

Article

# Theoretical Study of Pentacoordinated Lanthanide Single-Ion Magnets via Ab Initio Electronic Structure Calculation

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**Abstract:** A theoretical study, based on ab initio electronic structure calculation, is performed in a group of 16 pentacoordinate Dy-SIMs. Theoretical results provide a reasonable explanation of the observed SMM performance based on a concise criterion, i.e., the co-existence of long  $\tau_{\text{QTM}}$  and high  $U_{\text{eff}}$ . To have the desired electronic structure favoring good SMM performance, the contribution from the equatorial coordinating atoms might be even more important than that from the axial coordinating atoms. Widening the axial  $\angle\text{O-Dy-O}$  might be a probable way to improve the SMM performance of pentacoordinated Dy-SIMs. Starting from existing systems, a rigid-scan type exploration indicates the possibility of  $U_{\text{eff}}$  higher than 1600 K.

**Keywords:** single-molecule magnets; ab initio calculation; crystal field analysis; axial bond angle

## 1. Introduction

Single-molecule magnets (SMMs) refer to a type of molecular systems displaying magnet behavior at the unimolecular level [1–11]. Because of their potential to retain magnetic information in one single molecule, SMMs have gained widespread attention from researchers, especially in the field of ultra-high-density storage of data [4–9]. Compared to hard-disk drives, the information storage density using SMMs can reach to 300 Tbit in<sup>-2</sup>, which is up to 100 times higher [4,7]. Thus SMM could be the components in future revolutionary micro-electronic devices.

As research progresses, people have discovered the importance of lanthanide single-molecule magnets (Ln-SMMs) especially the mononuclear structures which are also called as lanthanide single-ion magnets (Ln-SIMs). Actually, many recent breakthroughs in the field of SMM are provided by Ln-SIMs [12–24]. However, a practical application of SMMs is still out of reach. As one important figure of merit of SMM, the blocking temperature ( $T_{\text{B}}$ ) means the highest temperature to observe blocked magnetization of a sample. Until now, the record  $T_{\text{B}}$  values of SMMs have been within 60–80 K [10,18–21]. Although they exceed the boiling point of liquid nitrogen, these records still remain far below room temperature. Thus, enhancing the performance, e.g., increasing  $T_{\text{B}}$ , is one central task in the current stage of SMM.

It is well known that the coordination environment dictates the performance of SMMs, especially in the case of Ln-SIMs. Recently reducing the coordination number (CN) has been suggested to be an effective strategy for enhancing the performance of Ln-SIMs [25]. This is because a low coordination environment can lead to high magnetic axiality, which is crucial for maintaining a preferred orientation of magnetic moment to achieve a long



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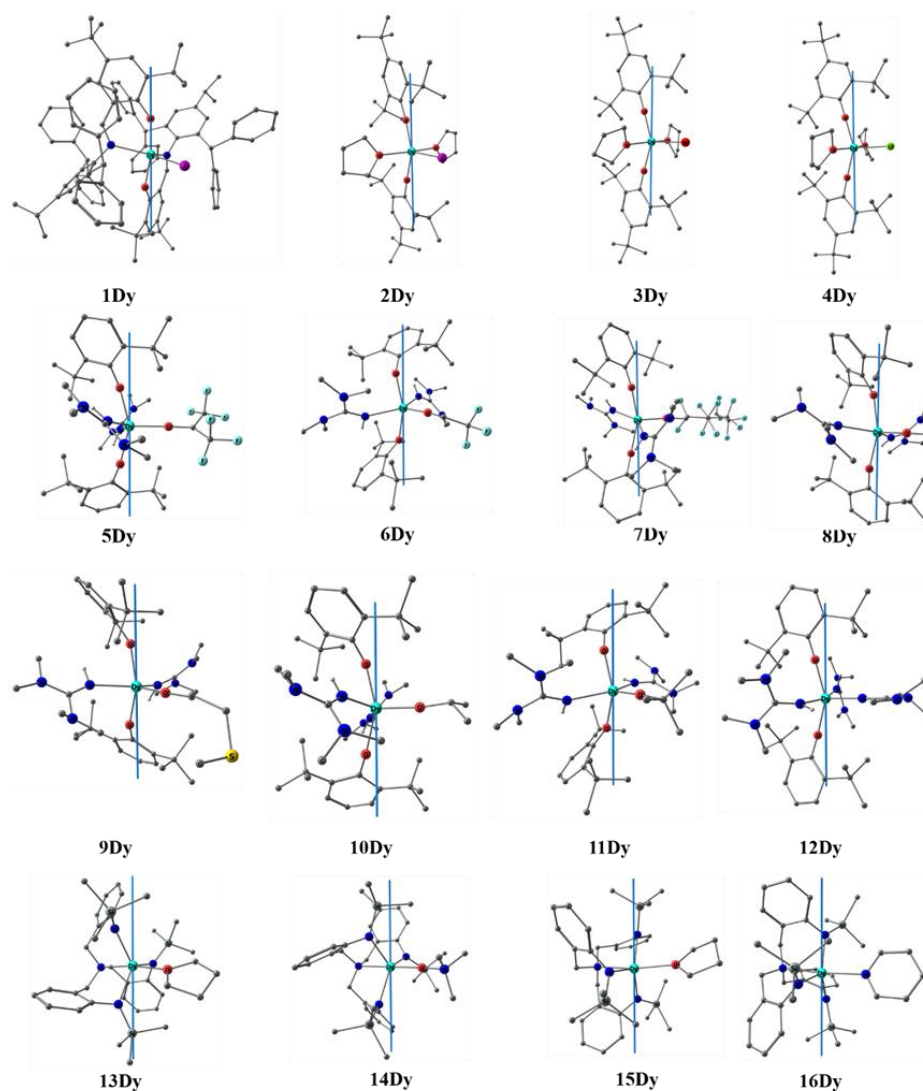
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relaxation time. Actually, the record-holding dysprosocenium SIMs just adopt sandwiched structures presenting effective/pseudo two coordination of the central ion.

