



*sp*² Carbon Stable Radicals

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Abstract: sp^2 Nanocarbons such as fullerenes, carbon nanotubes, and graphene molecules are not only open-shell species, but spatially extended, due to which their chemistry is quite specific. Cogently revealed dependence of the final products composition on size and shape of the carbons in use as well as on the chemical prehistory is accumulated in a particular property—the stabilization of the species' radical efficiency, thus providing the matter of stable radicals. If the feature is highly restricted and rarely available in ordinary chemistry, in the case of sp^2 nanocarbons it is just an ordinary event providing, say, tons-in-mass stable radicals when either producing such widely used technological products as carbon black or dealing with deposits of natural sp^2 carbons such as anthracite, shungite carbon, and other. Suggested in the paper is the consideration of stable radicals of sp^2 nanocarbons from the standpoint of spin-delocalized topochemistry. Characterized in terms of the total and atomically partitioned number of effectively unpaired electrons as well as of the distribution of the latter over carbon atoms and described by selectively determined barriers of different reactions exhibiting topological essence of intermolecular interaction, sp^2 nanocarbons reveal a peculiar topokinetics that lays the foundation of the stability of their radical properties.

Keywords: stable radicals; fullerenes; carbon nanotubes; graphene molecules; spin chemistry; topokinetics



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1. Introduction

Generally, radicals are objects of the spin chemistry of open-shell molecules. The total pool of molecular spins consists of N_{α} and N_{β} elements, oriented up and down, respectively, and the difference $N_{\alpha} - N_{\beta}$ formally determines spin multiplicity (*SpM*) of the molecule ground state. Predominant majority of α and β spins of the molecule inner shells form pairs, both components of which are located in the same space, thus subordinating to the Pauli principle and forming closed-shell spin-orbitals. A part of α and β spins of electrons of outer shells are located in different space, thus forming open-shell spin-orbitals, the same are the relevant molecules. Historically, radical open-shell molecules were attributed to the atomic systems with *SpM* higher than singlet. However, the open-shell concept is much broader and concerns a much bigger number of the molecule electrons, due to which the spin multiplicity is not the main characteristic of the state and does not exclude the open-shell status of singlet molecule as well. Thus, starting investigation of any new class of molecules, one has to answer two main questions: (i) Are the molecules under study of a closed-shell or open-shell type and (ii) what are the characteristic parameters of the molecule that describe its radical essence. The current paper suggests answers to these questions, related to a family of sp^2 nanocarbons. The paper is composed in the following way. A concise historical overview, concerning the spin chemistry of radicals in general, is given in Section 2. Grounds of UHF computational spin chemistry of sp^2 nanocarbons are discussed in Section 3. Sections 4-6 are devoted, respectively, to spin traits of openshell molecules of sp^2 nanocarbons, electron spins in intermolecular interaction, and the spin nature of the reaction final products, whose post-reaction existence is considered in Section 7. The conclusion summarizes the essences discussed.

2. A Historical Excurse in the Virtual Spin Chemistry of Radicals

The history of quantum-chemical consideration of open-shell molecules is quite long. It originates more than 65 years ago from the paper of Pople and Nesbett [1], who suggested unrestricted Hartree–Fock (UHF) approximation to describe electronic properties of radicals, which has remained conceptually the best until now. First applications of the approach to open-shell species revealed a characteristic UHF feature concerning the spin contamination (SC) of the spin multiplicity of the ground states in the term of the total squared spin profit $\Delta \hat{S}^2 = \hat{S}^2_{UHF} - \hat{S}^2_{exact}$ that is the most pronounced in the singlet case due to $\hat{S}_{exact}^2 = 0$. The SC evidences the breaking of spin symmetry of the electronic system. Prominent Löwdin's papers [2,3] allowed establishing a direct connection between SC and/or broken spin symmetry (BSS) with electron correlation, which results in a concept of configurational interaction (CI). Protesting against the BSS as a physical reality, its appearance in the UHF framework was explained by not taking CI into account to the full extent. From now on, the development of the quantum chemistry of open-shell molecules has continued into two directions. The first stream (CI branch herein) was based on the wish to restore BSS substituting two-determinant UHF computational algorithm by multi-determinant ones that provide CI accounting [3]. Changes concerned wave functions that became more and more complicated while the Hamiltonian of the systems remained unchanged. Many computational schemes has been suggested in this way. A most recent review [4], presented by Chattopadhyay's team, gives quite complete description of the CI branch modern state of art and supplies readers with many valuable references.

The second UHF branch was based on the acceptance of BSS in open-shell molecules as a physical reality with SC as a characteristic mark of the issue. The approach was originated by Takatsuka, Fueno, and Yamaguchi [5] and was supported by Davidson and his coworkers [6]. Forty-year development of the approach led to its formulation in terms of emergent phenomena in many-electron systems [7-12]. Conceptually, this view of electronic systems is as follows. When the many-electron system is spin symmetric, the interaction between electrons adiabatically reduces to the sum of solutions for individual electrons when the interaction falls away. This is typical for closed-shell electron systems and is successfully realized, say, in two Hartree–Fock (HF) versions, making restricted and unrestricted ones identical. When the symmetry is broken, the solution for interacting electrons does not obey this law; as a result, there are new residual (so-called *emergent*) phenomena at a zero interaction, revealed by UHF [13] and not seen by RHF. Thus, the key question is whether these residual phenomena can be regarded as compatible with physical reality. The answer divides quantum physicists into reductionists and emergentists, saying no and yes, respectively. This view on the situation with open-shell molecules was introduced to the scientific community by the Nobel Prize winner in Physics 1977, P.W. Anderson, in his famous article "More is different" [7], based on the UHF concept. The idea was supported and continued by one more Nobel Prize laureate in Physics 1998, R.B. Laughlin [8], and opened the door to a realm of unexpected phenomena [9-12]. As it turned out, in physics, emergent phenomena resulted from symmetry breaking are quite numerous and well known. It is enough to mention emergents, inseparable from the solidstate theory such as various quasiparticles: phonons, excitons, solitons, polarons, anions, and so forth, as well as physical phenomena such as topological conductivity, magnetism, and superconductivity. Analyzing the situation with the UHF application to chemistry [14], it turned out to be possible to propose the extension of the emergent concept on chemistry as well, thus addressing the consideration of open-shell molecules in terms of the UHF emergents. Such an approach not only supplies a computationist with classifying markers that make the treatment well-ordered and conceptually self-consistent, but has one more advantage over the CI branch, which is provided with high efficiency of the UHF algorithm, particularly implemented in semi-empirical versions, allowing computational treatment of large molecules.

On practice, in computational spin chemistry of open-shell molecules, there has been a paradoxical situation. Quantum chemists are mostly committed to the reductionist concept

of the CI branch. However, the practical application of advanced and most accurate CI methods is still limited to quite small molecular systems, while the real chemistry requires the consideration of large electronic structures containing above a hundred atoms. Meeting these requirements, a lot of effort was made to develop approximate but time-consuming techniques. At the same time, it happened historically that the UHF approximation was publicly repeatedly declared conceptually opposite to the mainstream CI one. Its inherent emergents were heralded to be fundamental errors [15,16] or even unphysical [17]. Expectedly, the approach has been excluded by the mainstream from the proper techniques, and the empty place was quickly occupied with approximate methods, such as density matrix renormalization group (DMRG) [18], restricted active space spin-flip (RAS-SF) [19], and various versions of DFT. If the first two methods could still be considered as some advance towards exact CI methods, then the DFT threw computationists far back into the domain of one-determinant methods. Notwithstanding, the quantum chemical community not only did not resist this seizure, as was in the case of UHF, but encouraged and approved it in every possible way. It did not matter that the DFT in all its aspects not only does not approach CI methods, but is significantly inferior to the UHF approximation. If for closed-shell molecules, this drawback could be compensated by the special empirically based adaptation of functionals, which makes the technique fully empirical, it turned out that DFT was not cut out for open-shell molecules at all (see a detailed discussion of the UDFT problems related to the case [20–22]). Similarly to UHF concept, DFT refuses to spin symmetry when transforming into an unrestricted (UDFT) version. In addition, UDFT algorithm operates with spins in non-direct and much more complicated way and touches on not only wavefunctions, but the Hamiltonian as well, thus making the restoration of spin symmetry absolutely impossible [8]. In all the cases of comparative studies, which used UHF, some CI approaches, and UDFT (see a brief review of the issue in [14] as well as the most recent publication [23]), UDFT demonstrated the worth results with respect to the former two techniques, which, in contrast, showed practically identical results. Despite these obvious and well known unfavorable circumstances, over the past two decades, DFT spin chemistry has turned into massive virtual computational chemistry of open-shell molecules, which has flooded hundreds and thousands of scientific publications. Not only UDFT, but widely used restricted DFT as well, can be met on these pages. To date, the capabilities, availability, and effectiveness of DFT methods have been compared with experimental synthetic and analytical procedures, because of which they have become an integral part of practical chemistry.

