



# *Article* **CFD Investigation on the Performance of Cyclone Separators with Divergent or Convergent Insertion Pipes**

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**Abstract:** For multi-phase separation, developing high-performance cyclone separators is highly demanded. In this study, different divergent or convergent insertion pipes bFelow the vortex finder are employed to improve the separation performance. The impacts of insertion pipe geometrical configurations on the flow characteristics, pressure drop, and separation efficiency are systematically analyzed. The results reveal that the employed insertion pipe can significantly affect the static pressure distribution inside the cyclone. A longer insertion pipe length and larger tilt angle result in a wider central low-pressure area and smaller overall static pressure. The divergent insertion pipes increase pressure loss, while the convergent insertion pipes augment pressure loss. A larger insertion pipe length significantly impacts the axial velocity distribution. For divergent insertion pipes, the maximum central axial velocity increases with increasing tilt angles and then decreases. For small particles  $(d_p \leq 5 \mu m)$ , a convergent insertion pipe exhibits a better separation performance. When the particle diameter  $d_p \geq 5$  µm, divergent insertion pipes with larger angles and lengths can significantly decrease the pressure drop while guaranteeing satisfied collection efficiency. When *L* = 75 mm and  $\theta$  = 60 $\degree$ , the pressure drop is reduced by 7.8%. This study may contribute to rationally designing high performance cyclone separators and also paves ways for improving the existing cyclone separators.

**Keywords:** cyclone separator; axial velocity; insertion pipes; collection efficiency; pressure drop

## **1. Introduction**

With a simple structure and low maintenance cost, cyclone separators are widely applied in industrial two-phase/multi-phase separations such as liquid–gas separation in the natural gas exploitation process [\[1,](#page-15-0)[2\]](#page-15-1) and solid–liquid separation in the fluidized bed coal combustion [\[3,](#page-15-2)[4\]](#page-15-3). Multi-phase separation is achieved by the centrifugal force [\[5](#page-15-4)[,6\]](#page-15-5). In cyclone separators, the rotating turbulence field inside the cyclone is rather complex [\[7,](#page-15-6)[8\]](#page-15-7). Simulations based on Reynolds stress and large eddy models were shown to accurately simulate the flow characteristics in the cyclone separators  $[9-14]$  $[9-14]$ . Compared to the large eddy models and direct numerical simulation(DNS), the Reynolds stress presents less demand on computational resources and satisfied accuracy, which is widely employed to numerically describe the complex flow characteristics inside the cyclone separators [\[15\]](#page-15-10). However, the Reynolds stress model can only provide the average information concerning the turbulence and cannot simulate too complex vortex motion. Griffiths [\[16\]](#page-15-11) concludes that the RNG  $k-\varepsilon$  model can better describe the anisotropy of the turbulent field characteristics using a comparative analysis with experiments. Dang et al. [\[17\]](#page-15-12) proposed a new method to simulate cyclone separators that can simultaneously decrease computational time and enhance accuracy for CFD simulations.

For cyclone separators, pressure loss, as well as separation efficiency, are the main performance indicators that should be addressed [\[18](#page-16-0)[–20\]](#page-16-1). Much attention was drawn to augment their performance. The inlet size is one of the important factors affecting its



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performance [\[21–](#page-16-2)[23\]](#page-16-3). Elsayed et al. [\[24\]](#page-16-4) studied different cyclone separators of various inlet sizes, revealing that the larger inlet size of the cyclone separator contributes to the reduction in the pressure drop. The inlet width presented a much more dominant impact than the inlet height. Horvath et al. [\[25\]](#page-16-5) simulated the axial velocity variation under different geometric configurations. Qian et al. [\[26\]](#page-16-6) investigated different inlet cross-section types and pinch angles. The pressure drop was minimized when the inlet cross-section angle was 45◦ . Tan et al. [\[27\]](#page-16-7) revealed that the larger particle diameter contributes to the separator via experiments and numerical simulations, respectively. However, Liu [\[28\]](#page-16-8) et al. claimed that there exists a critical diameter, leading to the maximum separator efficiency. Ehsan et al. [\[29\]](#page-16-9) found that the baffles have a major effect on improving the separation efficiency and turbulence intensity. In addition, Ehsan et al. [\[30\]](#page-16-10) also studied the effect of the number of inlets and the cyclone cone wall roughness on the swirling flow characteristics and separation efficiency of the cyclone.