However, the SMM performances of most synthesized low CN Ln-SIMs are apparently inferior to those of dysprosocenium systems. Thus, the potential of low CN structures as high-performance SMMs has not been amply realized. The search for low CN Ln-SIMs with good SMM performance needs rational guidance, especially from theoretical studies.

Recently, the SMM performance of a group of typical low CN Ln-SIMs, i.e., tetra-coordinated structures, has been well interpreted via the ab initio electronic structure calculation [26–44]. A theoretical study also indicated possible routes to improve the SMM performance and then pointed out the structures holding the possibility of  $T_B$  higher than 50 K for tetra-coordinated Ln-SIMs [39].

Encouraged by its capability, ab initio electronic structure calculation is carried out here in another typical type of low CN Ln-SIMs, i.e., the pentacoordinate complexes synthesized in recent years [45–49]. Here, we selected 16 structures as the objects of this study. For the symmetry of these 16 structures, **1Dy** to **12Dy** are close to  $D_{4d}$ , and **13Dy** to **16Dy** are close to  $D_{3d}$ . In addition to interpreting the reported systems, this work also tries to give suggestions for improving the SMM performance and to predict possible improvements (Figure 1).



**Figure 1.** The structures of all SMMs involved in the study.

## 2. Theoretical Background and Computational Details

The microscopic mechanism underlying the SMM behavior is the magnetic relaxation at the molecular level. Due to the co-existence of several relaxation pathways, a comprehensive magnetic relaxation treatment needs to include the characteristics of the electronic and vibrational states, the coupling between them and the interaction between the system and the environment. Sophisticated methods to accomplish this task have been proposed by several groups [50–52]. However, for this type of method, huge computational cost is hardly avoidable.

Recently, a concise criterion for good SMM has been proposed to be the co-existence of long quantum tunneling of magnetization (QTM) time  $\tau_{\text{QTM}}$  and a high effective barrier of magnetic reversal  $U_{\text{eff}}$  [39–43]. For Ln-SIMs, both  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$  can be obtained from one single ab initio calculation for a given system. Thus, the application of this criterion is easy for a large number of Ln-SIMs due to its low computational cost [53–55]. The reliability of this criterion has been verified in structurally similar systems, e.g., tetracoordinated Ln-SIMs and square antiprism ones [39,40].

$$\tau_{\text{QTM}}^{-1} = \frac{\beta B_{\text{ave}}}{h} \cdot \frac{g_{\text{XY}}^2}{2(g_{\text{XY}}^2 + g_{\text{Z}}^2)^{\frac{1}{2}}}, \quad g_{\text{XY}} = \sqrt{g_{\text{X}}^2 + g_{\text{Y}}^2} \quad (1)$$

$$\tau_{\text{QTM}}^{-1} = \frac{\beta B_{\text{ave}}}{h} \cdot \frac{1}{2} \cdot \frac{x_{\text{aniso}}^2 g_{\text{XY}}^2}{\sqrt{x_{\text{aniso}}^2 g_{\text{XY}}^2 + (3 - 2x_{\text{aniso}}^2) g_{\text{Z}}^2}} \quad (2)$$

$$x_{\text{aniso}} = \frac{B_{\text{trans}}}{B_{\text{ave}}}, \quad B_{\text{X}} = B_{\text{Y}} = B_{\text{trans}} \quad (3)$$

The systems studied here are all Kramers SIMs of which the zero-field QTM rate  $\tau_{\text{QTM}}^{-1}$ , i.e., the reciprocal of  $\tau_{\text{QTM}}$ , is calculated by Equation (1).  $\beta$  and  $h$  in Equation (1) are the Bohr magneton and Planck constant, respectively. The principal g-factors, i.e.,  $g_{\text{X-Z}}$ , of the ground Kramers doublet (KD) in Equation (1) are obtained from ab initio calculation.  $B_{\text{ave}}$  in Equation (1) is the averaged strength of the internal magnetic field which is empirically estimated as 20 milli Tesla (mT) here. The reliability of this selection has been proved in our previous works [39,41,42]. For field-induced systems, another parameter  $x_{\text{aniso}}$ , describing the anisotropy of the magnetic field, is needed as shown in Equations (2) and (3). Here, the applied direct current (DC) field is assumed to be added in the Z principal direction. In this case,  $B_{\text{X}} = B_{\text{Y}} = 20$  mT and  $B_{\text{Z}}$  is the sum of 20 mT and the applied DC field in experiment.

$$U_{\text{eff}}(T) = \sum_i \frac{\tau_{\text{QTM},i}^{-1,\text{eff}}(T)}{N} E_i \quad (4)$$

$$N = \sum_i \tau_{\text{QTM},i}^{-1,\text{eff}}(T) \quad (5)$$

$U_{\text{eff}}$  could be calculated as a weighted sum of energies of both ground and excited KDs (Equation (4)) [41,42]. The normalization factor  $N$  is the sum of the effective QTM rates of all the involved KDs (Equation (5)). The effective rate of the  $i$ th KD (Equation (6)) depends on its principal g-factors (Equation (7)) and the Boltzmann population (Equation (8)).

