



# Article Effect of Oxygen Annealing Atmosphere on Structural, Electrical and Energy Storage Properties of Bi<sub>0.5</sub>Na<sub>0.5</sub>TiO<sub>3</sub> Polycrystalline Thin Film

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**Abstract:** Bismuth sodium titanate (BNT) thin films were deposited on Pt/SiN substrates by Sol-Gel spin coating technique and annealed under  $O_2$  atmosphere. The microstructural, structural, and electrical properties of the obtained film were investigated. Electron microscopy scans and atomic force microscopy micrographs were used to analyze the microstructure of the films. Furthermore, energy-dispersive X-ray spectroscopy (EDX) analysis revealed a Na-deficient composition for the obtained film. X-ray diffraction and Raman spectroscopy allowed the identification of a pure perovskite BNT phase. Dielectric, ferroelectric, and leakage current measurements revealed good frequency stability of the dielectric constant and dielectric losses for BNT thin film. The results are discussed in terms of Na deficiency effects on the defect structure of BNT. Further, the film showed attractive electrostatic energy storage properties with energy density that exceeds 1.04 J/cm<sup>3</sup> under E = 630 kV/cm.

Keywords: BNT thin film; X-ray diffraction; AFM; Raman spectroscopy; energy storage

## 1. Introduction

The active use of sustainable energy sources, such as wind and solar, is a pressing need and a major challenge today. This need has been especially triggered by environmental concerns. The typical approach is to develop energy storage devices that provide energy on demand. Numerous energy storage systems have been developed and proposed for various applications, including mechanical, electrochemical, thermal, or electrical energy storage applications. Particularly, lithium/sodium ion batteries and electrochemical supercapacitors have been widely developed as solutions to store electricity because they show a very high energy storage density. Nonetheless, these electrochemical devices are prone to low power output. Ferroelectric/antiferroelectric materials are a viable option for high energy density ceramic capacitors, offering a great potential for electrostatic energy storage. In this perspective, much interest is devoted to environmentally friendly perovskites as potential candidates to replace  $Pb(Zr,Ti)O_3$  (PZT) [1,2] and PMN-PT [3], which are known for their toxicity. The use of these harmful compounds is now restricted by universal legislations, such as the European Directive 2011/65/EU 2011. Among the lead-free materials of interest, Bi<sub>0.5</sub>Na<sub>0.5</sub>TiO<sub>3</sub> (BNT) has emerged as one of the most promising candidates and has witnessed amazing research activity in recent years. This particular interest can be explained by considering the similarity between  $Bi^{3+}$  and  $Pb^{2+}$ . Both have stereochemically active lone electron pairs ( $6 s^2$ ) that are expected to contribute to the improvement of the ferroelectric and piezoelectric properties. An interesting piezoelectric coefficient of 73 pC/N with a high polarization (38  $\mu$ C/cm<sup>2</sup>) and a high Curie temperature of around



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/).  $325 \,^{\circ}C$  [4,5] were reported in the literature for BNT ceramics. Promising properties for this compound have also been evidenced, such as an abnormal electrocaloric effect [6] or an interesting energy storage density [7–9].

However, BNT also has some disadvantages such as a large coercive field (Ec = 73 kV/cm) and, most importantly, high leakage currents [10–12]. In fact, these disadvantages can be ascribed in part to the defect chemistry in BNT, which is related to different mechanisms. Bi vacancies may form due to the volatility of bismuth oxide, which induces the formation of oxygen vacancies for compensation. Volatility of Na<sub>2</sub>O is also expected and can induce A-vacancy.

