

Communication **High-Efficiency Grating Couplers for Pixel-Level Flat-Top Beam Generation**

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Abstract: We demonstrate a kind of grating coupler that generates a high quality flat-top beam with a small beamwidth from photonic integrated circuits into free-space. The grating coupler is designed on a silicon-on-insulator wafer with a 220-nm-thick silicon layer and consists of a dual-etch grating (DG) and a distributed Bragg reflector (DBR). By adjusting the structural parameters of DG and DBR, a pixel-level (6.6 µm) flat-top beam with a vertical radiation of −0.5 dB and a mode match of 97% at 1550 nm is realized. Furthermore, a series of high-efficiency grating couplers are designed to create a flat-top beam with different scales.

Keywords: grating coupler; dual-etch grating; distributed Bragg reflector; flat-top beam

1. Introduction

Grating couplers are widely used in optical communication and sensing systems [\[1](#page-7-0)[–9\]](#page-7-1). By converting the waveguide mode to the radiation mode, grating couplers have demonstrated a tremendous ability to couple the guided light into free space [\[10](#page-7-2)[–13\]](#page-7-3). So far, several structures for high-efficiency fiber-chip coupling have been demonstrated, including an overlay structure [\[14](#page-7-4)[,15\]](#page-8-0), a Bragg or metallic mirror substrate [\[16](#page-8-1)[–18\]](#page-8-2), a slanted tilted waveguide [\[19,](#page-8-3)[20\]](#page-8-4), an asymmetry waveguide [\[21](#page-8-5)[–23\]](#page-8-6) or an apodized grating [\[24](#page-8-7)[,25\]](#page-8-8). For example, by adding a poly-silicon layer deposition prior to grating etching, a highly efficient grating coupler can be obtained [\[14\]](#page-7-4). To reduce the transmission light and enhance optical coupling, a compact grating coupler combined with a reflector grating are proposed [\[26\]](#page-8-9). For the perfectly vertical coupling, a high efficiency two-layer vertical silicon grating coupler is optimized with the adjoint method and achieved a chip-to-fiber coupling efficiency of −0.035 dB at 1550 nm [\[21\]](#page-8-5). With the apodization technology, the grating coupler is designed to be apodized by varying the coupling strength for each grating period and a Gaussian intensity profile can be efficiently generated at the interface of grating [\[25\]](#page-8-8). On the other hand, highly efficient grating couplers have also been demonstrated with dual-etch structures [\[27–](#page-8-10)[30\]](#page-8-11). Recently, a coupler design consisting of a two etch-step blazed and silicon nanopillars structure has been proposed to obtain a high efficiency and a low back reflection [\[31\]](#page-8-12). In addition, subwavelength grating metamaterial engineering has also been successfully adopted to reduce index mismatch at structural transitions and improve coupling efficiency [\[32](#page-8-13)[–36\]](#page-8-14). More recently, a silicon-based surface grating antenna design with a coupling efficiency of −0.5 dB and a directionality higher than 94% has been predicted by utilizing subwavelength-based L-shaped radiating elements in a 300-nm silicon core [\[37\]](#page-8-15).

Most of the aforementioned grating couplers have been designed to efficiently generate the Gaussian intensity profile whose mode field diameter is around 10 μ m [\[38\]](#page-8-16). This is suitable for certain applications such as fiber-chip coupling. For applications in the fluorescence imaging [\[39\]](#page-8-17), optical phased arrays [\[40,](#page-8-18)[41\]](#page-9-0) and microscopy systems [\[42\]](#page-9-1), a smaller grating coupler is desirable. There are some works on compact on-chip couplers [\[42](#page-9-1)[–46\]](#page-9-2).