It had to happen that this period coincided with the time when specific molecules appeared on the stage of modern chemistry- sp^2 nanocarbons, including fullerenes, carbon nanotubes, and graphene. All the species contain even number of electrons. Spin multiplicity of the ground state of all of them must begin with a singlet. A whole army of quantum chemists, equipped with the most modern DFT versions, which are in the public domain, rushed to storm new peaks. On the other hand, quasi CI techniques DMRG and RAS SF, efficient enough to treat a large class of open-shell molecules related to polynuclear aromatic hydrocarbons (PAH) (see review [24]), turned out to be inapplicable to sp^2 nanocarbons. At the same time, all these molecules, unique in their properties, are quite complex with respect to handling methods. Accordingly, experimental studies have been noticeably lengthened and became more complicated, which led to the dominant contribution of DFT-based calculations to this field of chemistry, markedly dividing it into real and virtual. Therewith, virtual fullerenics and graphenics confidently heralds the explanation and prediction of everything: new properties, new materials, and, most importantly, new applications. However, real chemistry lags behind and does not reveal these new expectations. This discrepancy was especially noticeable during the fulfillment of one of the programs with the largest budget for material science known to date, which is the international program "Graphene Flagship" [25]. Serious complications, met with fulfilling given promises, first led to the appearance of the terms of "good" and "bad" (high-performance and low-performance) graphene [26], and then six years later, the program founders started

discussing the dishonesty of graphene material manufacturers [27]. However, the true reason for the problem is the incorrect concept of graphene as a technological material, which was imposed by the unlimited dictate of virtual DFT graphenics. The true properties of graphene turned out to be undisclosed, while presentations of its chemical and physical properties were erroneous. In practice, graphene really behaves as a radicalized object, the spin essence of which the DFT was unable to notice. Even in the latest publication, concerning a seemingly coordinated attitude to the radical properties of small graphene fragments [28], they are considered with an indispensable eye on the DFT. At the same time, remaining in shadow and developing in parallel, the UHF concept of computational graphenics has acquired new evidence of the legitimacy of the approach and the results obtained [29-37]. The semi-empirical UHF method has proven to be very effective so that the calculations of, say, fullerene C_{60} or C_{70} do not take more than ten minutes on an advanced personal computer, while systems of 200-400 atoms can be considered for one-three days. This allows performing not only single computations, but computational experiments on numerous objects to prove the words of one of the Nobel Prize laureates in chemistry R. Hoffman: "It goes without saying that theory is really of value when it is used to perform numerical experiments that capture a trend. Not numbers, but a trend" [38]. The current paper is devoted to trends in spin chemistry of sp^2 nanocarbons revealed by UHF emergents and supported by numerous experimental evidences. The paper presents the issue from the standpoint of a user of computational quantum-chemistry, based on the experience gained during about thirty years.

3. Grounds of UHF Computational Spin Chemistry of *sp*² Nanocarbons

3.1. General Remarks

Naturally, the combination of words "spin chemistry" carries an understanding of the special role of electron spins in the ongoing chemical transformations. To make this process visible from the viewpoint of the UHF-spin chemistry, we shall divide it into four conditional stages that present the main issues of practical chemistry:

- Spin traits of the reactants that enter into reactions;
- Spin kind of the intermolecular interaction that controls such reactions;
- Spin nature of the reaction final products;
- Post-reaction storage of spin chemistry products.

Before starting, we have to realize which features of the above issues will be described in terms of UHF emergents. Among many others, we will mainly concentrate on those that are related to the equilibrium ground state, leaving aside continuous symmetry problems caused by spin symmetry breaking [39] that drastically change the appearance of optical electron [35] and vibrational [40] spectra of open-shell molecules. Concerning the ground state, the following features are of interest:

- Ascertainment of the radical status of an open-shell molecule;
- Evaluation of the molecule chemical activity provided with spin density;
- Establishment of the spin density delocalization over the molecule atoms;
- Determination of the delocalization of the chemical activity over molecule, atoms thus presenting its "chemical portrait";
- Detection of the spin-chemical topology caused by the multi-target character of the molecules.

The following quantities calculated during the computational experiment are the source of the required information. First, there are the molecule total energies E_{sg}^{RHF} , E_{sg}^{UHF} , and E_{tr}^{UHF} , and two differential energies ΔE_{sg}^{RU} (= $E_{sg}^{RHF} - E_{sg}^{UHF}$) and ΔE_{ST}^{UHF} (= $E_{tr}^{UHF} - E_{sg}^{UHF}$) (subscriptions *sg*, *tr*, and *ST* mark singlet and triplet states and the singlet–triplet energy gap, respectively). The second place is occupied by emergent spin characteristics $\Delta \hat{S}^2$ (= $\hat{S}_{uHF}^2 - \hat{S}_{exact}^2$), *SpD*_{tot}, and *SpD*_A as well as N_D and N_{DA} (*SpD*_{tot} and N_D describe total spin density and total number of effectively unpaired electrons [5,6], while subscript *A* matches these values related to atom A). A complete set of {*sp*²C=C bonds} closes

the necessary suit of source data. In what follows, the description of the above issues will be carried out on the example of spin topochemistry of a representative set of sp^2 nanocarbon molecules, including fullerene C_{60} , a fragment of a single-walled carbon nanotube (SWCNT), and carbon honeycomb-structure compositions, presenting a set of graphene molecules.

3.2. Common Background for the sp² Nanocarbons Features

Despite the fact that { $sp^2C=C$ bonds} pool ends the above list of initial data, it is the network of these bonds, which is the general structural motive of substances as well as the main reason of their peculiarity. The bonds are quite labile and may change the length in the range of 1,326–2,158 Å (see Section 2 of the monograph [37] and Ref. [41]). In this way, they transform from covalent non-radical to fully radicalized bonds. The radicalization extent depends on the current bond length and starts from zero at the critical bond length $R_{crit} = 1,400 \pm 0,005 A$ and drastically grows when the length exceeds R_{crit} . The critical value slightly depends on the bond's surroundings and changes from 1,395 to 1,408 Å when going from ethylene to hexamethylbenzene. The transformation of the bonds from covalent to radicalized ones leads to the transition of a closed-shell electronic structure to an open-shell one. Certainly, we begin the consideration of the chosen nanocarbon molecules from the description of { $sp^2C=C$ bonds} distribution.

It is obvious that in the case of extended bond networks, not only individual bond lengths, but also a composition of the bonds in the pool are significant. The latter particularity is seen in Figure 1, where the bond distribution of three sp^2 carbon molecules is presented. Inserts in the figure represent equilibrium structures of fullerene C₆₀, a fragment of (4, 4) SWCNT, and right-angle fragment of a flat honeycomb structure with five benzenoid units along both zigzag and armchair edges, (5, 5) NGr molecule herein. As shown in the figure, in all the cases, the bond lengths cover a large region of ~0,3 Å in width. Those with the length over R_{crit} make up more than half of the pool. Evidently, the presence of these bonds lays the foundation of the open-shell character of the molecules. However, the generality of the { $sp^2C=C$ bonds} distribution of the sp^2 molecules in question ends there. Their distribution plottings are quite different and deserve particular consideration.



Figure 1. Cont.



Figure 1. $Z \rightarrow A$ distributions of $sp^2C=C$ bonds in fullerene C_{60} (**a**), a fragment of (4, 4) SWCNT (**b**), and nanographene molecule (5, 5) NGr (**c**). Calculations are performed using CLUSTER-Z1 software implementing AM1 semi-empirical HF approximation [42]. Closed-shell version of the study is presented by the RHF solutions.