Moreover, the A site of the BNT compound contains Na<sup>+</sup> and Bi<sup>3+</sup> with close ionic radii  $[r(Na^+) = 1.18 \text{ Å}, r(Bi^{3+}) = 1.17 \text{ Å}]$  [13] but the charge difference between these two cations favors their disordered arrangement in the matrix. Henceforth, a plethora of works reported difficulties to polarize bismuth sodium titanate ceramics due to the high electrical conductivity [14]. Therefore, efforts have been directed towards the fabrication of thin films. In this context, the growth of BNT thin films by various techniques has been reported [15–18]. Successful epitaxial layers have been reported in various works using different substrates and/or buffer layers [16,18], but single-phase BNTs could only be obtained with certain stoichiometries, for example using Bi- and/or Na<sup>+</sup>-rich targets or Manganese in the Ti-sites when PLD is used.

On the other hand, chemical solution deposition (CSD) has shown a high degree of control over the stoichiometry and the microstructure for the synthesis of BNT thin films. For instance, Abou Dargham et al. [18] reported that BNT films prepared by chemical solution deposition (CSD) and annealed under air atmosphere at 650 °C exhibited low crystallization, while when annealed at 700 °C they exhibited good crystallization without preferential orientation or secondary phases. The authors evidenced encouraging electrical properties, but only a leaky PE hysteresis loop was achieved without reaching saturation. However, Zannen et al. [19] reported that an air annealing of the polycrystalline BNT film at 700  $^{\circ}$ C during 5 min in a preheated tube furnace was more appropriate to obtain crack-free films with a closely saturated PE hysteresis loop under a high applied electric field. A slim saturated hysteresis loop is reported also by Fang Wang et al. for CSD film deposited on commercial Pt-substrate [20]. Furthermore, Hiroshi Maiwa et al. [21] annealed CSD thick films under air in an infrared furnace at 550–700 °C for 10 min. This temperature has been reduced to 400 °C in the work of Ye Zhao et al. which used LNO/Si (100) substrates [22]. The obtained PE hysteresis loop for CSD thick films were found comparable, in terms of ferroelectric hysteresis, to Zannen et al. From these previous works, it appears that the processing conditions play a crucial role in the microstructural and electrical properties of the obtained BNT thin films, and hence may explain the spread of the reported electrical properties. It is worth noting that a review of the extensive literature shows that a systematic analysis of the annealing atmosphere effect on the defect chemistry of BNT films and their associated electrical properties is lacking. Recall that a solid-state dielectric capacitor enables the storing of electrical energy directly without any conversion. Initially in a dielectric material, dipoles are randomly aligned and while applying an external electric field (E), these dipoles are polarized and aligned in the E direction. Note that the capacitor affords high-power density compared to the batteries and ultrafast charge-discharge performances compatible with high-power/pulsed-power applications. Nevertheless, the associated energy density is still very small. Shaping a dielectric material with improved energy storage properties becomes the challenge to meet the need of modern applications. There has been a lot of research conducted on this topic, which is still ongoing. In order to enrich this debate and to make a useful contribution that could be of interest to the scientific community dealing with BNT, we investigate in the present work the effect of the oxygen annealing atmosphere on the microstructure, structural and electrical properties of BNT thin film processed by Sol-gel under oxygen atmosphere. It has been shown that the electrical properties are highly influenced by annealing the film under  $O_2$ . Low dielectric

losses and hysteresis loops were obtained, whereby interesting electrostatic energy storage properties could be achieved.