The cylinder and the vertebrae are also important components of the cyclone separators, and their length, diameter, angle, and other geometric dimensions act dominantly in determining the pressure drop and separation efficiency [\[31\]](#page-16-11). Lee et al. [\[32\]](#page-16-12) revealed how the cylinder diameter impacts the particle collection efficiencies and flow characteristics. Brar et al. [\[33\]](#page-16-13) revealed that a vertebral length of approximately 6.5 times its diameter can significantly augment the separation efficiency. Demir et al. [\[34\]](#page-16-14) revealed that the friction loss is low at a small vertebral height. Hamdy et al. [\[35\]](#page-16-15) investigated the impacts of vertebral length, showing that increasing the vertebral length could increase the back flow below the vortex finder. Gimbun et al. [\[36\]](#page-16-16) and Elsayed et al. [\[37,](#page-16-17)[38\]](#page-16-18) found that changes in the dust discharge port diameter significantly altered separator performance. Satyanand et al. [\[39\]](#page-16-19) evaluated the effect of various geometrical shapes of the conical segment on cyclone performance, and they predicted the performance of different models using the Reynolds stress model considering two pressure-strain options.

The vortex finder also impacts cyclone separator performance [\[40](#page-16-20)[,41\]](#page-16-21). El-Batsh [\[42\]](#page-16-22) revealed that cyclone separator performance is mainly impacted by the finder diameter rather than the finder length. Tan et al. [\[43\]](#page-16-23) found that satisfied separation efficiency could be achieved when the vortex finder diameter was controlled at 0.3–0.5 *D* where *D* is the cylinder diameter. Hoekstra [\[44\]](#page-16-24) concluded that the maximum tangential velocity and pressure drop gradually decrease with increasing finder diameters. In addition, Hugi et al. [\[45\]](#page-16-25) revealed that under some situations of particle size distributions, employing vortex finders is unnecessary.

Although performance improvement and optimization of the cyclone separator were extensively studied in the previous literature, the separation performance of ultra-fine particles is still far from satisfied. Since the escape of particles is through the vortex finder at the upper end of the cyclone, optimizing the vortex detector can greatly improve the separation performance of the separator. In this study, unlike the optimized vortex detector shapes in previous studies, different divergent or convergent insertion pipes below the vortex finder were constructed to improve the internal flow characteristics and, thus, increase the separation efficiency. The Reynolds stress turbulence model is employed to describe the rotating turbulence field inside the cyclone. The pulsation velocity in all the flow directions has a significant impact on the movement velocity of small particles. To fully grasp the influence of these factors on the turbulence and pulsation velocity, the discrete random walk (DRW) is applied for particle tracking [\[46](#page-16-26)[,47\]](#page-16-27). The impacts of different divergent or convergent insertion pipes on the flow field characteristics, separation performance, and pressure loss were systematically analyzed. The undermining mechanisms are discussed. Finally, some useful conclusions are drawn. This study may contribute to rationally designing high performance cyclone separators and also pave the way for improving the existing cyclone separators.

# 2. Model Description

## 2.1. Geometrical Characteristics

As depicted in Figure [1,](#page-2-0) the reverse-flow cyclone with a volute inlet is employed for the numerical simulation. The sizes of the cyclone separator are based on Ref. [15]. The relevant modeling parameters of the studied cyclone separator are presented in Table [1.](#page-2-1) Different divergent or convergent insertion pipes are attached below the vortex finder. The divergent or convergent insertion pipes are characterized by the angle (*θ*) and length (*L*).<br>The langth *L* is set at 25–50 and 75 game association with the sure the study from a 20 to The length *L* is set at 25, 50, and 75 mm, respectively; and the angle *θ* varies from −30 to  $60°$ . *θ* = 0° or *L* = 0 mm in the study refers to the original configuration without installation of the insertion pipes, as shown in Figure [2b](#page-3-0).  $\theta > 0^\circ$  indicates the insertion pipe is divergent; θ < 0° represents that the insertion pipe is convergent. Figure 2a,c show the shape of the insertion pipes with  $\theta = 30^\circ$  and  $-15^\circ$  at the length  $L = 50$  mm, respectively.