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For instance, a coupler design has been used as a component to couple light from a photonic chip waveguide to a microscopy system, focusing on applications of quantumoptics and bio-optics experiments [\[42\]](#page-9-1). Besides, for imaging applications, a pixel-level flat-top beam can provide a detailed analysis, increase the resolution and ensure more benefits [\[39,](#page-8-17)[42\]](#page-9-1). Particularly, in fluorescence nanoscopy, the non-uniform illumination leads to position-dependent resolution and limits the field-of-view, which is harmful in high-quality super-resolution imaging [\[47\]](#page-9-3). On the other hand, for photodetectors, a smaller grating coupler can provide a compact waveguide integration scheme [\[48](#page-9-4)[,49\]](#page-9-5), and a flat-top beam with uniform intensity can alleviate the space charge effect [\[50\]](#page-9-6). Hence, there is a need for compact and efficient couplers which can generate small flat-top beams.

In this article, we present a silicon grating coupler that can transform the waveguide mode into the pixel-level flat-top mode. This is achieved by exploiting a highly directional dual-etch grating (DG) and a distributed Bragg grating (DBR) on a 220-nm-thick silicon-oninsulator platform. The DG provides high diffraction efficiency and low back reflection, and the DBR effectively increases the coupling length to enhance diffraction. The DBR can not only help to maintain high efficiency under a compact coupling length, but also improve the uniformity of radiation fields. By optimizing DG and DBR, the desired flat-top intensity and uniform wavefront in the orthogonal direction can be achieved. The grating coupler generates a pixel-level $(6.6 \mu m)$ flat-top beam and shows the vertical radiation of −0.5 dB and the mode match of 97%. Lastly, we demonstrate that this design is effective for grating couplers with various coupling lengths. This paper is organized as follows. The design concept and methodology of the proposed grating coupler are described in Section [2.](#page-1-0) The simulation results are presented in Section [3,](#page-2-0) the fabrication tolerance is analyzed in Section [4,](#page-5-0) the grating couplers with different lengths are discussed in Section [5,](#page-6-0) and the conclusions are summarized in Section [6.](#page-7-5)

2. Design Concept and Methodology

In this section, we first explain the design principles of each part of the grating coupler, including DG, DBR and the connecting waveguide. Then we specifically analyze the reason that DG can achieve high efficiency. The grating coupler comprises a DG, and a DBR in an SOI platform with a 220-nm-thick waveguide, 2 -µm buried oxide and 2 -µm silica cladding (Figure [1a](#page-2-1)). The DG implements an L-shaped structure with a shallow etch of 70 nm. Compared to the single-etch grating, DG enhances the diffraction strength due to its blazing effect [\[51\]](#page-9-7). In addition, the subwavelength pillars in DG provide the anti-reflection effect and reduce the back reflection [\[52\]](#page-9-8), resulting in a high diffraction efficiency in the upward direction. The DBR redirects the forward transmission light and makes it pass through the DG twice. Therefore, the length of the grating coupler can be reduced while maintaining a high efficiency. The DBR also helps to reshape the radiation mode to match the flat-top mode. Without the DBR, the uniform DG will have exponentially decaying light fields along the in-plane propagation direction. Compared with the flat-top mode, its optical intensity at the beginning of the DG is too strong and, at the end, is too weak. The DBR can reflect the forward transmission light back and compensate for the weak part of light. Thus, the diffraction fields can be reshaped to match the flat-top mode profile. Lastly, a silicon waveguide connects the DG and DBR, and its length has a strong impact on efficiency. Through the careful design of DG, DBR and the connecting waveguide, this grating coupler can effectively obtain the pixel-level flat-top beam. In the following text, we will demonstrate the design principles and procedure of the grating coupler in detail. Throughout this work, we utilize a particle swarm optimization algorithm and 2D finite-difference time-domain simulations.

The unit cell of DG has two grooves with different etching depths, i.e., shallowly etched and fully etched units (right upper inset of Figure [1a](#page-2-1)). The theoretical model of DG has been discussed in previous studies [\[53\]](#page-9-9), and we briefly summarize its design principle. Light propagating from left to right within the waveguide will encounter shallowly or fully etched grooves which act as a phased array of scatterers and couple light out of

the plane efficiently. As shown in Figure [1c](#page-2-1), assuming that light is emitted from the center of the sidewall of the groove [\[54\]](#page-9-10), the phase difference between light propagating from the fully etched grating and the shallowly etched grating can be decomposed into a vertical phase difference and a lateral phase difference. When the vertical and lateral phase differences accumulate $π/2$ phase shifts, respectively, constructive interference in the upward direction and destructive interference in the downward direction can be realized, and then unidirectional radiation can be achieved.