### 2. Materials and Methods

BNT thin film was prepared via chemical solution deposition combining a sol-gel process and the spin coating method. The precursor solution was prepared using highpurity bismuth acetate (III) ( $C_6H_9BiO_{6}$ ,  $\geq$ 99.99%, Sigma Aldrich, Darmstadt, Germany), sodium acetate Anhydrous (C<sub>2</sub>H<sub>3</sub>NaO<sub>2</sub>, Sigma Aldrich, Darmstadt, Germany) and titanium isopropoxide (C<sub>12</sub>H<sub>28</sub>O<sub>4</sub>Ti; 97+% Alfa Aesar, Karlsruhe, Germany). To yield a solution with concentration of 0.3 mol/L, appropriate amounts of the reagents were dissolved in acetic acid (CH<sub>3</sub>COOH), 2-Methoxyethanol (CH<sub>3</sub>OCH<sub>2</sub>CH<sub>2</sub>OH), and acetyl acetone (AcAc, Merk, Darmstadt, Germany), which were selected as stabilizers. In a first step, Bi- and Na- acetates were dissolved in acetic acid. However, Ti- isopropoxide was dissolved in 2-methoxyethanol with the addition of the chelating agent (AcAc). The two solutions were mixed together and stirred at room temperature for 24 h until getting a stable yellow solution. The solution was spin-coated onto Pt/SiN substrate at a speed of 2000 rpm for 35 s. Noting that the substrate was subjected to a cleaning procedure, firstly in ethanol and then in a de-ionized water ultrasonic bath, in order to remove the surface adsorbents and enable a uniform film growth. Five coating sequences were performed, and each layer was dried at 120 °C and then pyrolyzed at 400 °C for 10 min on a hotplate. Final annealing was performed at 600 °C in a tube furnace under an O<sub>2</sub> atmosphere for 30 min.

The microstructure of the investigated film was analyzed by scanning electron microscope (SEM) (Environmental Quanta 200 FEG, FEI) coupled with energy-dispersive X-ray spectroscopy (EDX). The surface morphology was studied by atomic force microscopy (AFM) using a commercial setup NTEGRA Aura (NT-MDT) microscope working in contact mode.

The identification of the purity of the phase formation was carried out by X-ray diffraction (XRD) using a four-circle-high-resolution Bruker Discover D8 diffractometer (D8 Advance, Bruker, Mannheim, Germany) operating at 40 kV and 40 mA, equipped with a copper anticathode. A Göbel mirror yielded a diffracted parallel beam and a LynxEye detector was used in the 1D mode, resulting in much shorter measurement times and better counting statistics. A beam attenuator is inserted in the incident X-ray beam. XRD investigations were carried out in both the out-of-plane mode and the grazing incidence mode (GIXRD). For GIXRD experiments, collimation was achieved by placing two divergence slits (0.2 mm and 0.1 mm) in the incidence path. A 0.2° equatorial Soller slit was used to limit the axial divergence of the diffracted X-ray beam. A K<sub>β</sub> nickel filter was mounted in the secondary path. The scans were collected with a grazing incidence angle of 2°, a 2 theta increment of 0.02°, and a step time of 1 s. For out-of-plane measurements, a double reflection channel-cut Ge monochromator was used to select the Cu K $\alpha_1$  radiation (1.5406 Å). A divergence slit (0.2 mm) was placed in the incident X-ray beam. The omega/2 theta scans were recorded with a step size of 0.01° and a step time of 1 s.

Raman spectroscopy was performed using a micro-Raman Renishaw spectrometer (green laser excitation of 514.5 nm) and the spectrum was collected in a back-scattering geometry. The laser power was kept below 20 mW to avoid sample heating. For electrical characterizations, top Au electrodes with 220  $\mu$ m of diameter were deposited by sputtering method (Bal-Tec SCD-050) using a shadow mask. Noting that a corner of the Pt bottom electrode was left uncoated for ensuring the electrical contact. Room temperature dielectric measurements were carried out using a Solartron Impedance analyzer SI-1260 at driving signal amplitude of 25 mV and in the frequency range from 1 kHz to 1 MHz. A Ferroelectric test system (TF Analyzer 3000, aix-ACCT) was used to collect *P-E* hysteresis loops at room temperature under different applied electric fields. A probe system attached to a Keithley 2611A source was used to measure the leakage current properties in the step mode with a delay time from 30 to 200 s to allow sample discharging.

# 3. Results and Discussion

# 3.1. Microstructural Analysis

Scanning electron microscopy (SEM) micrographs of thin BNT films annealed at 600 °C under an  $O_2$  atmosphere are shown in Figure 1. It is worth noting that the film exhibits a relatively dense grained structure without porosity and cracks. In addition, grains seem to be uniformly distributed (Figure 1a). The obtained microstructure is different to the one reported by Yang et al. [23] for Na<sub>0.51</sub>Bi<sub>0.50</sub>(Ti<sub>0.96</sub>W<sub>0.01</sub>Ni<sub>0.03</sub>)O<sub>3</sub> thin films. The authors showed that the microstructure is governed by Na nonstoichiometry. However, it is in good agreement with typical microstructure reported in the literature for BNT thin films prepared by CSD [7]. A typical cross-section of the film is presented in Figure 1b. It evidences a uniform thickness of about 475.6 nm.