<span id="page-2-0"></span>



<span id="page-2-1"></span>**Figure 1.** Geometrical diagram of the reverse-flow cyclone separator.



<span id="page-3-0"></span>

**Figure 2.** Divergent or convergent insertion pipes. **Figure 2.** Divergent or convergent insertion pipes.

### *2.2. Computational Fluid Dynamics Model*

# 2.2.1. Reynolds Stress Model

**Parameter Value**  Although the simulation accuracy of a large eddy simulation is better, it requires too many computational resources. Considering the simulation computational cost and the The SIMPLE algorithm is used for dealing with the pressure–velocity coupling; the PRESTO scheme is employed for dealing with the pressure gradient; and the QUICK differential format is applied to handle the other physical items  $[15]$ . accuracy of the simulation, the Reynolds stress model (RSM) is employed in the simulation.

The time-averaged conservation equations are applied to describe the rotating turbu-lence field inside the cyclone separator [\[48\]](#page-16-28):

$$
\frac{\partial \overline{u_i}}{\partial x_j} = 0 \tag{1}
$$

$$
\rho \overline{u_i} \frac{\partial \overline{u_i}}{\partial x_j} = -\frac{\partial \overline{P}}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ \mu \left( \frac{\partial \overline{u_i}}{\partial x_j} + \frac{\partial \overline{u_j}}{\partial x_i} \right) \right] - \frac{\partial \rho \overline{u'_i u'_j}}{\partial x_j}
$$
(2)

where  $\overline{u_i}$  and  $\overline{u_j}$  are the mean velocities;  $\rho \overline{u_i'u_j'}$  is the Reynolds stress caused by turbulent  $\mathbf{m}$  resources. Computations. Computations computations computations considering the simulation considering the simulation considering the simulations considering the simulation considering the simulation considering pulsations.

The RSM model is a turbulence model based on each anisotropy, without using Boussinesq's assumptions, that is suitable for solving strong cyclonic flows inside the cyclone separator;  $\alpha$ cyclone separator.

$$
\frac{\partial}{\partial t}\left(\rho \overline{u_i'u_j'}\right) + \frac{\partial}{\partial x_k}\left(\rho u_k \overline{u_i'u_j'}\right) = D_{T,ij} + D_{L,ij} + P_{ij} + G_{ij} + \varnothing_{ij} - F_{ij} - \varepsilon_{ij} + S_{user} \tag{3}
$$

where  $D_{T,ij}$  represents the diffusive transport term, which is calculated as:

$$
D_{T,ij} = -\frac{\partial}{\partial x_k} \left( \rho \overline{u'_i u'_j u'_k} + \overline{P' \left( \sigma_{jk} u'_k + \sigma_{ik} u'_j \right)} \right)
$$
(4)

 $\text{ion}(3)$  : (3) represents the molecular vise The term  $D_{L,ij}$  in Equation (3) represents the molecular viscous diffusion term, which  $\sum_{i=1}^{L}$ is given by:

$$
D_{L,ij} = \mu \frac{\partial}{\partial x_k} \overline{u'_i u'_j} \tag{5}
$$

Stress *Pij* is given by:

$$
P_{ij} = -\rho \left( \overline{u_i^{\prime} u_k^{\prime}} \frac{\partial u_j}{\partial x_k} + \overline{u_j^{\prime} u_k^{\prime}} \frac{\partial u_i}{\partial x_k} \right)
$$
(6)

The term *Gij* represents the buoyancy generation term:

$$
G_{ij} = -\rho \beta \left[ g_i(u_j \theta) + g_j(u_i \theta) \right]
$$
 (7)

The pressure strain correlation  $\varnothing_{ij}$  is given by:

$$
\varnothing_{ij} = \overline{P\left(\frac{\partial u'_i}{\partial x_j} + \frac{\partial u'_j}{\partial x_i}\right)}
$$
\n(8)

The system rotation generation term *Fij* is:

$$
F_{ij} = 2\rho\Omega_k \left( u'_j u'_j \varepsilon_{ikm} + u'_i u'_m \varepsilon_{jkm} \right) \tag{9}
$$