Fullerene C_{60} . Widely accepted presentation about the molecule local symmetry I_h is supported by closed-shell (RHF) calculations only. The exact symmetry of the molecule in the UHF approach is C_i [39], and the symmetry difference is clearly evident in Figure 1a. It should be noted that a division of bonds into a bilength pattern involving short and long ones remains in both cases. The difference concerns these bonds' dispersion, which is $1,385 \pm 0,0002$ and $1,463 \pm 0,003$ Å for the bond pairs in the RHF solution and $1,391 \pm 0,032$ and $1,464 \pm 0,013$ Å in the UHF case. Obviously, the dispersion changes are not too drastic, due to which the symmetry changing in fullerene C₆₀ presents a perfect example of a continuous symmetry when the reduced symmetry, in fact, remains high to a large extent [43]. In the current case, C_i symmetry of C₆₀ includes 95% of I_h [39]. Nevertheless, the deviation from the I_h is definitely revealed experimentally by the appearance of, say, forbidden transitions in optical [35,39] and vibrational ("silent modes") [40] spectra of the molecule.

It is important to note that the difference in the RHF and/or UHF description of the molecule $\{sp^2C=C \text{ bonds}\}$ pool concerns not only the change of equilibrium symmetry, but the reaction of the pool to any impact on the molecule. In the case of closed-shell approximation, each individual addition is local and it only slightly disturbs the distribution of the remaining bonds. In contrast, the UHF approach reveals a considerable rearrangement of the whole pool of bonds at each case of the intrusion, thus demonstrating a collective

character of the molecule valence electron structure (see detailed discussion of the feature on many examples in [44]).

(4, 4) SWCNT. The bilength bond structure is characteristic for not only fullerene C_{60} , but a series of PAHs and is commonly considered as a characteristic mark of the molecule aromaticity. Accordingly, until now, sometimes a referring to fullerene C_{60} as aromatic specie can still be found in literature. However, this format of the bond structure strongly violates in the case of C_{70} and fully disappears in CNTs and graphene molecules. Figure 1b exhibits the picture of $\{sp^2C=C \text{ bonds}\}$ distribution of the (4, 4) SWCNT fragment determined in two approximations [45]. In contrast to C_{60} , the closed-shell model reveals 10 groups of the bonds with small dispersion within each group and quite large changing between the groups. The open-shell approximation leads to a remarkable ordering of the tube bond structure, decreasing the group number practically by half. Particularly noticeable is the group in the plotting middle covering a continuous change of the length from 1,436 to 1,431 Å, which is related to the tube sidewall. Actually, when the fragment length increases, this group grows as well. Both distributions in Figure 1b also reveal short-length groups related to the tube cap and long-length ones attributed to the tube open end. When the cap is substituted with open end, the short-length bonds disappear from the plotting. This cap-sidewall-end plotting of the $\{sp^2C=C \text{ bonds}\}$ remains when tubes diameter increases as well as when (n, n) tubes are substituted with (n, m) ones [45]. The reaction of the $\{sp^2C=C \text{ bonds}\}$ on chemical addition depends on the locality of the latter. In the sidewall region, the response is quite local, while a considerable disturbance is characteristic for caps and open ends.

(5, 5) *NGr molecule*. A comparative pattern of $\{sp^2C=C \text{ bonds}\}$ of the closed- and open-shell compositions of the molecule is similar to that one discussed above for the tube with the only difference being related to the absence of characteristic "sidewall" bonds. Extending the molecule size leads to increasing the groups number while smoothing the difference between the groups, which results in a continuous decreasing of bond lengths from ~1,49 to 1,33 Å in the relevant Z \rightarrow A plottings. One more peculiarity is characteristic for graphene molecules. It concerns the response of the whole $\{sp^2C=C \text{ bonds}\}$ pool on the chemical addition, which drastically changes the pool distribution at each action (see a detailed discussion of the feature on various examples in [37]).

Besides the features discussed, Figure 1c draws attention to one more exclusive particularity of the molecule. It concerns the extremely small singlet–triplet gap E_{ST} , which in the case of (5, 5) NGr constitutes -6.096 kcal/mol. The triplet state is slightly lower than the singlet, which means the two states are strongly mixed. Applying the UHF approach to both states separately, we obtain quite similar { $sp^2C=C$ bonds} plottings, which is clearly seen in the figure.

Completing the description of $\{sp^2C=C \text{ bonds}\}\$ pools, we can draw the following conclusions.

- 1. More than half of $sp^2C=C$ bonds of sp^2 nanocarbons, including fullerenes, carbon nanotubes, and graphene molecules, are longer than critical interatomic distance R_{crit} , exceeding over which leads to the bond radicalization. The feature lays the foundation of the open-shell character of the species electron systems and radical character of the molecules.
- 2. If bilength bond composition is characteristic for the $\{sp^2C=C \text{ bonds}\}\ pool of fullerene C_{60}$, many-length composition is typical for more extended $\{sp^2C=C \text{ bonds}\}\ networks$ starting from fullerene C₇₀ and involving CNTs and graphene molecules.
- 3. Application of UHF approach allows disclosing a collective response of $\{sp^2C=C \text{ bonds}\}\$ pool to each act of any chemical addition to the relevant species in all the cases, thus revealing delocalization of the bond distribution disturbance.

4. Spin Traits of Open-Shell Molecules of *sp*² Nanocarbons

4.1. Fullerene C_{60}

Having dealt with the $\{sp^2C=C \text{ bonds}\}$ pool of the chosen molecules, we now turn to data concerning their energies and spin emergents. The collection of the corresponding source data is presented in Table 1. The data evidence convincingly that the considered molecules are of the open-shell type and their chemistry is spin by nature. The first acquaintance with UHF spin chemistry is best to start with C_{60} fullerene, which has all characteristic emergents of open-shell molecules, on the one hand, and is a real wellknown molecule, on the other, which allows addressing experimental data to confirm computationally predicted emergent features. As seen in Table 1, the UHF approach remarkably lowers the energy of the singlet state, which is much lower than the triplet one and constitutes itself as a ground state. The singlet-triplet gap accounts for ~3% of the total energy and is small enough for the spin contamination of the ground state to be reliably fixed. Due to the singlet character of the ground state, the total number of effectively unpaired electrons N_D equals to the doubled spin contamination ΔS_{so}^2 [5,6]. This number is distributed over the molecule atoms in terms of partial numbers N_{DA} , plotting of which over the molecule atoms is shown in Figure 2a in two manners, namely, as histogram presenting $Z \rightarrow A$ distribution and dotted curve related to the atom numbers in the output file. The first plotting allows distinguishing six clearly seen groups of atoms with 12 atoms of the same N_{DA} value per each group of the first four groups and with six atoms of groups 5 and 6. Atoms of the first group form two hexagons (see configurations of slight blue atoms in inserts in Figures 1a and 2a), atoms of groups 2, 3, and 4 are joined by pairs (red, rose, and green), and dark blue atoms are singles [46]. Figure 2b presents an $A \rightarrow Z$ spin density distribution that clearly demonstrates antiferromagnetic delocalization of the density over the molecule atoms providing the *SpD*_{total} exact zeroing.

Table 1. Energies (kcal/mol) and emergent spin characteristics of the sp^2 molecules in the ground state.

Molecules	E_{sg}^{RHF}	E_{sg}^{UHF}	ΔE_{sg}^{RU}	E_{tr}^{UHF}	ΔE_{ST}^{UHF}	$\Delta \hat{S}^2$	SpD _{tot}	N_D
C ₆₀	970.180	955.362	14.818	982.917	27.555	4.92	0	9.84
(4, 4) SWCNT	1819.509	1648.338	171.171	1627.308	-21.030	19.758 sg	0	39.515 sg
						20.325 tr	2	38.651 tr
(5, 5) NGr	1802.381	1454.492	347.889	1448.396	-6.096	16.930 sg	0	33.860 sg
						18.121 tr	2	34.242 tr

Since N_{DA} represents atomic chemical susceptibility (ACS) [47], the insert images in Figures 1 and 2 portray the chemical reactivity distributed over the molecule atoms from the most reactive (light blue) to the most inactive (dark blue), thus allowing drawing the fundamentals of the C_{60} spin chemistry. The first feature of the set states that the molecule is chemically active and its molecular chemical susceptibility (MCS) N_D constitutes 9.87 e. According to the second echelon, the molecule is a multi-target chemical object, since all its atoms can participate in the chemical reaction with a fractional ACS contribution N_{DA} . Following the third-step element, the molecule enters any chemical action by atoms of the highest ACS related to the largest N_{DA} value. Since N_{DA} distribution over the molecule is spatially peculiar and changes at each reaction step, a chemical reaction, involving fullerene C_{60} , acquires topological features depending on the chemical counteragent, which is the fourth-step element of the C_{60} spin chemistry. The fifth element concerns the polyderivative character of the reaction between any reagent and fullerene. The sixth one determines the derivative order related to the reaction completion, which is due to continuous decreasing of the molecular chemical susceptibility N_D in the course of the reaction until it is worked out up to nil. Evidently, the reaction may be stopped before N_D reaching nil due to sterical obstacles.