**Figure 1.** (a). SEM image showing the microstructure of BNT thin films annealed at 600 °C under O<sub>2</sub>. (b). Cross-sectional image of the BNT thin film annealed under O<sub>2</sub>.

Figure 2 presents the EDX spectra in compositional distribution for the investigated BNT films. As expected, characteristics of starting elements, namely Bi, Na, Ti and O, are detected. A close look to the obtained atomic weight reveals that the BNT films show a ratio of Bi/Na less than 1.0, thus it evidences a deficiency of Na atoms on the A- site of the BNT structure.

The surface topography and roughness investigated by AFM provide more insight into the understanding of the microstructure. The topography of the film surface obtained in contact mode AFM is shown in Figure 3. The image was recorded on the  $10 \times 10 \ \mu m^2$  scan region. A fine-grained structure was observed for the investigated sample, which is essentially smooth. The founded root mean square (RMS) roughness value was 1.5 nm.



Figure 2. EDX spectra with elemental composition of BNT thin films annealed under O<sub>2</sub>.



**Figure 3.** (a). AFM micrograph of the BNT thin film deposited by the Sol gel method on a Pt/SiN substrate and annealed under the atmosphere of oxygen, (b). the corresponding 3D AFM image.

## 3.2. Structural Investigations

The  $\theta$ -2 $\theta$  XRD patterns of the investigated sample is shown in Figure 4. The diffractograms of BNT-O<sub>2</sub> and of the substrate are compared in Figure 4a. Several peaks of the substrate can in fact mask those of the film. Thus, the grazing incidence mode (GI) was used to eliminate the substrate contribution, and the obtained XRD patterns are presented in Figure 4b. Noting that the film exhibits pure perovskite without secondary phase (in the limit of the diffractometer detection). The obtained diffraction peaks are indexed according to a pseudo cubic unit cell. The obtained diffractogram evidences a fully random orientation and exhibits 5 diffraction peaks in the 2 $\theta$  range between 20° and 80°. These peaks appeared at 2 $\theta$  = 22.69°, 32.27°, 39.7°, 46.31°, 57.57° and 67.31°, corresponding respectively to the (100), (110), (111), (200), (211), and (220) reflections of BNT bulk material crystallize in rhombohedral symmetry with *R3c* as a space group.

Raman spectroscopy is used in the present work as a powerful tool to get complementary information about structural changes, which are not accessible by the XRD technique. The room temperature spectrum of the investigated film is presented in Figure 5, together with the Raman spectrum of a BNT ceramic given for comparison.



**Figure 4.** (a). Room temperature X-ray diffractogram of BNT-O<sub>2</sub> (red profile) thin film and of the substrate (black profile). (b). X-ray diffraction patterns measured under grazing incidence of the BNT thin film.



**Figure 5.** The upper part shows the room temperature Raman spectrum of the BNT thin film annealed under O<sub>2</sub> atmosphere. It has to be compared with the experimental spectrum of BNT ceramic (bottom part) given as reference.

It is worthwhile to mention that for BNT bulk material with R3c symmetry, the irreducible representation is given by Equation (1) [24]:

$$\Gamma(\text{vibr}) = 7A_1 + 6E,\tag{1}$$

Experimentally, these observed modes are broad and overlap each other, and these features are the signature of disorder in the perovskite lattice caused by the random distribution of Bi and Na cations in the A sites. In addition, the deconvolution of the spectra gives six peaks. The first one is observed at  $135 \text{ cm}^{-1}$  and is attributed to the Na-O vibration lattice. The intense mode observed at  $275 \text{ cm}^{-1}$  is assigned to the Ti-O vibrations. The four modes observed in the wavenumber interval from 400–900 cm<sup>-1</sup> are related to the vibration and rotation of oxygen octahedra [25].

