

## Supplementary Materials

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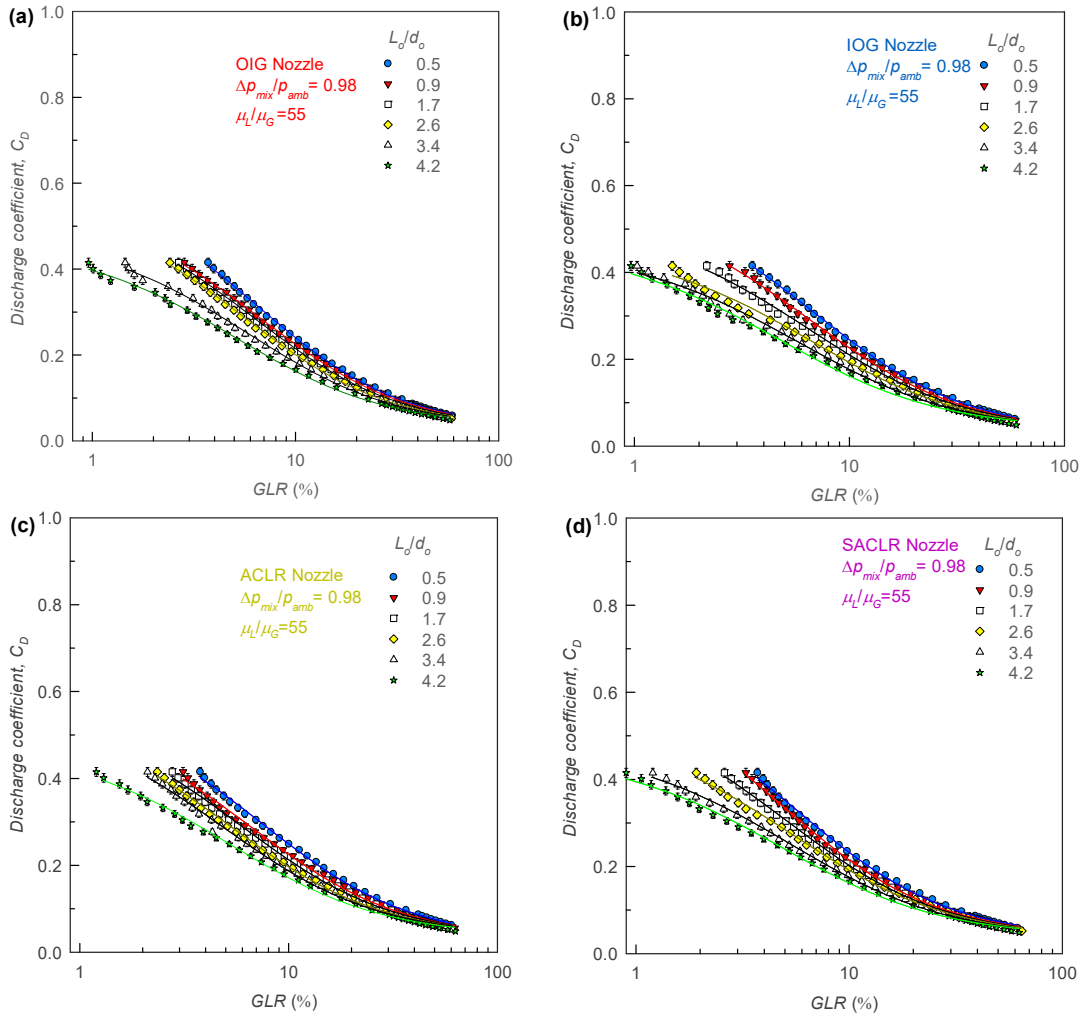
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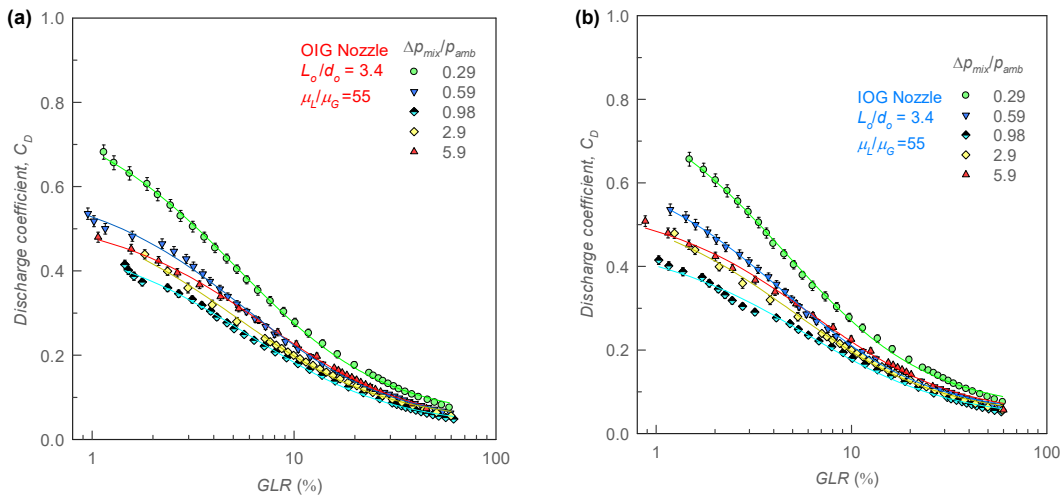
**Table S1:** A sample of operational conditions