Atom number

Figure 2. (a). Atomic chemical susceptibility N_{DA} of fullerene C₆₀, distributed over the molecule atoms according to either their numeration in the output file (curve with rhombs) or in the Z \rightarrow A manner (histogram). Different colors in the insert on the right distinguish six atomic groups shown by the histogram. (b) Spin density distribution.

4.2. (4, 4) SWCNT Fragment

As it turned out, the fundamentals discussed in the previous section govern generally the spin chemistry of not only C_{60} and higher fullerenes [44], but also other sp^2 nanocarbons such as CNTs and graphene molecules. As seen in Table 1, the UHF approximation eliminates the artifact when the RHF singlet state is located much above the triplet one and displaces the singlet downwards. The energy gap E_{ST} is small and makes up 1.3% of the energy of the singlet state. For the current case, the gap is negative, indicating that formally the triplet should be attributed to the ground state. Notwithstanding, the sign of the gap is not steady and changes when either length or diameter of the tube increases. The only steady point is that the gap is small so that singlet and triplet states are mixed. It should be noted that the spin contaminations of both states, $\Delta \hat{S}_{sg}^2$ and $\Delta \hat{S}_{tr}^2$, as well as the total numbers of effectively unpaired electrons, N_{Dsg} and N_{Dtr} , are considerable and practically the same. The spin-triplet near-degeneracy, which is typical for polyradicoloids with double C=C bonds [23,24], greatly complicates the description of open-shell electronic states [4,21,22], and a proper computational technique has been still absent. Therefore, we will have to limit ourselves to the available capabilities and hold a discussion of the question posed in terms of the UHF consideration of the singlet state.

The description of the singlet (4, 4) SWCNT molecule as an open-shell system is much the same as that of fullerene C₆₀. Plotting in Figure 3 presents the ACS N_{DA} distribution over the molecule atoms. The distribution convincingly tell us that (i) the tube is a multi-target object; (ii) the main reaction ability is concentrated on open-end atoms and these atoms enter any reaction always first; and (iii) fewer active atoms are located in the cap zone and still fewer active atoms are distributed along sidewall. Different from the fullerene case are the extremely high ACS values for open-end atoms. The feature is connected with the fact that ACS of cap and sidewall atoms is determined by the { $sp^2C=C$ bonds} pool, due to which their ACS is comparable with that of fullerene atoms, while ACS of open-end atoms are additionally provided by dangling bonds (DBs). Actually, as seen in the figure, saturation of these DBs by monoatomic hydrogens drastically inhibits the end atoms' reactivity, equalizing it with the sidewall one. The discussed fundamentals govern all general features of the CNT spin chemistry, which are widely confirmed experimentally [48].



Figure 3. Standard ACS N_{DA} image maps over atoms of (4, 4) single-walled carbon nanotubes shown in insert with empty (curve with dots) and hydrogen-terminated (histogram) ends. The numbering follows a movement along the tube atoms from the cap to the open end.

4.3. (5, 5) NGr Molecule

As seen in Table 1, everything that was said earlier with respect to the singlet–triplet degeneracy of the CNT states can be readdressed to this graphene molecule. In the latter case, the degeneracy becomes even more pronounced, since the E_{ST} gap decreases even more and accounts for 0.4% of the total energy. Expectedly, the sign of E_{ST} can easily alternate and, in fact, this is what happens when size, shape, and chemical modification in the area of edge atoms change. Leaving for the future a correct theoretical consideration of open-shell systems with nearly degenerate states, we restrict ourselves below to the discussion of graphene molecules in the framework of the UHF consideration of one of the degenerate states. As has occurred in the current study, the consideration of either singlet or triplet state leads to practically the same results that might be caused by the close equality of $\Delta \hat{S}^2$ and N_D data for both states.

A considerable value of MCS N_D evidences high chemical activity of the (5, 5) NGr molecule as a whole. Distributed over the singlet molecule atoms, it is presented as an ACS N_{DA} histogram plotting in Figure 4. The spin density distribution is qualitatively identical to that of fullerene C₆₀ in Figure 2b with *SpD*_{total} equal zero [46]. As for N_{DA}

plotting shown in the figure, edge atoms dominate due to large contribution providing with DBs. As in the case of CNT, considered previously, their chemical reactivity can be inhibited by monoatomic termination of edge-atom DBs by hydrogens. In this case, the molecule becomes one of known polyradicaloids belonging to *perip*entacenes [24], the radical essence of which is presented by the curve with dots in Figure 4. Edge atoms mark the zone of the highest reactivity, while the reactivity of those in the basal plane is mainly determined by the {*sp*²C=C bonds} pool and is at the level of fullerene and CNT sidewall atoms. The molecule as a whole is evidently multi-target prone to polyderivatization. Each step of polyderivatization is accompanied by the redistribution of remaining *sp*²C=C bonds and, consequently, of N_{DA} values, thus evidencing a collective character of the electron system of the molecule. A drastic difference in chemical reactivity of edge and basal-plane atoms as well as a sharp anisotropy of the spatial structure in the direction normal to the basal plane provide extreme conditions for topological spin chemistry [49]. Taken as a whole, the described chemical behavior of graphene molecules is observed experimentally. Readers can find a number of examples in monograph [37].



Figure 4. Standard ACS N_{DA} image maps over atoms of (5, 5) NGr molecule with empty (histogram) and hydrogen-terminated (curve with dots) edges. Insert: equilibrated structures of the parent (5, 5) NGr molecule and its monohydrogenated homologue *peri*pentacene.

All the peculiarities of molecules discussed above are rooted in the spin symmetry breaking. We share the view that the action is resulted from the occurred quantum transition [14] that makes the UHF approach a good basis for the description of ground state, experimental justifications of which were discussed in [14] and have received the additional confirmation just recently [23]. Characterized in terms of UHF emergent, spin traits of the discussed molecules include the following issues. At atomic level, the latter concerns a large set of local spins that lay the foundation of the over-atom delocalization of both spin density and chemical activity. At the molecular level, high molecular chemical susceptibility, evidencing radical character of the molecules, and topological character of chemical reactions are the main issues. At the energy level, small energy gap ΔE_{ST}^{UHF} of alternate sign draws attention to an exceptional feature concerning singlet–triplet near-degeneracy. The issue causes the necessary inclusion of the development of the quantum theory of open-shell electronic systems with pronounced singlet–triplet degeneracy in the agenda of modern quantum chemistry.

5. Electron Spins in Intermolecular Interaction

When one of the partners of a chemical reaction is of the open-shell type, the intermolecular interaction (IMI) between partners considered in the UHF approximation takes spins into account directly, operating with two kinds of determinants related to α and β spin orbitals. The participation of spins in the formation of this interaction is hidden from the outside view, and the correctness of their accounting can be judged only by results concerning, say, final products of the reaction. This aspect will be discussed in detail in the next section. Herein, we shall consider a particular case when spins are evidently involved in the IMI. The matter is that sp^2 nanocarbons molecules are not only an open-shell species, but are characterized by exclusive donor–acceptor records. Quite low ionization potentials and high electron affinities allow them behaving both donors and acceptors simultaneously. The issue is of particular importance when concerning IMI [44,50]. Combining both open-shell and donor–acceptor character, IMI leads sometimes to an exciting result. Photodynamic (PD) effect, directly concerning IMI of fullerene C₆₀ and molecular oxygen [51], can be the best example. The effect is widely used in the medicinal chemistry. It concerns the transformation of triplet molecular oxygen into a singlet one under photoexcitation in the presence of fullerene C₆₀. Turning off the light returns the system to its previous state with inactive oxygen.