In this work, theoretical predictions of QTM time via Equations (1)–(3) and effective barrier via Equations (4)–(5) are labeled as  $\tau_{\text{QTM}}^{\text{Zee}}$  and  $U_{\text{eff}}^{\text{Zee}}$  respectively. The corresponding experimental results are labeled as  $\tau_{\text{QTM}}^{\text{exp}}$  and  $U_{\text{eff}}^{\text{exp}}$  respectively.

$$\tau_{\text{QTM},i}^{-1}(T) \propto \frac{\exp(-E_i/k_B T)}{Z} \tau_{\text{QTM},i}^{-1,\text{eff}} \quad (6)$$

$$\tau_{\text{QTM},i}^{-1,\text{eff}} = \frac{g_{XY,i}^2}{2(g_{XY,i}^2 + g_{Z,i}^2)^{\frac{1}{2}}} \quad (7)$$

$$Z = \sum_i \exp(-E_i/k_B T) \quad (8)$$

The ab initio calculations in this work consist of two steps: first, a set of spin eigenstates are obtained via the state-averaged complete active space self-consistent field method (SA-CASSCF) [56]; then, the final states, i.e., KDs here, are obtained via state interaction which diagonalizes the spin-orbit-coupling (SOC) matrix under the basis of spin eigenstates from the first step.

A free academic version of MOLCAS 8.0 was used to perform ab initio calculation [57]. The active space consisted of 9 electrons in 7 orbitals and 21 spin sextets were included in the SA-CASSCF step [39–43]. The scalar relativistic effect was accounted via DKH2 transformation. Then, state interaction was performed via the RASSI-SO module [58], with the SOC integrals from the AMFI method [59]. We choose the ANO-RCC relativistic basis set [60,61], including VQZP for Dy, VDZP for C, VDZ for H and VTZP for the others. The SINGLE\_ANISO module was used to gain the g-factors and other magnetic parameters [62,63]. The numerical results of the ab initio calculation are included in Tables S1~S16.

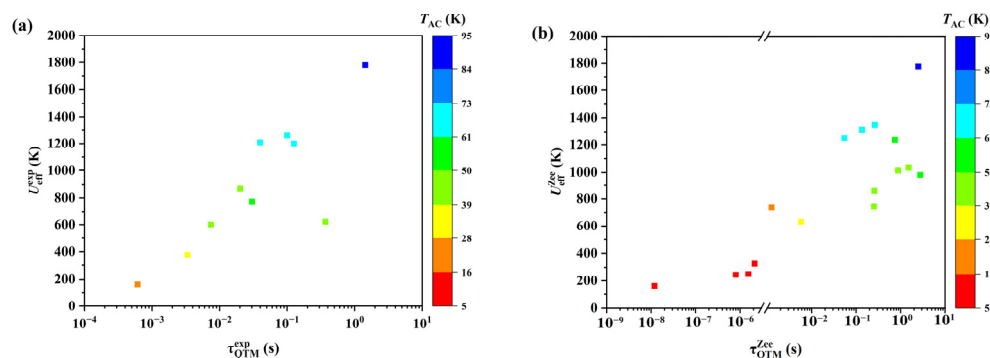
### 3. Results and Discussion

#### 3.1. The Comparison Between Theoretical Predictions and Experimental Results

The most quoted evidence for SMM characteristics is the temperature- or frequency-dependence of the imaginary part of the alternating-current (AC) magnetic susceptibility, especially a peak. The highest temperature to observe such a peak is labeled as  $T_{AC}$  here.  $T_{AC}$  only represents the short-term magnetic memory effect and thus is less conceptually sound than a magnetic hysteresis loop or zero-field cooled susceptibility. However,  $T_{AC}$  is available for most SMMs, including all the Dy-SIMs studied here. In comparison, neither magnetic hysteresis nor zero-field cooled susceptibility holds such an availability.  $T_{AC}$  has been used to quantify  $T_B$  for a lot of SMMs [9]. Our recent works have also verified the capability of  $T_{AC}$  as a common measurement of SMM performance [42,64]. Thus,  $T_{AC}$  at 1000 Hz is utilized here.

As shown in Figure 2, higher  $T_{AC}$  is generally located at a position closer to the lower right corner of the plane defined by  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$ . This corner just corresponds to both the longest  $\tau_{\text{QTM}}$  and the highest  $U_{\text{eff}}$ . **1Dy**, which holds the highest  $T_{AC}$  here, has both the longest  $\tau_{\text{QTM}}$  and the highest  $U_{\text{eff}}$  according to either theoretical prediction or experimental results (Table 1). Thus, the co-existence of longer  $\tau_{\text{QTM}}$  and higher  $U_{\text{eff}}$  does correspond to better SMM performance in the pentacoordinated Ln-SIMs. The proposed criterion also works here.

Formally, this criterion only includes the QTM and thermally-activated (TA) pathways, i.e., Orbach and TA-QTM, but neglects Raman pathway. Thus, in principle, it is only necessary rather than sufficient. However, one recent in-depth statistical analysis has indicated the existence of a correlation between  $U_{\text{eff}}$  and Raman parameters, especially in high  $U_{\text{eff}}$  cases [9]. Thus, when applying the criterion, the effect of the Raman pathway might be accounted implicitly. Also, in structurally similar systems, the effect of the Raman pathway might not vary sharply [39,40].