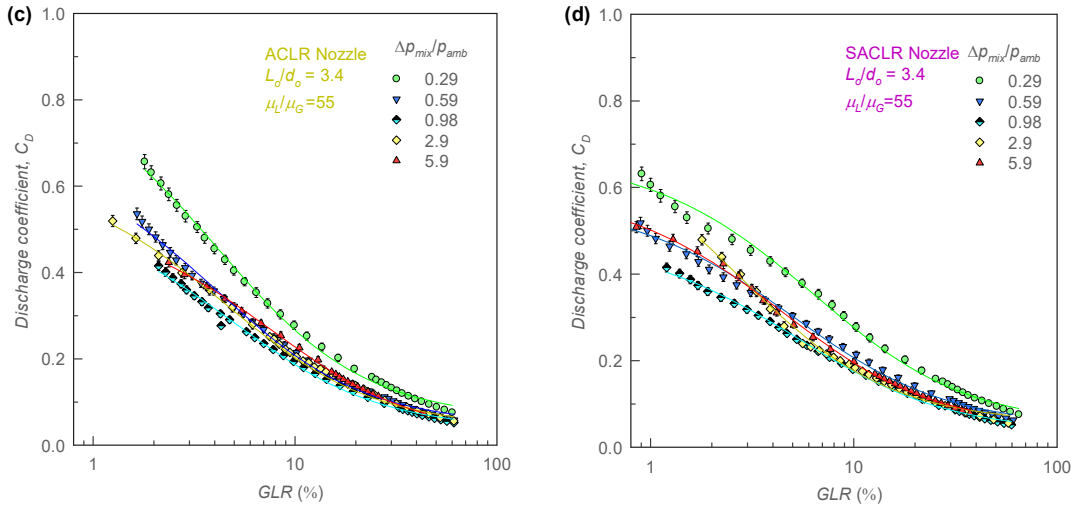
$\dot{m}_L$ (kg/h)	$u_r(\dot{m}_L)$ (%)	$\dot{m}_G$ (kg/h)	$u_r(\dot{m}_G)$ (%)	GLR (%)	$u_r$ (GLR) (%)
19.97	2.5	0.207	9.2	1.0	9.6
17.97	3.3	0.264	7.2	1.5	7.9
15.97	3.4	0.327	5.8	2.0	6.8
13.98	3.7	0.436	4.4	3.1	5.7
11.98	2.5	0.452	4.2	3.8	4.9
11.58	2.5	0.459	4.2	4.0	4.9
11.18	2.5	0.477	4.0	4.3	4.7
10.78	2.5	0.487	3.9	4.5	4.7
10.38	2.5	0.507	3.8	4.9	4.5
9.98	2.5	0.523	3.7	5.2	4.4
9.58	2.5	0.549	3.5	5.7	4.3
9.18	2.5	0.568	3.4	6.2	4.2
8.78	2.5	0.614	3.1	7.0	4.0
8.39	2.5	0.633	3.0	7.5	3.9
7.99	2.5	0.656	2.9	8.2	3.8
7.59	2.5	0.687	2.8	9.1	3.7
7.19	2.5	0.720	2.7	10.0	3.6
6.79	2.5	0.763	2.5	11.2	3.5
6.39	2.5	0.784	2.4	12.3	3.5
5.99	2.5	0.812	2.4	13.6	3.4
5.59	3.2	0.826	2.3	14.8	4.0
5.19	3.3	0.851	2.2	16.4	4.0
4.79	3.4	0.879	2.2	18.4	4.1
4.39	3.6	0.901	2.1	20.5	4.2
3.99	3.8	0.928	2.1	23.3	4.3
3.59	4.0	0.952	2.0	26.5	4.4
3.19	4.2	0.981	1.9	30.8	4.6
2.80	4.6	1.021	1.9	36.5	4.9
2.50	2.5	1.043	1.8	41.7	3.1
2.40	2.5	1.045	1.8	43.5	3.1
2.30	2.5	1.053	1.8	45.8	3.1
2.20	2.5	1.056	1.8	48.0	3.1
2.10	2.5	1.062	1.8	50.6	3.1
2.00	2.5	1.069	1.8	53.5	3.1
1.90	2.5	1.075	1.8	56.6	3.1
1.80	2.5	1.082	1.8	60.1	3.1
1.70	2.5	1.089	1.8	64.1	3.1