Many spears have been broken in attempts to explain the observed effect without taking into account the open-shell character of the fullerene (see [52,53] and references therein). Until now, the mechanism of the effect has been hidden behind a slogan "triplet state photochemical mechanism" according to a widely accepted scheme [53,54]

$${}^{1}C_{60} \xrightarrow{h\nu} {}^{1}C_{60}^{*} \to {}^{3}C_{60}^{*} \xrightarrow{{}^{3}O_{2} \to {}^{1}O_{2}} {}^{1}C_{60}$$
(1)

The scheme implies the energy transfer from the singlet photoexcited fullerene to the triplet one, which further transfers the energy to convenient triplet oxygen, thus transforming the latter into an active singlet one. The first two stages of this "singlefullerene-molecule" mechanism are quite evident, while the third one, the most important for the final output, is obscure in spite of a number of speculations available [54]. Obviously, this stage efficacy depends on the strength of the IMI between fullerene and oxygen molecules. Numerous quantum chemical calculations show that pairwise interaction in the *f*-*o* dyad [$C_{60} + O_2$] in both singlet and triplet state is practically absent. The UHF computations [55] fully support the previous data and determine the coupling energy of the dyad E_{cpl}^{f-o} equal zero in both cases. This poses a serious problem for the explanation of the third stage of the above scheme, forcing the suggestion of the origination of a peculiar IMI between C_{60} and O_2 molecules in the excited state once absent in the ground state.

However, the IMI in the PD solutions is not limited by the fullerene–oxygen interaction only. There are two other interactions, namely: fullerene-fullerene (f-f) and fullerenesolvent (f-s), among which the former is quite significant, thus revealing itself as the fullerene dimerization [56] as well as a considerable amplification of the spectral properties of fullerene solutions [57]. The *f*-*s* interaction in the case of aqueous and benzene solutions can be ignored. Besides a significant strength, the *f*-*f* interaction possesses some peculiar features caused by the exclusive D-A ability of fullerenes [50]. A significant contribution of the D-A component into the total IMI results in a two-well shape of the potential energy term of a pair of fullerene molecules in the ground state, which is schematically shown in Figure 5a. According to the scheme, the pairwise interaction between the molecules in convenient solutions always leads to the formation of bi-molecular or more complex homoclusters of fullerenes in the vicinity of the R^{00} minimum on the potential energy curve. The dimerization (as well as oligomerization) is a barrier reaction and does not occur spontaneously. Particular measures should be undertaken to come over the barrier and provide the molecule chemical coupling, in spite of the clusterization is energetically profitable. Photoexcitation is one of the most efficient tools. Therefore, the PD solutions under ambient conditions should involve conglomerates of clustered C₆₀ molecules as shown schematically in Figure 5b, which is experimentally proven in many cases (see for example [57–59]). If we remember that $E_{cpl}^{f-o}=0$ in both singlet and triplet state, it becomes clear that oxygen molecules do not interact with either individual fullerene molecule or the

molecule clusters, so that the total energy of any f-o dyad [(C_{60})_n- O_2] (n= 1, 2, 3 . . .) is just a sum of those related to the dyad components. It is always by 9.93 kcal/mol less in the triplet state due to the difference in the energy of the triplet and singlet oxygen (the UHF energy of ${}^{3}O_{2}$ and ${}^{1}O_{2}$ molecules constitutes -27.75 and -17.82 kcal/mol, respectively). Therefore, the ground state of the f-o dyads is triplet.



Figure 5. Photodynamic effect of the $[C_{60} + O_2]$ complex. (**a**) Scheme of the IMI terms related to the interaction between two fullerene molecules. (A^0B^0) and (A^+B^-) match branches of the terms related to the interaction between neutral molecules and their ions, respectively. R^{+-} and R^{00} mark minimum positions attributed to the formation of tightly bound dimer (AB) and weakly bound charge transfer complex $(A^0 + B^0)$, respectively. R_{scn} indicates the point of avoidable intersection of terms (A^0B^0) and (A^+B^-) . (**b**) Schematic presentation of fullerene clusterization in solution. (**c**) The formation of an ionic pair of C_{60} under photoexcitation. The only ion pair is formed under photoexcitation of the $(C_{60})_n$ cluster of any content. (**d**) Schematic presentation of the spin-flip in oxygen molecule under photoexcitation. (**e**) ACS distribution over atoms of ${}^2[C_{60}^- + O_2]$ (histogram) and ${}^2[C_{60}^+ + O_2]$ (red curve) complexes.

Computations have shown [56,57] that each pair of fullerene molecules as well as any fullerene cluster of more complex structure formed at the R^{00} minimum is a charge transfer complex. Their absorption bands related to B_2 phototransitions in Figure 5a are located in the UV-visible region. The photoexcitation of either pair or cluster of fullerene molecules within this region produces a pair of molecular ions that quickly relax into the ground state of neutral molecule after the light is switched off. Calculations revealed [55] that, in contrast

to neutral C_{60} , both molecular ions C_{60}^{-} and C_{60}^{+} actively interact with oxygen molecule producing coupling energy E_{cpl}^{-f-o} and E_{cpl}^{+f-o} of -10.03 and -10.05 kcal/mol, respectively, referring to ${}^{3}O_{2}$ molecule and -0.097 and -0.115 kcal/mol in regards to ${}^{1}O_{2}$. Therefore, the pristine oxygen molecule is quite strongly held in the vicinity of both molecular ions, thus forming $[C_{60} + O_2]^-$ and $[C_{60} + O_2]^+$ complexes, as schematically shown in Figure 5c. The complexes are of ${}^{2}[C_{60}^{-}+O_{2}]$ and ${}^{2}[C_{60}^{+}+O_{2}]$ compositions of the doublet *SpM*. Both fullerene ions take the responsibility over the multiplicity, so that two odd electrons of the oxygen molecule "lose their job" and do not more maintain the molecule triplet SpM, thus adding two effectively unpaired electrons to the N_D pool of unpaired electrons of the whole complex, as shown in Figure 5e. A dominant contribution of electrons located on oxygen atoms 61 and 62 is clearly seen, thus revealing the most active sites of the complexes. It should be noted that these distributions are intimate characteristics of both complexes, so that not oxygen itself but ${}^{2}[C_{60}^{-}+O_{2}]$ and ${}^{2}[C_{60}^{+}+O_{2}]$ complexes as a whole provide the oxidative effect. The effect lasts until the complexes exist and is practically immediately terminated when the complexes disappear when the light is switched off. The obtained results make it possible to suggest the PD mechanism schematically presented in Figure 5d. As shown in the figure, changing SpM from triplet to doublet under photoexcitation due to passing from neutral molecule complex to those based on fullerene molecular ions results in a spin flip in the system of two odd electrons of the oxygen molecule. This approach allows attributing PD effect of fullerene solutions to a specific type of spinchemical reaction. Particular D-A properties when the molecule can be both the donor and acceptor of electrons are evidently characteristic not only to fullerenes C_{60} and C_{70} as well as their derivatives, but to CNT [45] and nanosize graphene molecules [60], thus demonstrating them as an additional characteristic feature of open-shell molecules. This opens a large new branch of a spin photochemistry of the species.

6. Spin Nature of the Reaction Final Products

As follows from the abovementioned, the considered representatives of sp^2 nanocarbons enter a chemical reaction equipped with high MCS and a large network of target atoms marked by ACS. The targets are definitely discriminated by the relevant N_{DA} value. Thus, the first step of any additional reactions involving fullerenes C_{60} will occur with one of the hexagon light blue atoms shown in Figures 1a and 2a. In the case of CNTs and bare graphene molecules, open-end and zigzag-edge atoms play the role, respectively. A lot of information concerning a particular chemical activity of open-end atoms of CNTs and edge atoms of graphene sheets can be found in literature. Actually, convincing evidence that the edge atoms of graphene carry additional electronic (including spin) density was shown by unique experiments on scanning graphene ribbons with atomic resolution [61,62] (see a detailed discussion of the experiments in [14]). As for fullerene C₆₀, a convincing confirmation of the existence of special two rings in this molecule structure was first discovered in 2008 and then confirmed in 2012 in atom-resolved STM [63] and AFM [64] studies. The joint results of the studies are presented on panel I in Figure 6. A scrupulous analysis of the STM image [63] showed that the molecule is attached to the Cu(111) substrate via contact area having a hexagon shape; therewith the area is duplicated above, thus forming the imaged produced by scanning two hexagon circles of atom located one over the other. In the molecule structure, there is only one pair of such hexagon configurations that coincide with those marked by light blue color in Figure 1a. It is obvious that when the molecule interacts with an extended solid body, the coupling depends on the number of contacts and the interaction strength in each contact. Six light blue carbon atoms best satisfy both requirements, which explains the hexagon configuration of the molecule contact with the flat Cu(111) surface, as seen by STM. The experimental image of AFM scanning (I), in its turn, exhibits homogeneous distribution of the interaction force over the atoms, which is expected if taking into account the equality of N_{DA} values for the atoms (see Figure 2a). A tight connection with exclusive atom-resolved AFM images of sp^2 carbon species (see a profound review [65]) and the corresponding N_{DA} distribution is discussed in details in Ref. [14].