The dissipative  $\varepsilon_{ij}$  is:

$$
\varepsilon_{ij} = 2\mu \frac{\overline{\partial u_i'} \, \overline{\partial u_j'}}{\overline{\partial x_k} \, \overline{\partial x_k}})
$$
(10)

The near-wall velocity is calculated by [\[49\]](#page-17-0):

$$
\frac{UC_{\mu}^{1/4}k^{1/2}}{\tau_w/\rho} = \frac{1}{\kappa}\ln(Ey^*)
$$
\n(11)

$$
y^* = \frac{\rho C_\mu^{1/4} k^{1/2} y}{\mu} \tag{12}
$$

The relevant parameters can be seen in Refs. [\[44](#page-16-24)[,50\]](#page-17-1).

## 2.2.2. Discrete Phase Model

Due to the low concentration of particles in this simulation, the discrete phase model (DPM) is applied in the present simulation. Due to the small particle diameter and the pulsating velocity of the gas flow in all directions, this can have a direct effect on the particle motion. Considering the effect of gas turbulence and pulsation velocity on particle motion, the discrete random walk model was chosen to track the particles. The model equations used are summarized as follows:

Tee equations for mass and momentum conservation of the gas phase are given by:

$$
\frac{\partial (\rho_g \varepsilon_g)}{\partial t} + \nabla \cdot (\rho_g \varepsilon_g u_g) = 0 \tag{13}
$$

$$
\frac{\partial (\rho_g \varepsilon_g u_g)}{\partial t} + \nabla \cdot (\rho_g \varepsilon_g u_g u_g) = -\nabla P + \mu \varepsilon_g \nabla^2 u_g + \rho_g \varepsilon_g g - S \tag{14}
$$

$$
S = \frac{\sum F_D}{V} \tag{15}
$$

$$
m_p \frac{\vec{du}_p}{dt} = m_p \frac{\vec{u} - \vec{u}_p}{\tau_r} + m_p \frac{\vec{g}(\rho_p - \rho)}{\rho_p} + \vec{F}
$$
(16)

where *F* is the sum of the particle swaying forces acting inside the grid cell.  $m_p$  is the particle mass;  $\tau_r$  is the particle residence time, which is given by:

18

$$
\tau_r = \frac{\rho_p d_p^2}{18u} \frac{24}{C_d Re} \tag{17}
$$

### *2.3. Boundary Conditions*

The inlet gas is methane at room temperature and pressure. The velocity inlet of  $15 \text{ m/s}$  is employed. The hydraulic diameter and turbulence intensity at the inlet are calculated from Equations (18) and (19). erature and pressure. The velocity inlet of  $= 19$ .

$$
D_H = \frac{4 \times S}{C} \tag{18}
$$

$$
I = 0.16 \times \left(\frac{\rho_g D_H V_{in}}{\mu}\right)^{-0.125}
$$
(19)

where *S* is the flow cross-sectional area; *C* is the inlet wetted perimeter; *ρ<sup>g</sup>* is the inlet gas density;  $\mu$  is the inlet gas viscosity;  $D_H$  is the hydraulic diameter; and *I* is the turbulence intensity turbulence intensity. where  $\sigma$  is the now cross-sectional area, c is the first weited permitter,  $\rho_g$  is the first

The exit boundary condition is set to outflow and the inlet to velocity boundary condition. A no-slip boundary is employed on other boundaries. In the calculation, a steady-state simulation is used first, followed by transient simulation to obtain a stable flow field, thus, reducing the convergence difficulty and improving the accuracy. When performing the DPM iteration, the bottom of the cyclone is set to trap, and the other boundaries are set to reflect. The particles are liquid droplets with diameters ranging from  $0.1~10 \mu m$ .

### *2.4. Grid Independence Analysis*  $\sigma$  original cyclone separator is selected as an example. Different tested hexahedral tested hexahedral tested hexahedral control tested hexahedral tested hexahedral tested hexahedral tested hexahedral tested hexahedral z. H. Grud nuc penuence zinuiyois<br>Tantari are involved. Figure 3 dependence 3 depicts are involved. Figure 3 depicts and 1,880,000, and 1,880,00