Figure 1. (**a**) Schematic of the grating coupler consisting of DG and DBR. The DG utilizes a blazed subwavelength structure with period and optimization variables $[d_1, d_2, d_3, d_4, d_5]$. The period length of the DBR is Λ*r*. (**b**) Description of the operation of the grating coupler. Light is incident from the left waveguide and has four output channels, i.e., the channel along the vertical radiation, back reflection, bottom leakage and forward transmission. (**c**) Description of the operation principle of DG.

3. Results and Discussion

In this section, we design and investigate a grating coupler, which consists of a 10 periods DG, a DBR and a connecting waveguide. Firstly, the DG is optimized to achieve the highest vertical radiation at the wavelength of 1550 nm. As shown in Figure [1b](#page-2-1), the light incident to DG has four possible output channels, namely vertical radiation, back reflection, bottom leakage and forward transmission. The vertical radiation is defined as Γ *= Pvertical/Pinput*, where *Pvertical* is the vertically radiated power and *Pinput* is the incident power. In the simulation, a waveguide mode with transverse electric polarization is incident from the left. The structural parameters of d_1 , d_2 , d_3 , d_4 , and d_5 are optimized using the particle swarm algorithm which has been widely used in various optical designs such as gratings [\[31\]](#page-8-12), lens [\[55\]](#page-9-11), nanophotonic structures [\[56\]](#page-9-12). The detailed algorithm implementation can refer to article [\[57\]](#page-9-13). We assume that the DG is covered by $SiO₂$ as a top-cladding layer and the refractive indices of Si and $SiO₂$ are 3.48 and 1.44, respectively. The obtained optimal structural parameters are: $d_1 = 92$ nm, $d_2 = 84$ nm, $d_3 = 252$ nm, d_4 = 133 nm and d_5 = 99 nm. The total length of DG with 10 periods is 6.6 μ m.

The above DG enhances the vertical radiation and suppresses the bottom leakage. This is useful for improving the efficiency. However, when reducing the dimension of DG, the light cannot be radiated out-of-plane at one time and there will be a lot of forward transmission light. To correct this issue, we adopt the compensation effect of the DBR. The

DBR is designed based on the Bragg condition of $\beta_m = \beta + mG$, where β_m represents the *m*th diffraction wave vector, *β* is the incident light wave vector, and *mG* is the wave vector introduced by the grating (Figure [2a](#page-3-0)). The DBR uses the negative first-order diffraction (i.e., *m* = −1) to reflect the forward transmission light. Therefore, in this case, the Bragg condition can be written as:

$$
n_{core}\Lambda_r ff + n_{clad}\Lambda_r (1 - ff) = \frac{\lambda}{2},\tag{1}
$$

where *n_{core}* and *n_{clad}* are the effective refractive indices of Si core and SiO₂ cladding, Λ_{*r*} is the period length of reflection grating, *ff* is the fill factor (*ff* = 0.5) and λ is the center wavelength $(\lambda = 1550 \text{ nm})$. By substituting these values into the Bragg condition, the period length is calculated to be around 322 nm. To accurately find the parameters corresponding to the highest reflectivity, we simulate the DBR with a period length from 200 nm to 500 nm. In the simulation, both the wavelength interval and the period length interval are 1 nm. The results are shown in Figure [2b](#page-3-0). We selected the period length to be 311 nm to achieve high reflectivity in a wide spectral range. Then, the designed DBR is placed after the DG to form a grating coupler. To see the compensation effect of DBR, we compare the forward transmission light and vertical radiation of the grating coupler with and without DBR (Figure [2c](#page-3-0),d). The forward transmission is greatly suppressed since it drops from about −5 dB to about −30 dB. As a result, the vertical radiation is enhanced near 1550 nm.