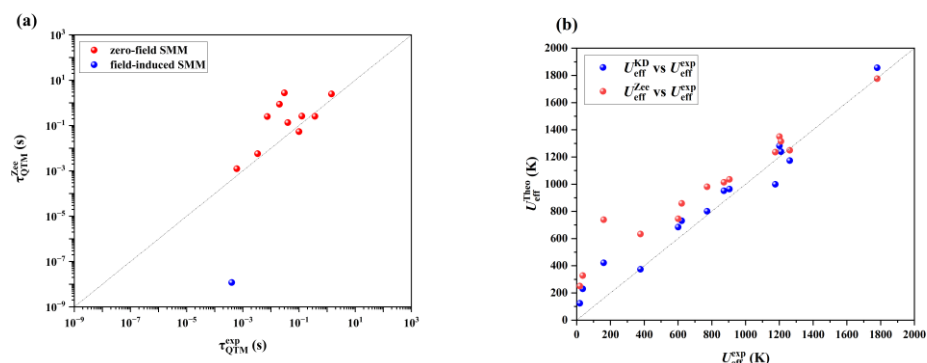
**Figure 2.** The relation among  $T_{AC}$ ,  $\tau_{QTM}$  and  $U_{eff}$ . (a)  $T_{AC}$  vs. experimental  $\tau_{QTM}$  and  $U_{eff}$ . (b)  $T_{AC}$  vs. theoretical  $\tau_{QTM}$  and  $U_{eff}$ .

**Table 1.** The experiment values and theoretical predictions of  $\tau_{QTM}$  (s) and  $U_{eff}$  (K).

	Refcode	$\tau_{QTM}^{exp}$	$\tau_{QTM}^{Zee}$	$U_{eff}^{exp}$	$U_{eff}^{Zee}/U_{eff}^{KD}$	$T_{AC}$ <sup>a</sup>
1Dy	LEVLEH	1.43	2.49	1780	1776/1856	95
2Dy	XUWDAX	$1.26 \times 10^{-1}$	$2.62 \times 10^{-1}$	1201	1350/1282	64
3Dy	XUWCUCQ	$3.98 \times 10^{-2}$	$1.35 \times 10^{-1}$	1210	1315/1239	64
4Dy	XUWCOK	$1.00 \times 10^{-1}$	$5.42 \times 10^{-2}$	1262	1249/1173	64
5Dy	ENACOO	N/A <sup>b</sup>	$7.41 \times 10^{-1}$	1176	1236/999	60
6Dy	ENACII	N/A	1.51	905	1035/964	49
7Dy	ENACUU	$2.02 \times 10^{-2}$	$8.77 \times 10^{-1}$	872	1014/951	41
8Dy	ENABON	$3.02 \times 10^{-2}$	2.77	773	981/801	50
9Dy	ZESGAJ	$3.68 \times 10^{-1}$	$2.56 \times 10^{-1}$	622	859/731	45
10Dy	E.NACAA	$7.45 \times 10^{-3}$	$2.51 \times 10^{-1}$	601	745/684	40
11Dy	ENACEE	$3.35 \times 10^{-3}$	$5.75 \times 10^{-3}$	378	633/374	33
12Dy	ENABIH	$6.11 \times 10^{-4}$	$1.25 \times 10^{-3}$	160	738/422	22
13Dy	DEYRIO	N/A	$2.12 \times 10^{-6}$	36	328/230	6
14Dy	FEYREK	N/A	$1.53 \times 10^{-6}$	19	250/124	5
15Dy	DEYRIO	N/A	$8.00 \times 10^{-7}$	N/A	245/0	6
16Dy	FEYRAG	$4.03 \times 10^{-4}$	$1.19 \times 10^{-8}$	N/A	160/0	6

<sup>a</sup> The highest AC frequency is usually 1000 Hz, the exception is **9Dy** (1488 Hz). <sup>b</sup> Data were not provided by experiments.

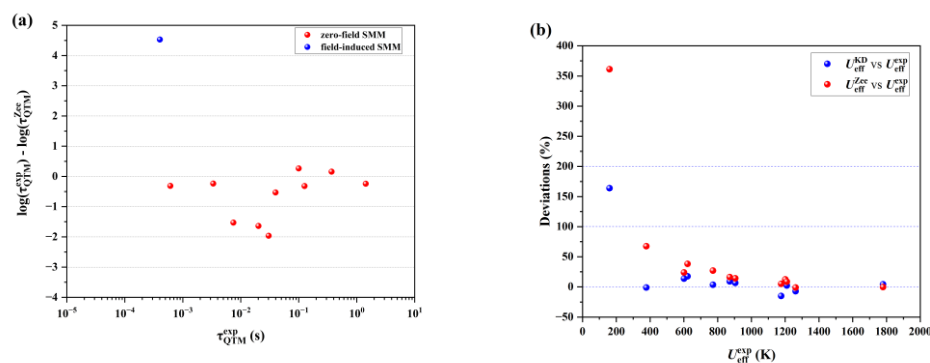
As shown in Figure 3, the order of either  $\tau_{QTM}^{Zee}$  or  $U_{eff}^{Zee}$  is generally consistent to that of the corresponding experimental  $\tau_{QTM}^{exp}$  and  $U_{eff}^{exp}$  respectively. With only one exception of **16Dy**, the deviations in  $\tau_{QTM}^{Zee}$  are all less than two orders of magnitude (Figure 3a). For the SIMs holding the first four longest  $\tau_{QTM}^{exp}$  here, i.e., **1Dy–4Dy**, the deviations in  $\tau_{QTM}^{Zee}$  are all less than one order of magnitude. It needs to indicate that even the theoretical results from those sophisticated methods may still bear deviations of one or two orders of magnitude [53]. The large deviation in  $\tau_{QTM}^{Zee}$  of field-induced **16Dy** might be attributed to the difficulty of obtaining accurate  $\chi_{aniso}$  [43]. As a vector field, magnetic fields have different sources, e.g., dipolar interaction with other electronic magnetic moment in the sample and hyperfine interaction due to nuclear spin [43]. Thus, the anisotropy of a magnetic field depends on both the electronic and nuclear contributions.