Figure 6. (I) STM image of C_{60} on Cu(111) (left-up-corner insert) that reveals the orientation of C_{60} , while the main image presents the constant-height AFM images of C_{60} on Cu(111) obtained with a CO tip (see text). (II–VI) Computational spin chemistry of fullerene C_{60} . Monodentant polyderivatives $C_{60}H_{18}$ (II), $C_{60}F_{18}$ (III), $C_{60}(CN)_{18}$ (IV), and $C_{60}Cl_{18}$ (V) obtained at the 18th step of the successive polyderivatization following N_{DA} algorithm; the same for bidentant poliderivative $C_{60}(NH)_9$ (VI) at the ninth step. See detailed discussion in [44].

When the first-step derivative is formed, the molecule responds to the action by reconstruction of its { $sp^2C=C$ bonds} pool and redistribution of N_{DA} markers. The newly appeared highest N_{DA} mark determines the target carbon atom for the second step and so forth. Therefore, following the highest N_{DA} as descriptor of the target atom at each reaction step determines the N_{DA} algorithm of sp^2 carbon molecules polyderivatization. Practical chemistry of sp^2 nanocarbons gives many examples confirming the N_{DA} algorithm implementation. The most characteristic results are obtained for fullerene C₆₀ [44]. Exhibited in Figure 6, polyderivatives II–V present a collection of one-dentant $C_{60}(X)_{18}$ (X=H, F, CN, Cl) species. The first three molecules represent so-called crown structures of local symmetry C_{3v} . These structures were obtained computationally at the 18th step of the successive addition of the addends to C_{60} following the N_{DA} indication. All the above polyderivatives were synthesized in practice, and their structures identical to shown in Figure 6 were determined (see a detailed discussion of the issue in [44]). If the successive addition of addends in the case of $C_{60}H_{18}$ (II), $C_{60}F_{18}$ (III), and $C_{60}(CN)_{18}$ (IV) proceeds quite similarly, addition of chlorine behaves differently from the first step, due to which the structure of $C_{60}Cl_8$ (V) turns out different. This result correlates with known problems concerning the fullerene chlorination [66]. $C_{60}(NH)_9$ (VI) molecule is a bi-dentant species, and its structure at the ninth step of reaction is of C_{3v} local symmetry, thus showing a similar "crown" configuration, which perfectly fits experimental data.

Another face of the N_{DA} algorithm action can be seen from plottings in Figure 7. Those present the evolution of the heat of formation, ΔH , per-step coupling, E_{cpl} , and N_D quantities in due course of hydrogenation and fluorination of fullerene C_{60} [67,68]. As seen in the figure, the two reactions are characterized by significantly different energetic parameters with an obvious favoring to fluorination. Actually, the total energy ΔH of hydrides gradually decreases, which favors the polyhydrides formation, until *k* reaches 15, after which the decreasing temp is slowed down approaching zero at k = 25 and then the energy starts to increase. Since for hydrogen $\Delta H_{mol} = 0$, the E_{cpl} behavior directly exhibits the above changing in the total energy. The behavior of the total and coupling energies of fluorides is similar, with the only difference concerning much bigger values of both ΔH and E_{cpl} as well as the absence of the ΔH increasing at k > 25. However, due to a significant negative value of ΔH_{mol} in this case, the coupling energy becomes positive at k > 25.

Molecular chemical susceptibility N_D is the other characteristic quantifier. As seen in Figure 7b, $N_D(k)$ functions are practically identical for both families, gradually decreasing

at higher *k* and approaching zero at *k*~20–24. Therefore, decreasing E_{cpl} by absolute value correlates with decreasing MCS N_D , or, in other words, with working out the pool of effectively unpaired electrons, which results in a considerable lowering of the reaction activity when *k* changes from 18–20 to 25–26. According to both characteristics, the reaction is terminated at *k* > 25. It is important to note that in spite of obvious obstacles, *k*-high products might be abandoned among the final products. This is due to accumulative character of the reaction until the next addition of the atom pair is energetically favorable. This means that (1) the attachment of a next atom pair will not proceed at positive E_{cpl} and (2) the accumulation time (and mass yield of the product) will greatly depend on the absolute value E_{cpl} : the less the value, the longer time is needed. That is why more than four-times difference in the E_{cpl} absolute values for hydrides in favor of fluorides at k = 18 and their small absolute value result in the termination of hydrogenation process by $C_{60}H_{36}$ product, while fluorination still continues and is completed by $C_{60}F_{48}$. The data presented in Figure 7 are in full consent with experimental ones.

Figure 7. Evolution of the total energy ΔH (**a**), molecular chemical susceptibility N_D , and per-step coupling energy E_{cpl} (**b**) at growing the number of atom pairs *k* for C₆₀ hydrides (dotted curves with empty circles) and C₆₀ fluorides (solid curves with filled circles).

Figure 8 briefly summarizes main features concerning polyderivatization of the (5, 5) NGr molecule. The pristine bare molecule is flat and consists of 66 carbon atoms. Chemical portrait of the molecule is given in the upper part of the figure as ACS N_{DA} distribution over atoms. Following N_{DA} algorithm, the formation of framed graphene molecules occurs at the first stage of the molecule chemical modification (see detailed discussion in [31,32,37]), after which the basal plane becomes the battlefield. Final products are produced in the course of topochemical reaction due to dependence on such important factors as (1) fixation or free standing of the molecule, (2) accessibility of either one or both sides of the molecule plane, and (3) chemical addends in use. The role of these three factors can be seen in Figure 8, where a collection of (5, 5) NGr polyderivatives related to the maximum covering of the

parent molecule by addends is exhibited. Thus, the left column presents graphene hydrides obtained computationally in the course of successive hydrogenation of the parent molecule following N_{DA} algorithm at different conditions. As seen, their structures differ drastically, changing from regular graphane one (a) to highly bent pancake (c) [69]. Not shown in the figure, a canape-like structure of hydride obtained under one-side access of a fixed molecule completes a full list of the products. Experimentally, regular graphane and amorphous canape-like structures of hydrogenated graphene membranes were observed under the relevant conditions [70]. When hydrogen is substituted by fluorine (see Figure 8a), the structure of polyfluorides changes drastically, supporting, in general, the (a)–(c) tendency of hydrides. However, none of the regular graphane-like structures were obtained. A thorough experimental study of graphene fluorides [71] confirms this conclusion. The situation becomes still more cumbersome when hydrogen is substituted with hydroxyls (Figure 8b) or a combination of oxygen atoms and hydroxyls (Figure 8c). The last two cases present selected variants of numerous configurations related to graphene molecule oxygenation [72].

Figure 8. Top–Equilibrium structure of the (5, 5) NGr molecule and the spatial map of the ACS N_{DA} distribution over its atoms. (**a**–**c**) Equilibrium structures of complete graphene hydrides (left column), graphene fluoride, and two graphene oxides (right column, from top to bottom). The double notification, say, C₆₆H₄₄H₄₄, means that the first 44 hydrogen atoms are bound with 22 edge atoms of the (5, 5) NGr molecule, while the other 44 hydrogens are attached to the carbon atoms located in the molecule basal plane.