The original cyclone separator is selected as an example. Different tested hexahedral<br>the variation in separator is selected as an example. Different tested hexahedral grid numbers (700,000, 1,100,000, 1,480,000, and 1,880,000) are involved. Figure [3](#page-5-0) depicts the gha numbers (100,000, 1,100,000, 1,100,000, and 1,000,000) are involved. Tigate 5 depicts are variation in separator efficiency with particle diameter under different mesh numbers. The maximum difference of collection efficiency in cyclone between 700,000 and 1,100,000 mesh numbers is near 20%. The maximum difference of collection efficiency between 1,100,000 and  $1,480,000$   $1,880,000$  mesh numbers is less than 5%. The grid number of  $1,100,000$  is employed here, which is enough to guarantee convincing results. This meshed model of the cyclone separator is indicated in Figure [4.](#page-6-0)

<span id="page-5-0"></span>

**Figure 3.** Grid independence verification. **Figure 3.** Grid independence verification.

<span id="page-6-0"></span>

**Figure 4.** Schematic diagraph of the mesh representation. **Figure 4.** Schematic diagraph of the mesh representation.  $\frac{1}{\sqrt{1-\frac{1$ 

## *2.5. Model Validation 2.5. Model Validation*

In order to verify the accuracy of the numerical method, the simulation results were comp[ar](#page-16-24)ed with the experimental data [44]. As shown in Figure 5, the pressure drop of the cyclone separator was compared at different inlet velocities. The simulation results are slightly larger than the experimental data overall. However, the overall error is not<br>significant, which validates the model employed in present study. significant, which validates the model employed in present study. significant, which validates the model employed in present study.

<span id="page-6-1"></span>

Figure 5. Comparison of the pressure drop for the experimental and simulation results.

#### separator under different divergent or convergent insertion pipes. It can be seen that the static pressure gradually decreases along the radial direction from the wall to the center. **3. Results and Discussion**

### $\mathcal{F}$  comparisons in the center of the center of the center of the cyclonesis because of the cyclonesis because  $\mathcal{F}$ **3. Results and Discussion**  *3.1. Pressure Drop Analysis*

Figure [6](#page-7-0) shows the static pressure distribution in the middle section of the cyclone *1.1. Pressure distribution in the middle section of the cyclone*<br>separator under different divergent or convergent insertion pipes. It can be seen that the continuously transformed into dynamic pressure. Figure 6 shows the static pressure distribution in the middle section of the cyclone static pressure gradually decreases along the radial direction from the wall to the center. Furthermore, a clear low-pressure area appears in the center of the cyclone. This is because Turnlermore, a clear low-pressure area appears in the center of the cyclone. This is because<br>the gas phase in the cyclone creates an accelerated vortex motion from the outer wall to the center. As the gas phase gradually approaches the center, its static pressure is continuously transformed into dynamic pressure.



<span id="page-7-0"></span>low-pressure area, and the radial pressure gradient is also the smallest.

**Figure 6.** Static pressure contours of cyclone separators with different divergent or convergent **Figure 6.** Static pressure contours of cyclone separators with different divergent or convergent insertion pipes. (a)  $L = 75$  mm  $\theta = -30^{\circ}$ ; (b)  $L = 0$  mm; (c)  $L = 75$  mm  $\theta = 60^{\circ}$ .

As can be seen from Figure [6,](#page-7-0) the presence of the divergent or convergent insertion pipes significantly affects the static pressure distribution. Compared with the original configuration, the overall pressure in the cyclone with the convergent insertion pipe of  $L = 75$  mm and  $\theta = -30^\circ$  is higher. The static pressure distribution is more symmetrical with the narrowest low-pressure zone in the center. The asymmetry of static pressure distribution is most obvious in the original configuration. In the cyclone separator with the divergent insertion pipe of  $L = 70$  mm and  $\theta = 60^\circ$ , the cyclone has the widest central low-pressure area, and the radial pressure gradient is also the smallest.

Figure [7](#page-8-0) shows the static pressure distribution of the cyclone separator at different divergent insertion pipe lengths for *θ* = −15◦ . Near the vortex finder, there is a low-pressure core area with the lowest pressure in the cyclone separator. As the length *L* increases, the static pressure in this area becomes smaller; The central low-pressure area within the cyclone is narrower, while the overall static pressure of the cyclone is greater.

