisotropy of the aggregates' contact force network tends to weaken. Combined with the previous PDF features, kneading and shearing action during gyratory compaction can have a positive effect on the homogenization and isotropy of asphalt mixture contact force.

<span id="page-13-0"></span>

**Figure 13.** 3D spherical histogram of local average normal contact force  $\overline{f}_n$  under different gyratory compaction cycle: (**a**) in front view; (**b**) in vertical view.

## **5. Conclusions**

This study was carried out to analyze the mesoscale mechanical behaviors of coarse aggregates in asphalt mixtures during gyratory compaction. The particles' contact stress was obtained by a novel granular sensor (SmartRock), and the evolution of the normal contact network for aggregates was explored and developed in a DEM simulation model. The mechanistic results can be used to guide on-site compaction control and mix proportion design. In summary, the main findings are as follows:

- 1. The measured contact stress among particles changes periodically during gyratory compaction, and the amplitude of stress tends to be stable with the increase of compaction cycles;
- 2. Particles' contact stresses are discrete and influenced by the shapes of aggregates. Flat particles are subjected to greater stress than the angular and fractured/elongated particles during gyratory compaction;
- 3. It can be inferred that flat particles are easy to trap in stress concentrations, resulting in their being crushed in gyratory compaction. Therefore, the proportion of particles with flat shapes in a mixture should be reduced as much as possible;
- 4. According to the contact network simulated by DEM models, the proportion of strong contacts is high in the initial gyratory compaction stage and decreases with the

increase of compaction cycles. The contacts among particles tend to homogenize in the compaction process.

5. Given the gravity accumulation of the aggregates, the normal contact forces of samples form vertical distributions in the initial gyrations. Strong contacts form and grow up locally along the axis in 1.25◦ orientation at earlier cyclic loading, then decrease in the later stage. The anisotropy of aggregate contact force networks tends to be weakened by kneading and shearing of the asphalt mixture.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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