Therefore, polyderivatization is extremely complicated and covers a great number of final products. As mentioned earlier, addition of each addend at every step is accompanied by immediate reconstruction of the $\{sp^2C=C \text{ bonds}\}$ pool. The pool is highly labile and readily responds to any perturbation. This N_{DA} -reconstructing distribution makes the polyderivatives production highly variable due to high sensitivity to any current situation, thus depriving such names as "graphene hydride", "graphene oxide", "graphene fluoride", and so forth of an exact chemical formulae and allowing speaking about large classes of substances that are related to the above names. Therefore, the chemistry of graphene molecules is not a chemistry of a molecule, but the chemistry of a molecular class.

So far, we have dealt with products of the highest complete derivatization. The massproduced "graphene oxide" (GO) class is their best-known representative [73]. However, there are still innumerable products that are not completely derivated. Framed graphene molecules are of such species. These molecules became a regular participant in the scientific agenda a decade ago when a new high-tech material, reduced graphene oxide (rGO), entered practical graphenics. The product is not synthesized from the bottom, but is produced from the top using GO as a parent species. Evidently, a large GO class gives life to a new rGO class, additionally subjected to variations due to variable conditions of the reduction procedures (see a profound review [74]). rGO molecules present fragments of the honeycomb domains framed by different atomic groups, depending on the reduction technology. The mass product presents a powder of amorphous structure consisting of layered stacks of a few-nanometer thickness and from first nanometers to submicron dimension in the lateral direction. Interlayer distance is close to that of graphite, thus justifying a flat graphene-like structure of the layers (see as example, a neutron scattering study of different-origin rGOs [75]). Accordingly, in the literature, you can often find a reference to rGO as graphene, due to which it was suggested to cite it as "technical graphene" [76].

A long time from the beginning of the graphene era, there was an opinion that chemical derivatives of graphene, mainly GO, rGO, and teflon, came into life together with graphene itself. The first breakdown was caused by discovering that natural amorphous carbon, known as shungite carbon, is a natural deposit containing a million tons of rGO [77]. Then, similar conclusions were made about the natural anthraxolite [78] and anthracite [79]. In time, it came to the industrial multi-tonnage carbon blacks as well [79-81]. Therefore, having been known for more than one-and-a-half thousand years, amorphous carbon is undergoing a rebirth and appears as agglomerative compositions of framed graphene molecules, thus becoming a special subject of modern nanotechnology. A recent extended study was devoted to a detailed investigation of the structure and chemical composition of amorphous carbons of the highest carbonization [79-82]. For the first time, reasonable models of graphene molecules, which are the basic structural units (BSUs) of the studied solids and which correspond to both their structure and chemical composition, including a definite C:O:H atom relation, were suggested. A set of selected models is shown in Figure 9. The same (5, 5) NGr molecule, which is commensurate with experimentally determined BSUs of shungite carbon, anthraxolite, and carbon black 632, was chosen as parent structure in all the cases. The choice allows drawing the main attention to the framing areas of the models without distracting from the structure of the graphene domains. As seen in the figure, BSUs of amorphous carbons belong to the class of graphene oxyhydrides, differing by the hydrogen content and chemical composition of oxygen containing groups. Bright spots on the N_{DA} distribution maps reveal the radical character of the species. Later on, the models were corrected based on IR reflection [81] and Raman scattering [82] data. The correction concerned the structure-chemical pattern of the heteroatom distribution around the pristine (5, 5) NGr molecule, keeping the relation of C:O:H components fixed and the radical character of the models conserved.

Revealing the molecular structure of amorphous carbon significantly changes our view of the world. We live on a land containing a high amount of amorphous carbon, we breathe air with a high content of combustion products of organic substances, we eat

food as polluted as air, and we drink water extracted from underground sources or rivers suffering from carbon pollution. Is it not time to ask ourselves if we realize that in most cases we are dealing with radicalized graphene molecules and that this circumstance casts doubt on our safety? Obviously, the answers concern the post-reaction existence of the radical molecules. Let us examine which answers we can get now.

Figure 9. Appearance of natural amorphous carbon (top) and equilibrium structures of molecular BSU models (middle): (a) graphene oxihydrides $C_{68}O_4H_6$ attributed to "C=O" shungite carbon, (b) $C_{64}O_4H_{10}$ of "O=C-O-C' antraxolite, (c) and (d) $C_{64}O_4H_3$ (c) and $C_{64}O_4$ (d) of "C-O-C" carbon blacks CB632 and CB624, respectively. (bottom) N_{DA} distribution over atoms of BSU model molecules (see text). UHF calculations.

7. Post-Reaction Storage of the Spin Chemistry Products

UHF calculations reveal that all the models shown in Figure 9 are radicals. Characterizing by N_D value, the molecules form a following series of data: 27.4 e (shungite carbon), 22.2 e (anthraxolite), 29.7 e (carbon black 632), and 30.9 e (carbon black 624) [81]. The quantities are quite big, evidencing strong radicalization. As seen in Figure 9, black balls of the N_{DA} portraits in the circumference areas of the molecules clearly exhibit a fully inhibited chemical ability of both heteroatoms and carbon atoms to which the former are attached. Nevertheless, the remaining part of the molecules' circumferences still remains

highly active and easily accessible to not only gaseous reagents, but to bulky ones as well, even once aggravated with sterical constrains in the latter case.

Due to high radicalization of each suggested model and since the models, in general, are fully consistent with the discussed structural-compositional characteristics of the studied ACs [81], the authors made an astonishing conclusion that sp^2 amorphous carbons are conglomerates of stable radicals. In itself, this conclusion, however unexpected it may be, is not knockdown. Currently, stable organic radicals in the form of stable tetrabenzo-Chichibabin's hydrocarbons [83], materials based on long acenes [84,85], radical polymers [86], and synthetic metals [87] occupy an increasing part of the agenda of modern chemistry. Graphene fragments were not left aside as well, as can be judged by a series of in-depth reviews of the case [88–94]. However, it is difficult to imagine that the huge amount of sp^2 amorphous carbons, both natural and engineered, as well as their exclusively broad involvement in various chemical and technical processes for more than a thousand years could not disregard such an important characteristic of the substance if it existed. Nevertheless, in fact, by now there have not been communications joining radical terminology and the vast available data concerning sp^2 amorphous carbons. At the same time, specific peculiarities concerning metal free carbocatalysis [95–106] (see a brief review of the latter state of art [107]) and electron-spin resonance [108–115] have been really observed. However, until now, they have not been connected with specific radical properties of sp^2 carbons as well. Against this background, a study [116] that voiced the term "radical" in relation to sp^2 amorphics for the first time when attempting to explain carbonaceous soot inception and growth in term of resonance-stabilized hydrocarbonradical chain reactions is quite revolutionary.

Restoration of BSUs radicals in their rights confronts us with new problems to be solved, and the first one is to understand why sp^2 carbon molecular radicals are stable. The appeal should be attributed to fullerenes and CNTs as well, the radical essence of which has been convincingly established [44]. The question of the stabilization of openshell molecules has been raised repeatedly (see reviews [23,24,89,93]). However, the time-dependent stability of molecules was determined not directly, but by a qualitative comparison of calculated thermodynamic factors [117]. The procedure was applied to molecules with terminated DBs, such as PAHs or *periacenes*. For these molecules, it was established that spin-delocalized character of the molecule radicalization, provided with the conjugation of sp^2 electrons over the total number of carbon atoms, definitely favors the stabilization. Additionally, nearly degenerated spin-triplet gap E_{ST} as well as incorporation of heteroatoms (O, N, S) inside benzenoid units or outside the latter support the stabilization as well. All these factors are typical for graphene molecules, both bare and framed, such as, say, (5, 5) NGr and *peripentacene in Figure 5* as well as semi-bare or/and semi-framed BSU molecules in Figure 9. The latter, as we know exactly, do live for a long time [79].

Another problem of these bodies concerns the real implementation of BSU structures from the available variety of possible models. The model's total energies E_{gr} evidence a potential ability only, while the nature of empirical observations concern the chemical kinetics rather than the thermodynamic stability of the products. Reaction occurrence is governed by parameters that control the interrelation between reactants and products, forming free energy basins separated by barriers of different high. One can easily imagine how complicated the picture of the basins is when one of the reactant is multi-target. Until now, a possibility to quantitatively consider the relevant problems related to the formation of, say, shungite carbon BSUs, has seemed impossible. However, the appearance of a new method, called by its authors "a multi class harmonic linear discriminant analysis" (MC-HLDA) [118], presenting metadynamics with discriminants as a tool for understanding chemistry, inspires some optimism that in the near future, similar complex problems can be solved.