Figure [8](#page-8-1) shows the static pressure distribution of the cyclone separator at different divergent insertion pipe lengths for  $\theta = 30^\circ$ . Near the vortex finder, there is a low-pressure core area with the lowest pressure in the cyclone separator. As the length *L* increases, the static pressure in this area also becomes smaller; The central low-pressure area within the cyclone is shortened. Near the outlet of the vortex finder, there also exists a low-pressure core area, which disappears at a greater length.

pipe length *L*, the larger the pressure drop of the cyclone separator. At  $\theta > 0^\circ$ , the presence Figure [9](#page-9-0) shows the pressure drop variation in the cyclone separator under different divergent or convergent insertion pipes. When the length *L* of the insertion pipes remains unchanged, the pressure drop of the cyclone separator gradually decreases with the increase in the angle *θ*. When  $θ = 30°$  and  $60°$ , the pressure drop of the cyclone separator is lower than that of the case without the insertion pipe. The pressure drop reduction for  $L = 25$  mm is not as obvious as that for *L* = 50 mm and 75 m. The pressure drop of the cyclone separator is significantly higher when  $\theta = -30^{\circ}$  and  $-15^{\circ}$ ; At the same angle  $\theta$ , the longer the insertion of the divergent insertion pipe will expand the intersection of the cylindrical region to the vortex finder. The longer the length, the larger the expanded area, which can effectively

reduce the pressure loss in this area. However, when the length  $L$  is too long, it will impede the downward rotational motion of the vortex in the cylindrical region and increase the flow resistance. Therefore, the pressure drop at  $L = 75$  mm is not significantly smaller than that at *L* = 50 mm; when  $\hat{L}$  = 75 mm and  $\theta$  = 60°, the pressure drop is reduced by 7.8%. On the contrary, when  $\theta < 0^\circ$ , the presence of the convergent insertion pipe increases the pressure loss from the cylindrical body to the vortex finder. The longer the length *L,* the smaller the intersection of the cylindrical region to the vortex finder, which leads to a greater pressure loss.  $\cos$ .

<span id="page-8-0"></span>

**Figure 7.** Static pressure distribution of the cyclone separator at different convergent insertion pipe lengths for  $\theta = -15^{\circ}$ . (**a**)  $L = 25$  mm; (**b**)  $L = 50$  mm; (**c**)  $L = 75$  mm.

<span id="page-8-1"></span>

**Figure 8.** Static pressure distribution of the cyclone separator at different divergent insertion pipe **Figure 8.** Static pressure distribution of the cyclone separator at different divergent insertion pipe lengths for  $\theta = 30^{\circ}$ . (a)  $L = 25$  mm; (b)  $L = 50$  mm; (c)  $L = 75$  mm.

<span id="page-9-0"></span>

**Figure 9.** Pressure drop as a function of tilt angle and length under different divergent or convergent **Figure 9.** Pressure drop as a function of tilt angle and length under different divergent or convergent insertion pipes. insertion pipes.

## *3.2. Axial Velocity*

Figure 10 shows the axial velocity distribution at the Y =  $-420$  mm and Y =  $-750$  mm axis arrangement can be seen in Figure 1. The [v](#page-2-0)ertical axis is the ratio of axial velocity to inlet velocity, and the horizontal axis is the ratio of the radial position and the cross-section radius. As can be seen from Figure 10, the axial velocity distribution presents the fiverted<br>*V*-shaped distribution. The maximum axial velocity is located at the center of the cyclone separator. As can be seen from Figure 10, [th](#page-10-0)e cyclone flows downward near the separator wall, while the fluid flows upward near the central part. The reason is that the two-phase nuid from the miet mio the separator, according to the now channer, to form a downward<br>cyclonic flow. When reaching the vertebra, the fluid generates acceleration due to the  $\overline{\text{c}}$  change in vertebral angle. The different densities of the components produce different acceleration, resulting in differences in speed, and the acceleration of the solid particles is greater. Finally, due to the negative pressure effect of the vortex, a negative pressure zone<br>is created in the control part of the separator, which quides the low density components upwards. Compared to the original configuration without insertion pipes, the maximum axial velocity is augmented with insertion pipes installed. The effect of the insertion pipe on the axial velocity distribution is mainly reflected in the central upward flow region.<br>The effect is relatively small for the suter downward flow region. A smaller angle of the insertion pipe leads to a larger central axial velocity, such as  $\theta = -30°$ ,  $-15°$ , and 30°. For the divergent insertion pipes, the maximum central axial velocity increases with increasing tilt angles and then decreases. When  $\theta = 60^\circ$ , the axial velocity tends to be relatively small.<br>As the inequiring singularity I in grosses, the impact on the suith relatively distribution is more obvious, which is reflected in not only the overall increase in axial velocity but also the more obvious asymmetry of axial velocity distribution. cross-sections of each cyclone separator, where Y is the Y-axis coordinate and the coordinate radius. As can be seen from Figure [10,](#page-10-0) the axial velocity distribution presents the inverted fluid from the inlet into the separator, according to the flow channel, to form a downward is created in the central part of the separator, which guides the low density components The effect is relatively small for the outer downward flow region. A smaller angle of the As the insertion pipe length *L* increases, the impact on the axial velocity distribution is