$\mu_r$  is the relative uncertainty.

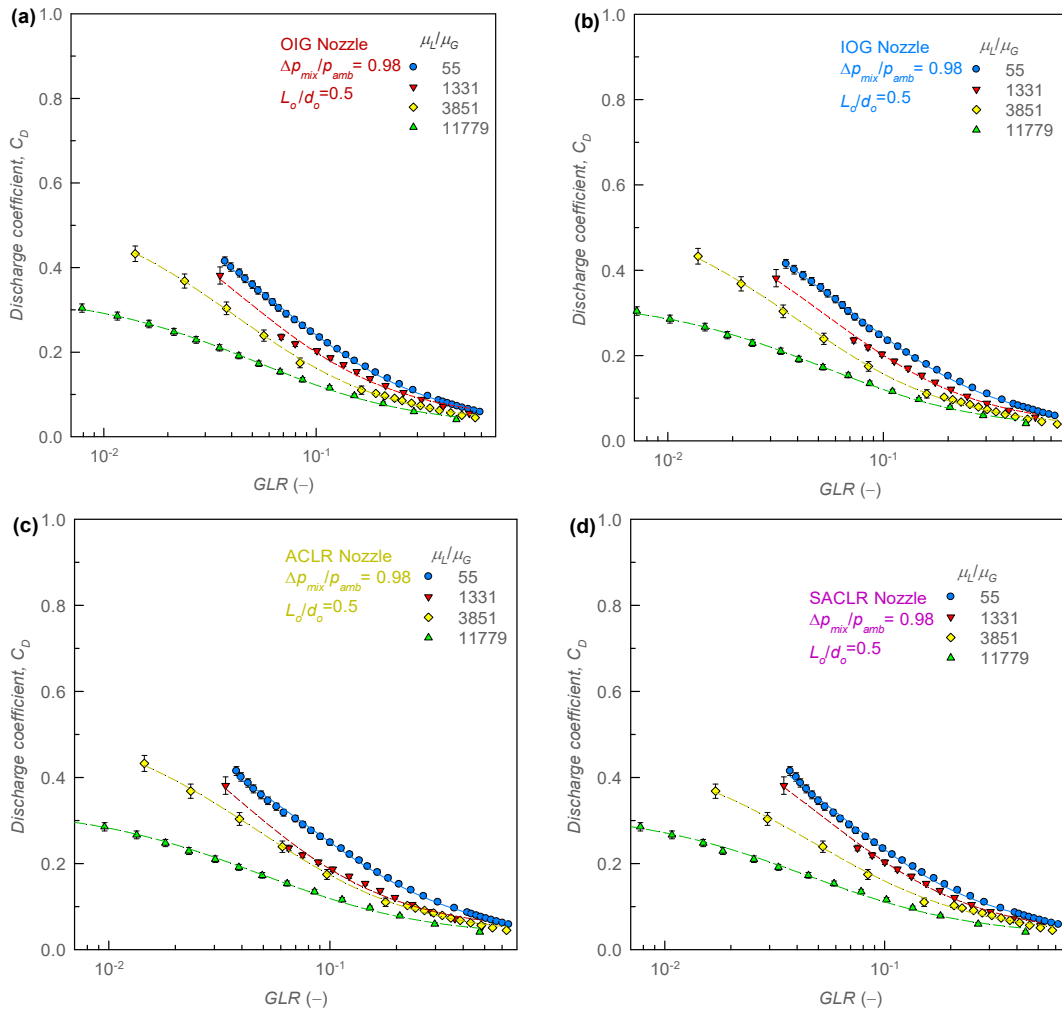


**Figure S1.** Effect of GLR on  $C_D$  at different  $L_o/d_o$  for different nozzles: (a) OIG; (b) IOG; (c) ACLR; and (d) SACLR.