**Figure 3.** Comparison between theoretical prediction and experimental fitting. (a)  $\tau_{QTM}^{Zee}$  vs.  $\tau_{QTM}^{exp}$ . (b)  $U_{eff}^{Zee}$  vs.  $U_{eff}^{exp}$ .

In the aspect of effective barrier, we do find some large discrepancies between theoretical  $U_{eff}^{Zee}$  and experimental  $U_{eff}^{exp}$ , i.e., **11Dy–16Dy**. Their  $T_{AC}$  values are around 20 K or apparently lower (5~6 K) while other Ln-SIMs have  $T_{AC}$  values lying within the range of 40~95 K. Therefore, those large discrepancies mainly occur in systems holding inferior SMM performance as represented by low  $T_{AC}$ . In these inferior systems, pure dominance of the Orbach pathway is hardly possible and other pathways strongly drive the fitted  $U_{eff}^{exp}$  away from having a solid physical meaning [40]. Thus, in these systems,  $U_{eff}^{exp}$  becomes closer to a purely phenomenological parameter and  $U_{eff}^{Zee}$  is not obligated to be close to it [40].

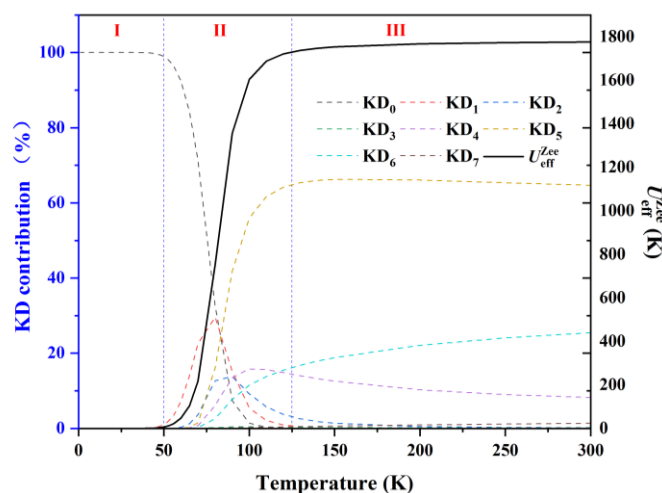
Besides  $U_{eff}^{Zee}$ , we can also calculate  $U_{eff}$  as the energy of a given excited KD, identified as the most probable one wherein magnetic reversal takes place. This theoretical  $U_{eff}$  is labeled as  $U_{eff}^{KD}$  here after (Table S17 and Figure S1). As shown in Figure 4b, these two types of theoretical barrier are generally consistent with each other. They both identify that the barrier of **1Dy** is clearly higher than those of all the others.



**Figure 4.** The deviations in  $\tau_{QTM}^{Zee}$  and  $U_{eff}^{Zee}$  compared to experimental results. (a) Order-of-magnitude deviation in  $\tau_{QTM}^{Zee}$ . (b) percentage deviation in  $U_{eff}^{Zee}$ .

### 3.2. Mechanisms of Magnetic Relaxation

According to Equation (4),  $U_{eff}^{Zee}$  can be decomposed into contributions from various KDs (Figure 5). This decomposition is capable of providing some mechanistic information about the magnetic relaxation. Since  $U_{eff}^{Zee}$  varies with the temperature value used in the calculation, two cases are analyzed for one Ln-SIM: the saturated case and the reproducing case [64]. The saturated case refers to the result when  $U_{eff}^{Zee}$  becomes a saturated value which is obtained by using 300 K in Equation (4). The reproducing case refers to the result when  $U_{eff}^{Zee}$  exactly reproduces  $U_{eff}^{exp}$  with a special temperature value  $T_{rep}$  used in Equation (4). It needs to be clarified that there is no direct relationship between  $T_{rep}$  and  $T_B$  in principle.



**Figure 5.**  $U_{\text{eff}}^{\text{Zee}}$  and the contributions from various KDs of **1Dy**.

As shown in Table 2, the most important KDs of the saturated  $U_{\text{eff}}^{\text{Zee}}$  of **1Dy** are  $\text{KD}_5$  and  $\text{KD}_6$ , of which the sum contribution is 91%. These two KDs remain to be the most important ones (68%) in the reproducing case while  $\text{KD}_4$  (16%) also plays a role. Thus, the most important KDs of  $U_{\text{eff}}$  of **1Dy** are some highly excited ones which do not change heavily between the saturated case and the reproducing case. The contributions from the ground and other lower excited KDs are negligible. These results suggest that, in **1Dy**, the slow thermally-activated relaxation, proceeding mainly via  $\text{KD}_5$  and  $\text{KD}_6$ , is important while the ground KD QTM is not efficient. This is consistent to the long  $\tau_{\text{QTM}}$  and high  $U_{\text{eff}}$  and  $T_{\text{AC}}$  of **1Dy**. Similar results occur in **2Dy–5Dy**.