Figure 2. (**a**) Wave-vector diagram of the DBR which uses the negative first-order diffraction to reflect the forward transmission light. (**b**) Reflectivity phase diagram of the DBR whose fill factor is 0.5. (**c**,**d**) Comparison of the forward transmission and vertical radiation for structures without and with DBR.

Note that the spacing between DG and DBR is another important parameter because it significantly affects the coupling efficiency. Figure [3](#page-4-0) plots the vertical radiation, back reflection and bottom leakage as a function of the connecting waveguide width *W^d* . They change periodically with the increase in *W^d* . At some points with the highest vertical radiation, the back reflection and the bottom leakage are suppressed. In our paper, the connecting waveguide length is chosen to be W_d = 90 nm. In this case, the light reflected by the DBR destructively interferes with the light reflected by the DG. Similarly, destructive

interference occurs by emitting bottom-coupled light from the left and another emitting bottom-coupled light reflected by the DBR and from the right.

Figure 3. Vertical radiation (red), back reflection (blue) and bottom leakage (green) as a function of the connecting waveguide width.

Overall, a high efficiency grating coupler is obtained by carefully selecting the structural parameters of DG, DBR and the connecting waveguide. The simulated electric fields of the optimized grating coupler are shown in Figure [4a](#page-5-1). Most of the light is vertically coupled along the +y direction, and electric fields in other directions are weak, indicating that the unwanted diffraction loss is suppressed. In our optimized structure, the vertical radiation reaches −0.5 dB. Besides the diffraction efficiency, we also analyze the mode matching capability of the grating coupler. To do this, the *Ez* slices of the optimized beam are shown in Figure [4b](#page-5-1),c. Obviously, both the amplitude and phase of the simulated electric field are close to the flat-top contour of the design target over most of the width of the beam, only slightly offset near the edge of the beam. This offset does not lead to a significant reduction in mode match. To quantitatively measure the mode match between simulation and target flat-top mode, we define a mode match coefficient based on the overlap integral [\[3\]](#page-7-6):

$$
\eta = \left| \frac{\int (E_s(x) \cdot E_t^*(x))^2 dx}{\int E_s^2(x) dx \cdot \int E_t^2(x) dx} \right|.
$$
 (2)

Here, $E_s(x)$ and $E_t(x)$ respectively correspond to the electric fields of the simulation wave and target mode (represented by the super Gaussian function $E_t(x) = \exp\left(-(x/w)^N\right)$, where *w* is the half-maximum beam width and $N = 24$). Ideally, the out-coupled mode should exhibit a maximum overlap with the flat-top mode, i.e., *η* = 100%. In our optimized structure, the mode match exceeds 97% at the wavelength of 1550 nm and is close to the ideal result. Besides, the mode match is larger than 80% (i.e., 1 dB) in the whole C band, and shows broad spectral characteristics (Figure [4d](#page-5-1)). Moreover, the far-field radiations of light with different wavelengths are calculated to see the diffraction directionality (Figure [4e](#page-5-1)). The designed grating coupler can keep vertical diffraction well at 1550 nm. The radiation angle wavelength shift is 0.11◦/nm over 1500–1600 nm.

Figure 4. Performance of the grating coupler with a 10 periods DG and a DBR (**a**) The real part of *Ez* shows the simulated radiation with the high vertical radiation and flat wavefront. (**b**,**c**) Comparison between the simulated (**b**) amplitude and (**c**) phase of *Ez* for the optimized grating coupler and the target flat-top wavefront. (**d**) The mode match results of the designed structure. (**e**) The far-field radiation performance of the optimized grating coupler.