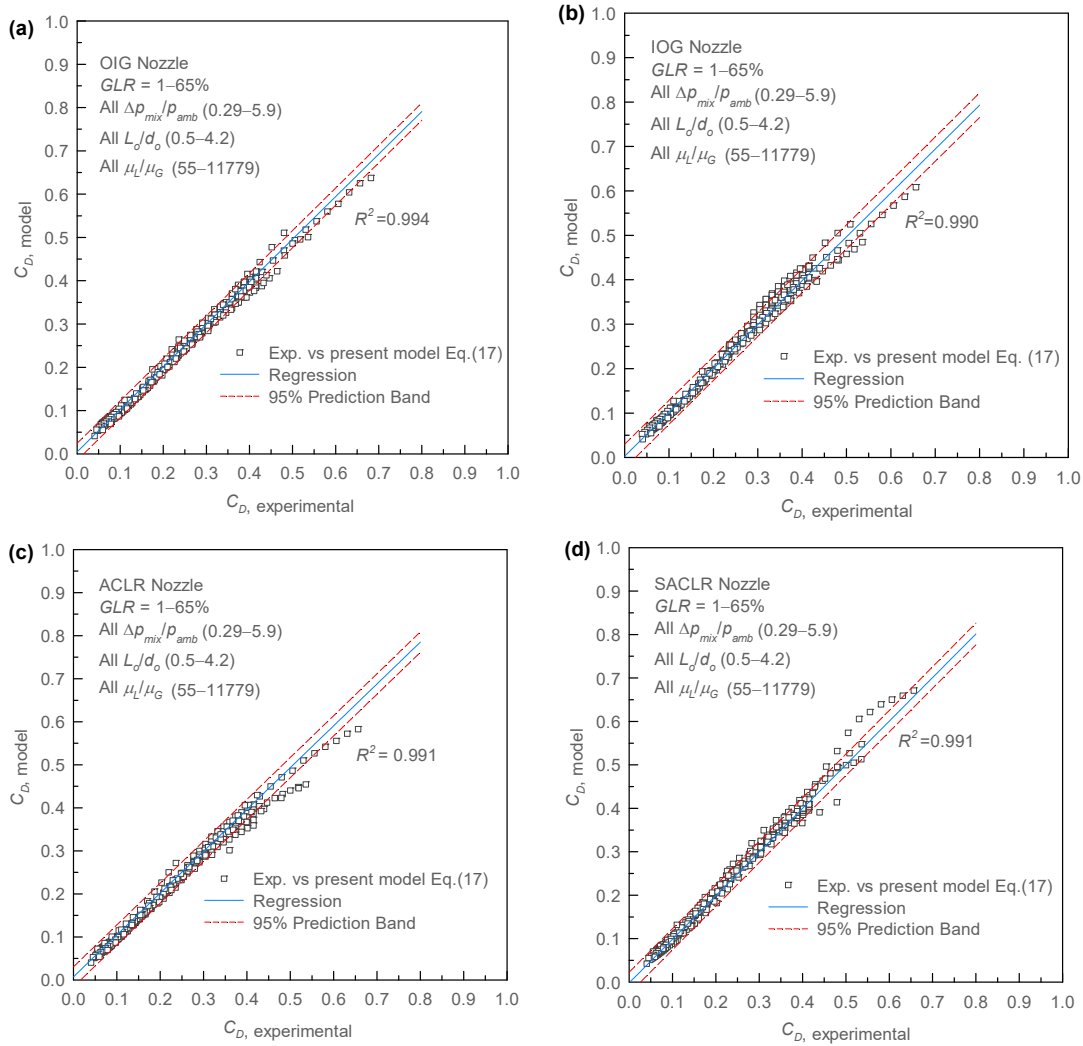




**Figure S2.** Effect of GLR on  $C_D$  at different  $\Delta p_{mix}/p_{amb}$  for different nozzles: (a) OIG; (b) IOG; (c) ACLR; and (d) SACL.



**Figure S3.** Effect of GLR on  $C_D$  at varying  $\mu_l/\mu_g$  for different nozzles: (a) OIG; (b) IOG; (c) ACLR; and (d) SACL.



**Figure S4.** Comparison of the experimental and predicted  $C_D$  from the present model Eq. (17) for different nozzles: (a) OIG, (b) IOG, (c) ACLR, and (d) SACL R