**Table 2.** The contributions of various KDs to  $U_{\text{eff}}$  in the saturated and reproducing cases.

	Saturated Case	Reproducing Case	$T_{\text{rep}}$
<b>1Dy</b>	$\text{KD}_5 + \text{KD}_6$ (91%)	$\text{KD}_5 + \text{KD}_6$ (68%), $\text{KD}_4$ (16%)	100 <sup>a</sup>
<b>2Dy</b>	$\text{KD}_3 + \text{KD}_4$ (97%)	$\text{KD}_4 + \text{KD}_3$ (82%)	79
<b>3Dy</b>	$\text{KD}_3 + \text{KD}_4$ (95%)	$\text{KD}_3 + \text{KD}_4$ (77%), $\text{KD}_2$ (21%)	86
<b>4Dy</b>	$\text{KD}_3 + \text{KD}_4$ (96%)	$\text{KD}_3 + \text{KD}_4$ (86%)	90 <sup>a</sup>
<b>5Dy</b>	$\text{KD}_4 + \text{KD}_5 + \text{KD}_6$ (79%)	$\text{KD}_4 + \text{KD}_5 + \text{KD}_6$ (75%), $\text{KD}_3$ (15%)	160
<b>6Dy</b>	$\text{KD}_3$ (38%) + $\text{KD}_5$ (36%) + $\text{KD}_4$ (18%)	$\text{KD}_3$ (47%) + $\text{KD}_0$ (28%) + $\text{KD}_2$ (11%)	49
<b>7Dy</b>	$\text{KD}_4$ (53%) + $\text{KD}_5$ (28%) + $\text{KD}_6$ (16%)	$\text{KD}_4$ (62%) + $\text{KD}_1$ (9%) + $\text{KD}_5$ (8%)	56
<b>8Dy</b>	$\text{KD}_3$ (42%) + $\text{KD}_5$ (38%) + $\text{KD}_4$ (12%)	$\text{KD}_3$ (52%) + $\text{KD}_2$ (19%) + $\text{KD}_0$ (13%)	48
<b>9Dy</b>	$\text{KD}_5$ (40%) + $\text{KD}_3$ (38%) + $\text{KD}_2$ (15%)	$\text{KD}_2$ (48%) + $\text{KD}_3$ (25%) + $\text{KD}_0$ (18%)	44
<b>10Dy</b>	$\text{KD}_2$ (46%) + $\text{KD}_3$ (35%) + $\text{KD}_4$ (18%)	$\text{KD}_2$ (71%) + $\text{KD}_0$ (15%) + $\text{KD}_3$ (12%)	38
<b>11Dy</b>	$\text{KD}_3$ (53%) + $\text{KD}_2$ (43%)	$\text{KD}_2$ (54%) + $\text{KD}_0$ (25%) + $\text{KD}_3$ (12%)	40
<b>12Dy</b>	$\text{KD}_3$ (52%) + $\text{KD}_2$ (16%) + $\text{KD}_7$ (12%)	$\text{KD}_0$ (74%) + $\text{KD}_3$ (13%)	42
<b>13Dy</b>	$\text{KD}_2$ (48%) + $\text{KD}_1$ (39%) + $\text{KD}_3$ (10%)	$\text{KD}_0$ (83%) + $\text{KD}_1$ (16%)	31
<b>14Dy</b>	$\text{KD}_3$ (66%) + $\text{KD}_4$ (14%)	$\text{KD}_0$ (86%) + $\text{KD}_1$ (13%)	23
<b>15Dy</b>	$\text{KD}_1$ (70%) + $\text{KD}_2$ (21%)	N/A <sup>b</sup>	N/A
<b>16Dy</b>	$\text{KD}_1$ (44%) + $\text{KD}_2$ (30%) + $\text{KD}_0$ (16%)	N/A	N/A

<sup>a</sup> In these cases, the saturated theoretical barrier is still a little bit lower than the experimentally fitted one. Thus,  $T_{\text{rep}}$  in these cases is taken as the temperature at 2/3 position of region II. <sup>b</sup>  $U_{\text{eff}}^{\text{exp}}$  were not provided by experiments.

For other Ln-SIMs'  $U_{\text{eff}}$ , the contributions from the lower excited KDs and even the ground  $\text{KD}_0$  are more important. In some reproducing cases, i.e., **12Dy–14Dy**,  $\text{KD}_0$  even becomes the most important one. These results support a smaller contribution from slow thermally activated relaxation and a larger contribution from fast ground KD QTM. This is consistent with their inferior SMM performance as represented by lower  $T_{\text{AC}}$  when compared to **1Dy–5Dy**.

### 3.3. Crystal-Field Analysis and Theoretical Magneto-Structural Correlation

Since 20 mT  $B_{\text{ave}}$  is used for most Ln-SIMs here, their SMM performance ought to be mainly dictated by the principal g-factors and energies of the KDs. These are all determined by the electronic structure. The crystal field (CF) Hamiltonian (Equation (9)) is a suitable theoretical tool for interpreting the electronic structure of Ln-SIMs. Since  $O_k^q$  are common operators, the electronic structure characteristics arise solely from the CF parameter (CFP)  $B_k^q$  [11,30,41,65].