<span id="page-10-0"></span>

Figure 10. Axial velocity distributions under different divergent or convergent insertion pipes. (a)  $L = 25$  mm Y = -420 mm; (b)  $L = 25$  mm Y = -750 m; (c)  $L = 50$  mm Y = -420 mm; (d)  $L = 50$  mm m; (**e**) L = 75 mm Y = −420 mm; (**f**) L = 75 mm Y = −750 m. Y = −750 m; (**e**) *L* = 75 mm Y = −420 mm; (**f**) *L* = 75 mm Y = −750 m.

#### *3.3. Particle Separation* gravity of the particle, the greater the greater the corresponding centrifugal force. The particles are particles are particles are  $q$

Figure [11](#page-11-0) depicts the particle movement in the cyclone separator for different particle diameters for the original cyclone separator. At a particle diameter  $d_p = 0.1 \mu m$ , some particles escape from the vortex finder orifice, and the particles have a short residence time<br>The cyclone and eventually run of the cyclone and eventually run of the cyclone and eventually run out of the c inside the cyclone. However, at the particle diameter  $d_p = 10 \mu m$ , all particles reach the dust removal port, and the collection efficiency reaches 100%. After the particles enter the cyclone from the inlet, the particles are rotated inside the cyclone by centrifugal force under<br>motion. The motion of the cyclone by centrifugal force under the airflow and gravity. The larger the particle diameter  $d_p$  and the greater the gravity of the particle, the greater the corresponding centrifugal force. The particles are more likely to collide with the wall and fall to the bottom of the cyclone and be captured. Therefore,<br>insertion particles decreases with the number of the collision of the same particles decreases with the same p the collection efficiency increases with the increase in particle diameter. Small particles are carried by the airflow more easily as they are subject to less centrifugal force. They keep rotating with the airflow in the cyclone and eventually run out of the cyclone with the<br>indicates the particle resistance time can be particle resistance time can be particle resistance time can be airflow or are finally captured. The interaction forces between particles ensure that there are a few particles in the cyclone separator to form a long period of circular motion. more likely to collide with the wall and fall to the bottom of the cyclone and be captured.  $T_{\text{PICIS}}$  is the particle inovenient in the cyclone separator for unferti particle

the cyclone from the inlet, the inlet, the particles are rotated inside the cyclone by centrifugal force  $\alpha$ 

<span id="page-11-0"></span>

**Figure 11.** Particle movement in the cyclone separator under different particle diameters for the **Figure 11.** Particle movement in the cyclone separator under different particle diameters for the original configuration. (a)  $d_p = 0.1 \mu m$ ; (b)  $d_p = 1 \mu m$ ; (c)  $d_p = 10 \mu m$ .

Figures [12](#page-12-0) and [13](#page-12-1) depict the particle movement in the cyclone separator under different particle diameters for cyclone separators with convergent and divergent insertion pipes. The same phenomenon exists. The number of escaped particles decreases with the increasing particle diameters. Compared to the original cyclone separator, the divergent insertion pipe can significantly decrease the particle resistance time under the situations of small and large particle diameters. However, the particle resistance time can be always obviously reduced under the studied range of the particle diameters.