The idea of a particular role of kinetics in the case of multi-target chemical compounds with highly delocalized spin density puts the time in the avant-garde row of particularly significant parameters. The chemistry of sp^2 nanocarbons requires the determination of the time of life of manufactured products. Despite the revolutionary contribution of sp^2 nanocarbons to modern chemistry, this area itself is still young, so the question of lifetime may seem premature. Nevertheless, evidence of the legitimacy of such an issue has already been obtained in synthetic chemistry. Thus, it was found that the lifetime of the simplest sp^2 radicals, which are well-known polyacenes, is different. Long-lived members of this series are naphthalene, anthracene, tetracene, and pentacene. As for longer acenes, the lifetime drastically shortens when the number of BUs increases, so that hexacene has been still observed for a short time, while the higher species cannot even be recorded as a result of chemical synthesis [24,119,120]. Synthesis of multinuclear PAHs imitating graphene molecules by Müllen's team [121] also faces the problem of sustainability of the final products. The undoubted success of the synthesis is the existence of stable graphene materials, such as mass-produced GO, rGO, and graphene quantum dots based on it. Although these materials have not been even two decades old and their temporal stability has not yet been truly investigated, the time-instability of GO has been rigidly fixed [75]; many chemists are familiar with spontaneous oxidation of fullerenes.

Besides synthetic laboratories, there is a unique natural laboratory, for which carbon is an absolute favorite. The laboratory operates in a time scale of billions (shungite carbon) and millions (anthraxolite, anthracite) of years. The time is large enough to expect that all chemical transformations, which could have happened with sp^2 carbons, already occurred. Consequently, compounds exist in size, shape, and chemical composition, which no longer change. A careful analysis of these properties allows us to highlight a number of unique characteristics of natural amorphous carbons. (1) The average BSUs size of shungite carbon, anthraxolite, and anthracite is of 1.5 nm, nondependent on the local place of deposits [75,79]. (2) The chemical composition of these mineral BSUs is similar [79]. Apparently, these factors are favorable for the radical stabilization. At the same time, the BSUs preserve their radical character, which can be opened by changing the conditions of existence and/or storage of the substances. The latter lays the foundation of particular features of shungite carbon, favoring its application in medical treatment [122], biology [123], non-linear optics [124], mechanics [125], and so on [126]. So far, anthracite and anthraxolite have not been known from this side, while many exciting discoveries can be expected.

It becomes obvious as well that the properties of shungite carbon itself and in the vicinity to other minerals should be different due to a possible activation of the radical ability of the former. Actually, any mineral nucleus is an atomic cluster covered with DBs, thus having a radical nature. The latter are saturated when stacking with other nuclei promotes the mineral growth. Obviously, the termination of the bonds by another's addends terminates the growth [38]. Let us demonstrate the said on the example of the growth of a particular quartz in the presence of shungite carbon. $(SiO_4)_{48}$ cluster in Figure 10a presents a silica nucleus, leading to the growth of α -quartz. The cluster is composed in such a way that the consequent growth can occur from the basal top plane of the cluster that accommodates nine silicon atoms with one DB each. The shungite carbon BSU molecule (Figure 10b), which appears nearby, reacts with the cluster almost barrierlessly and is bound to it by two Si-C bonds, irrespective of the initial arrangement of the reactants (Figure 10e,f). The coupling energy constitutes -139.93 and -124.35kcal/mol, respectively. Evidently, the presence of the molecule prevents from joining two silica clusters for the quartz growth to be continued. When the carbon molecule number is big, they together may form a "patchwork fabric" to cover or envelope the silica nucleus. Assuming the nucleus spherical shape, geometry allows the evaluation of the sphere radius *R*, when it is fully covered by the fabric consisting of $\sim 1.5 \times 1.5$ nm² patches, which gives the value of *R*~80–100 nm. Therefore, it is possible to expect the formation of a mineral matter consisting of peculiar "chocolate candies" with a hard silica core inside, surrounded by shungite–carbon shell.

The problem under discussion did not arise from scratch. It was stimulated by a thorough physicochemical study of conditional shungite rocks with low carbon content [127]. Such a component is always present in shungite deposits. As occurred, the mineral matter actually consists of agglomerates of close-to-spherical nanoparticles presenting a crystalline inner core of perfect α -quartz surrounded by shungite–carbon shell. The size of quartz core is of ~60–80 nm irrespectively of the deposits place. The shell can be easily separated from the core. The study of this carbon mass has revealed its full similarity to that one related to high-carbon shungite rocks. It is evident that this first observation of a particular symbiosis of shungite carbon and silica should not be the only one. It can be assumed that the discovered phenomenon, which is self consistently explained from the standpoint of spin chemistry of nanocarbons, opens a new page in the history of geology, devoting it to the spin geochemistry.

Figure 10. Equilibrium structures of $(SiO_4)_{48}$ (**a**) and $C_{66}H_6O_4$ graphene molecule (**b**) imitating α -quartz nucleus and BSU of shungite carbon, respectively. (**e**,**f**) Equilibrium structures of silica-shungite carbon composites at starting positions of the components (**c**) and (**d**), respectively. UHF calculations.

8. Conclusions

The paper presents a self-consistent overview of a selected number of the top issues related to sp^2 nanocarbons from the viewpoint of an experienced long-working user of computational quantum chemistry. sp^2 Nanocarbons are considered to be specific objects, the electronic structure features of which are presented in light of the general concept of

emergent chemical phenomena. The latter are a consequence of a quantum phase transition caused by the spin symmetry breaking due to the correlation of p_z odd electrons. This correlation depends on the distance between the odd electrons and becomes noticeable when the shortest one, defined by C=C bond length, exceeds critical value $R_{crit} = 1,400 \pm 0,005 A$. The UHF formalism clearly evidences the broken symmetry occurrence and perfectly suits self-consistent description of the issue. The UHF emergents, such as (i) open-shell character of electron spin-orbitals; (ii) splitting and/or spin polarization of electron spectrum; (iii) spin-mixed character of the ground state and, consequently, depriving the exact spin multiplicity of electronic states; as well as (iv) a pool of local spins at zero total spin density, are empirically supported and convincingly certified. They significantly expand the concept of the ground state of sp^2 nanocarbons and give a clear vision of the spin features of their chemistry as the chemistry of stable radicals. Once multitarget and spatially extended, stable radicals of sp^2 nanocarbons should be considered from the standpoint of spin-delocalized topochemistry. The latter is based on both spin density and chemical activity delocalization over molecules' atoms, on the one hand, and on selectively pronounced barriers of different reactions exhibiting topological essence of intermolecular interaction, on the other. Accordingly, sp^2 carbon radicals reveal a peculiar topokinetics that lay the foundation of their stability. The stability is time-marked, which entails the emergence of a new characteristic term in the modern chemistry of sp^2 carbons—the species lifetime. A number of examples exhibiting main traits of computational spin chemistry of fullerene C_{60} , a fragment of (4, 4) SWCNT, and a family of graphene molecules on the basis of a parent (5, 5) NGr one are presented. A perfect fitting of calculated and experimental data is discussed. Particular attention is given to graphene molecules presenting basic structure units of synthetic and natural amorphous carbons. The stable-radical character of the latter allows raising questions about spin geochemistry due to the ubiquitous presence of amorphous carbon in nature.

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Abbreviations

atomic chemical susceptibility			
broken spin symmetry			
basic structural unit			
benzenoid unit			
configuration interaction			
carbon nanotube			
dangling bonds			
density functional theory			
density matrix renormalization group			
graphene oxide			
intermolecular interaction			
molecular chemical susceptibility			
effectively unpaired electrons fraction at atom A			
total number of effectively unpaired electrons			
polyaromatic hydrocarbons			
photodynamics			

RAS-SF	restricted active space spin-flip
rGO	reduced graphene oxide
RHF	restricted Hartree-Fock
SC	spin contamination
{ <i>sp</i> ² C=C bonds}	a complete set o C=C bonds
SpD _A	spin density fraction at atom A
SpD _{tot}	total spin density
SpM	spin multiplicity
SWCNT	single walled carbon nanotube
UDFT	unrestricted density functional theory
UHF	unrestricted Hartree-Fock

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