4. Fabrication Tolerance Analysis

The experimental realization of the above grating coupler is feasible. The proposed structure relies on a simple double etching process and is compatible with standard siliconon-insulator technology. Its minimum feature size is larger than 80 nm, which ensures a convenient platform for further fabrication. These results are promising for current and future applications, especially considering that this structure has been fabricated using the existing CMOS process [\[31\]](#page-8-12). Since there might be fabrication errors in the grating width, the thickness of the shallowly etched area, and the connecting waveguide length during the fabrication, vertical radiation and mode match are calculated for cases where fabrication errors happen. Here, the errors of the grating width caused by the full etching and the shallow etching are assumed to be ∆*d^F* and ∆*dS*, while the errors of the length of the connecting waveguide and the shallowly etched depth are defined as ∆*d^L* and Δd_T , respectively. Thus, these fabrication errors are expressed by: $d_1 = d_{1,0} + \Delta d_F$, $d_2 = d_{2,0} - \Delta d_F$, $d_3 = d_{3,0} + \Delta d_F/2 - \Delta d_S/2$, $d_4 = d_{4,0} + \Delta d_F/2 + \Delta d_S/2$, $d_5 = d_{5,0} - \Delta d_F$, $d_L = d_{L,0} - \Delta d_L$, $d_T = d_{T,0} - \Delta d_T$, where parameters with subscript "0" represent the ideal values. As shown in Figure [5a](#page-6-1), vertical radiation and mode match show relatively large fluctuations as the width changes. The performance of the grating coupler is more affected by the fully etched area. Furthermore, the performance variations remain comparatively small for the fabrication error of shallowly etched area (Figure [5b](#page-6-1)). We also consider the impact that a variation in the waveguide length could have on the grating performance. This variability is much smaller than the fabrication variations related to the lithography. Figure [5c](#page-6-1) shows that the performance of the grating coupler is slightly affected within the selected range of waveguide length variations. Figure [5d](#page-6-1) shows the calculation result of the change in vertical radiation and mode match with respect to the depth of the shallowly etched area. The vertical radiation of >3 dB and mode match of >80% can be maintained for deviations of \lt \pm 15 nm.

Figure 5. Fabrication tolerances of the vertical radiation and mode match. (**a**) Width error caused by full etching process. (**b**) Width error caused by shallow etching process. (**c**) Length error of connecting waveguide. (**d**) Depth error caused by shallow etching process.

5. Grating Couplers with Different Lengths

In the above, we have designed a grating coupler with a pixel level of 6.6 μ m. In this section, we verify that this design method can be applied to grating couplers with other pixel-level lengths. In Figure [6a](#page-6-2), we calculate the vertical radiation and mode match of DG with 1 to 21 periods and all other structural parameters are the same as those in Figure [4.](#page-5-1) The vertical radiation and mode match are high for when the number of periods is larger than 6, but the vertical radiation is low when the number of periods is smaller than 6. For example, the *E^z* slice of output modes of DG with three periods shows that although most of the light is radiated upward, the electric fields at the bottom are also strong. This indicates that there exists a high bottom leakage and DG with small periods should be further modified to achieve high vertical radiation. Therefore, we use the particle swarm algorithm to find the optimal structural parameters of DGs with one to six periods. The optimized DGs yield a grating coupler with a higher vertical radiation than that of the unoptimized one (Figure [6b](#page-6-2)). Meanwhile, the mode match of the optimized grating coupler remained almost unchanged (~95%).

Figure 6. Performance of DGs with different numbers of periods. (**a**) The vertical radiation is deteriorated in DGs with small periods. The inset shows the real part of *Ez* of the DG with 3 periods. Here, structural parameters except the number of periods of DG are the same as those in Figure [4.](#page-5-1) (**b**) The optimal performance of DGs (solid line) with 1 to 6 periods whose structural parameters are found by using the particle swarm algorithm to ensure low diffraction loss.

6. Conclusions

In conclusion, a grating coupler that efficiently couples a fundamental mode of silicon waveguide to a pixel-level flat-top beam in free space is designed and numerically demonstrated. Several different pixel-level grating couplers are verified as well. Specifically, the DG offers a high-efficiency diffraction and the followed DBR provides a compensation effect and makes sure to reduce the circuit footprint. Meanwhile, the flat-top beam is achieved by optimizing the structural parameters of the grating coupler. The vertical radiation of the grating coupler is above −0.5 dB, and its mode match is up to 97%. This kind of grating coupler can be a module for the interaction of the photonic chip with other systems, such as biosensing, high-precision image sensors, structured light illumination and so on.

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