Accurate CFPs could be extracted from ab initio results via irreducible tensor operator (ITO). The point charge electrostatic model (PCEM) can also help to give a rough estimate of CFPs as a sum of contributions from the coordinating atoms (Equation (10)) [65].  $Z_{\text{eff}}$  and  $R_j$  in Equation (10) are the effective charge and distance to the central ion of a given coordinating atom  $j$  respectively.  $Y_k^q$  is the spherical harmonic function of which the variables are azimuthal coordinates  $\theta_j$  and  $\phi_j$  of the coordinating atoms.

$$\hat{H}_{\text{CF}} = \sum_{k=2,4,6} \sum_{q=-k}^k B_k^q \hat{O}_k^q(\hat{J}) \quad (9)$$

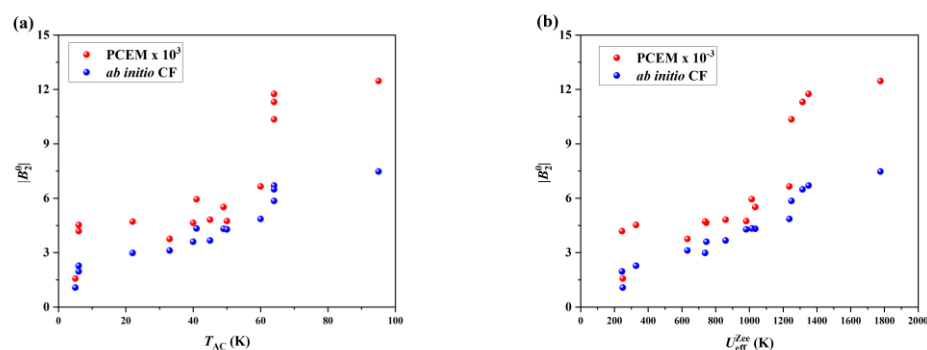
$$|B_k^q| \sim \sum_j^{\text{ligand}} \left\{ \frac{Z_{\text{eff},j}}{R_j^{k+1}} Y_k^q(\theta_j, \phi_j) \right\} \quad (10)$$

It must be clarified that Equation (10) only provides a rough estimate of the relative magnitude of CFPs rather than the actual value. The PCEM estimate does not even have the unit of energy. It also neglects the covalent contribution which has been shown to be capable of playing an important role recently [66,67]. However, there are some advantages of the PCEM estimate. First, as it is related to the position and charge of the coordinating atoms, it is chemically intuitive [39–41]. Second, it can help measuring the importance of different coordinating atoms since it is a sum of atomic contributions.

In principle, CFPs up to at least  $k = 6$  need to be included. However, recent works have indicated that 2nd-rank CFPs, especially the diagonal term  $B_2^0$ , can be the leading ones to give a reasonable explanation by themselves [64]. All the ITO  $B_2^0$  are negative and hence we only need to discuss their magnitude, as indicated by their absolute values  $|B_2^0|$ .

As shown in Figure 6, a larger  $|B_2^0|$  usually corresponds to higher  $T_{\text{AC}}$  or  $U_{\text{eff}}$ . The best SMM here, **1Dy** ( $T_{\text{AC}} = 95$  K), holds the largest  $|B_2^0|$  (Table S18). **2Dy–4Dy** also have a high  $T_{\text{AC}}$  (86 K) and their  $|B_2^0|$  values, are slightly smaller than that of **1Dy** but clearly larger than all the others. Although being less accurate, the PCEM estimate also captures the general trend (Figure 6 and Table S18) and thus subsequent PCEM analysis should be reliable.





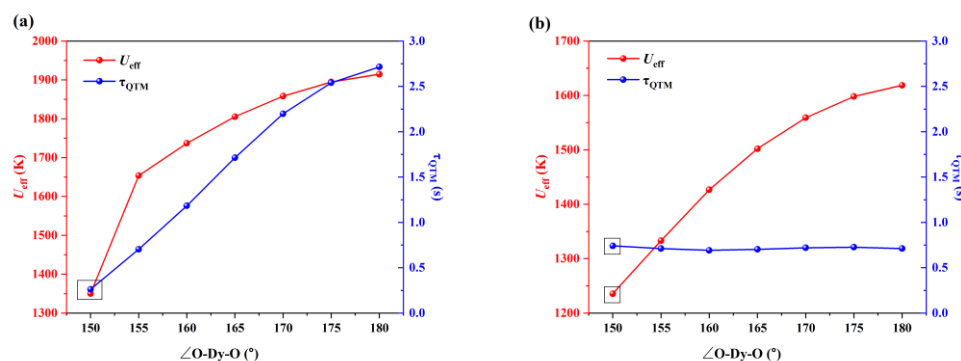
**Figure 6.** Crystal field analysis based on both ab initio ITO and PCEM. (a)  $T_{AC}$  vs.  $|B_2^0|$  in the studied systems. (b)  $U_{eff}^{Zee}$  vs.  $|B_2^0|$  in the studied systems.

Based on their positions with respect to the magnetic easy axis, the coordinating atoms could be divided into two types: the axial ones lying close to the easy axis and the equatorial ones perpendicular to the easy axis (Table S20) [65]. PCEM suggests that the contribution from axial atoms tends to increase  $|B_2^0|$  while that from equatorial atoms is destructive.

**1Dy** holds the largest PCEM estimate of  $|B_2^0|$  but its contribution from the two axial atoms is even smaller than that of **2Dy** (Table S20). Interestingly the amount of destructive contribution from the equatorial atoms of **1Dy** ( $-4.45 \times 10^{-3}$ ) is clearly smaller than that of **2Dy** ( $-5.39 \times 10^{-3}$ ). This smaller destructive contribution is one important reason for the largest PCEM estimate of  $|B_2^0|$  of **1Dy**. Although **3Dy** has the largest constructive contribution to  $|B_2^0|$  from the axial coordinating atoms (Table S20), its destructive contribution from equatorial atoms is also larger than that of **1Dy**. Thus, the eventual  $|B_2^0|$  of **3Dy** is smaller than that of **1Dy**.