Figure [14](#page-13-0) shows the variation in separation efficiency with particle diameter under different insertion pipes. When the particle diameter  $d_p \geq 5$  µm, the difference in the collection efficiency between the different separator configurations is rather small. The influence of the insertion pipes on the collection efficiency is weakened. The collection efficiency is above 95%. At the insertion pipe length  $L = 25$  mm, the difference in the collection efficiency is relatively small due to the short insertion pipe. However, when *θ* = 60°, for particle diameter 1 μm ≤  $d_p$  ≤ 5 μm, the collection efficiency is significantly lower than in other situations. The larger the tilt angle, the larger the area of the lower side of the vortex finder, which augments the possibility of particle escape. For divergent insertion pipes of  $L = 50$  mm and 75 mm, the collection efficiency is lowered when  $\theta = 30^\circ$ and  $\theta = 60^\circ$  due to the enlarged area of the lower side of the vortex finder. It is worth

noting that under the divergent insertion pipes with *L* = 25 mm and *L* = 50 mm, the lowest collection efficiency occurs at  $\theta = 60^{\circ}$ , while when  $L = 75$  mm, the lowest collection efficiency occurs at  $\theta = 30^\circ$ . For divergent insertion pipes ( $\theta < 0^\circ$ ), the collection efficiency of the cyclone separator can be improved, especially under small diameter particles. The collection efficiency increases with increasing length and tilt angles. The most obvious collection efficiency improvement is achieved when  $L = 75$  mm and  $\theta = -30^\circ$ , where the area of the lower side of the vortex finder is the smallest. In terms of collection efficiency and pressure drop, for small particles  $d_p \leq 5 \mu m$ , a convergent insertion pipe of  $L = 75 \text{ mm}$  and  $\theta = -30^{\circ}$  exhibits better separation performance. When the particle diameter  $d_p \ge 5$   $\mu$ m, the divergent insertion pipes with larger angles and lengths can significantly decrease the pressure drop while guaranteeing satisfied collection efficiency.

<span id="page-12-0"></span>

<span id="page-12-1"></span>Figure 12. Particle movement in the cyclone separator under different particle diameters for the convergent insertion pipe of  $L = 70$  mm  $\theta = -30^\circ$ . (a)  $d_p = 0.1$   $\mu$ m; (b)  $d_p = 1$   $\mu$ m; (c)  $d_p = 10$   $\mu$ m.



Figure 13. Particle movement in the cyclone separator under different particle diameters for the **EXECUTE 13. Figure 13. Figure 13. Figure 13. Figure 3. Figure 3. Particle different particle** divergent insertion pipe of  $L = 70$  mm  $\theta = 30^\circ$ . (a)  $d_p = 0.1$  µm; (b)  $d_p = 1$  µm; (c)  $d_p = 10$  µm.

<span id="page-13-0"></span>

**Figure 14.** The variation in collection efficiency with particle diameters under different divergent or convergent insertion pipes. (a)  $L = 25$  mm. (b)  $L = 50$  mm. (c)  $L = 75$  mm. convergent insertion pipes. (**a**)  $L = 25$  mm. (**b**)  $L = 50$  mm. (**c**)  $L = 75$  mm.

## **4. Conclusions**

In this study, different divergent or convergent insertion pipes below the vortex finder were constructed to improve separator performance. The impacts of different divergent or convergent insertion pipes were systematically analyzed. The following conclusions were obtained.

- 1. The insertion pipe can obviously affect the inside static pressure distribution inside. A longer insertion pipe length and larger tilt angle lead to wider central low-pressure areas and a smaller overall static pressure.
- 2. The installed convergent insertion pipe increases the pressure loss, while the installed divergent insertion pipe augments the pressure loss. When  $L = 75$  mm and  $\theta = 60^{\circ}$ , the pressure drop is reduced by 7.8%.
- 3. With the insertion pipe installed, the maximum axial velocity is enhanced. A larger insertion pipe length contributes to the impact on the axial velocity distribution. For the divergent insertion pipes, the maximum central axial velocity increases with increasing tilt angles and then decreases.
- 4. For small particles  $d$ <sup>*p*</sup> ≤ 5 μm, a convergent insertion pipe of *L* = 75 mm and  $θ$  = −30° exhibits a better separation performance. When the particle diameter  $d_p \geq 5 \mu m$ , the divergent insertion pipes with larger angles and lengths can significantly decrease the pressure drop while guaranteeing satisfied collection efficiency.

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## **Nomenclature**





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