For the Dy-SIMs studied here, the bond angle between the central Ln ion and two axial atoms is around  $150^\circ$ . A previous study of tetracoordinated Ln-SIMs has indicated that widening this angle can improve the SMM performance significantly [39]. Linear or quasi-linear O–Dy–O arrangement will facilitate the generation of high magnetic axiality due to the oblate shape of the electron density of the ground state of the central Dy<sup>III</sup> ion. This widening might be made possible by applying pressure [68]. The two axial O atoms of **1Dy** come from the same bidentate ligand HL (2-((2,6-dibenzhydryl-4-isopropylphenylimino)methyl)-4,6-di-*tert*-butylphenol) and thus widening of the axial bond angle is probably restricted there. Consequently, we chose to explore **2Dy** and **5Dy** wherein only monodentate ligands were involved. This exploration was performed in a rigid-scan way wherein only the axial bond angle is varied. Clearly this rigid-scan exploration has limited precision, and the results only provide some possibility. However, the capability of rigid-scan has already been verified in our recent work on Ln-SIMs [39].

As show in Figure 7, widening  $\angle O-Dy-O$  up to  $180^\circ$  can lead to an increase in  $\tau_{QTM}$  by one order of magnitude, i.e., from around 0.25 s to around 2.75 s. Meanwhile,  $U_{eff}$  also experiences a sharp increase by about 600 K, from  $\sim 1300$  K ( $150^\circ$ ) to  $\sim 1900$  K ( $180^\circ$ ). For **5Dy**, there is no significant change in  $\tau_{QTM}$  with widening  $\angle O-Dy-O$ . Meanwhile,  $U_{eff}$  increases by about 400 K from around 1200 K ( $150^\circ$ ) to around 1600 K ( $180^\circ$ ). Thus, starting from the reported pentacoordinated Ln-SIMs, widening the axial bond angle might be a probable way to improve the SMM performance.



**Figure 7.** Theoretical prediction of two structures in a rigid-scan way. (a)  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$  along  $\angle\text{O-Dy-O}$  of 2Dy. (b)  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$  along  $\angle\text{O-Dy-O}$  of 5Dy.

#### 4. Conclusions

A theoretical study, based on ab initio electronic structure calculation, was carried out in a group of 16 pentacoordinate Dy-SIMs. The experimentally observed SMM performance is well explained by a concise criterion, i.e., the co-existence of  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$ .

Crystal field analysis indicated that 2nd-rank CFPs, especially the diagonal term  $B_2^0$ , are the leading ones to generate the desired electronic structure favoring good SMM performance. To have the needed CFPs, the contribution from the equatorial coordinating atoms might be even more important than that from the axial coordinating atoms.

Widening the axial bond angle between the central Ln ion and two axial atoms might be a probable way to improve the SMM performance of pentacoordinated Ln-SIMs. Starting from existing systems, a rigid-scan type exploration indicates the possibility of  $U_{\text{eff}}$  higher than 1600 K.

**Supplementary Materials:** The following supporting information can be downloaded at: <https://www.mdpi.com/article/10.3390/magnetochemistry11010003/s1>, Table S1. ab initio results of 1Dy (LEVLEH); Table S2. ab initio results of 2Dy (XUWDAX); Table S3. ab initio results of 3Dy (XUWCUQ); Table S4. ab initio results of 4Dy (XUWCOK); Table S5. ab initio results of 5Dy (ENACII); Table S6. ab initio results of 6Dy (ENACII); Table S7. ab initio results of 7Dy (ENACUU); Table S8. ab initio results of 8Dy (ENABON); Table S9. ab initio results of 9Dy (ZESGAJ); Table S10. ab initio results of 10Dy (ENACAA); Table S11. ab initio results of 11Dy (ENACEE); Table S12. ab initio results of 12Dy (ENABIH); Table S13. ab initio results of 13Dy (DEYRIO); Table S14. ab initio results of 14Dy (FEYREK); Table S15. ab initio results of 15Dy (DEYRIO); Table S16. ab initio results of 16Dy (FEYRAG); Table S17. Various  $U_{\text{eff}}^{\text{KD}}$  values according to transition magnetic moment  $|\mu|$ , angle of easy axis of excited KD with respect to that of ground KD ( $\theta$ ) and crystal field wave function composition; Table S18. ab initio and PCEM crystal field parameters (in  $\text{cm}^{-1}$  and a.u. respectively) of Dy-SIMs<sup>a</sup>; Table S19. The distance R to Dy<sup>3+</sup> (in Å), atomic charge  $Z_{\text{eff}}$  (in  $|e|$ ) and angle  $\theta$ ,  $\phi$  with respect to the ab initio magnetic easy axis (in °) of atoms in the first sphere; Table S20. The average distance R to Dy<sup>3+</sup> (in Å), average atomic charge  $Z_{\text{eff}}$  (in  $|e|$ ), average angle  $\theta$  with respect to the ab initio magnetic easy axis (in °) and contribution to  $|B_2^0|$  from the atoms in the first sphere; Table S21. Theoretical prediction of 2Dy  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$  with different  $\angle\text{O-Dy-O}$ ; Table S22. Theoretical prediction of 5Dy  $\tau_{\text{QTM}}$  and  $U_{\text{eff}}$  with different  $\angle\text{O-Dy-O}$ ; Table S23. Cartesian coordinates of complexes; Figure S1. Possible relaxation mechanism based on transition magnetic moment for the Ln-SIMs studied here; Figure S2.  $U_{\text{eff}}^{\text{Zee}}$  and the contributions from various KDs of other SIMs.

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