The obtained modes are given in Table 1, along with a comparison with the literature data on ceramics, single crystal, epitaxial, and polycrystalline thin films [7,12].

**Table 1.** Raman modes observed for pure BNT film at room temperature. Experimental Peak data reported in the literature are also given along with their mode assignments.

BNT Sample Type	A1TO1 Symmetry Na-O Mode (cm <sup>-1</sup> )	ETO <sub>2</sub> Ti-O Mode (cm <sup>-1</sup> )	E(TO8)	A1(TO8)	LO3	LO3	Ref.
BNT Ceramic	135	275	514	583	760	840	[25]
BNT single crystal	135	275	530		400-600		[26]
BNT polycrystalline thin films	135	276	514	582	767	845	[27]
BNT-O <sub>2</sub>	109	275	530	600	786	856	This work

The comparison of the Raman spectra presented in Figure 5 and the peak data reported in the Table 1, shows no change in position for the intense band assigned to the Ti-O vibration at 275 cm<sup>-1</sup> almost similar in the bulk ceramic. However, the lower mode corresponding to the Na-O vibration exhibits a downward shift for BNT film. The shift of this mode towards lower frequencies could be attributed for instance, to the increase in the mass of the cations of sublattice A as in the case of the substitution of Na+ with large cation K<sup>+</sup> in the solid solution  $(Na_{1-x}K_x)_{0.5}Bi_{0.5}TiO_3$  [24]. However, in our study, there is no substitution of Na<sup>+</sup> but only a Na deficiency that might lead to a strong anisotropic lattice distortion, because the Na –  $V_{\ddot{O}}$  – Na distance is elongated compared to that of Na–O-Na, in agreement with the work of Tyunina et al. [28]. The authors reported that in ATiO<sub>3</sub> thin films (A = Ba, Sr), the elongation of Ti –  $V_{\ddot{O}}$  – Ti compared to Ti-O-Ti induces the stress around the vacancy. With this increase of the chemical bond length while maintaining the same force constant, the vibrational frequency is expected to decrease. Such an effect could explain the low-frequency shift of Na-O vibration mode.

In the BNT ceramic, the high frequency modes (~514 cm<sup>-1</sup>, ~583 cm<sup>-1</sup>, ~760 cm<sup>-1</sup> and ~840 cm<sup>-1</sup>) result from TiO<sub>6</sub> octahedral vibrations while cations are almost at rest. These modes are also observed in the thin film. Concerning the ~514 cm<sup>-1</sup> and ~583 cm<sup>-1</sup> (doublet d1) modes, it is reported that the evolution of these bands is governed by the increase of the average ion radii of the cations in sublattice A, similar to the case of the BNT-BT solid solution [27] or rare earth doped BNT ceramics [29,30]. It is worthwhile to note that in the pure BNT ceramic these two modes are reported with equal intensity, thus forming a plateau-like band [25]. However, while increasing the temperature (or doping), the intensity of the first mode becomes the dominant one, whereas the second one vanished as reported in the cited references above. In a study carried out on BNT single crystal, Liang Luo et al. [27], have correlated this behavior to the presence of Ti–O rotations with short correlation lengths. Regarding these modes in the present study, the intensity of the first more intense.

The vibration modes observed around 760 and 840  $\text{cm}^{-1}$  for BNT ceramic (doublet d2) are well known to involve oxygen atoms vibrations. As depicted from the figure, these

two modes seem merged to a broad one in the BNT thin film. The occurrence of oxygen vacancies should affect the bond length and angles of the oxygen octahedra [31]. An expansion in octahedra could lead to an increase of the bond length between the ions, and, thus, could reduce the stiffness of the bond leading to the downshift in frequency [32]. The vibration modes ~514 cm<sup>-1</sup> and ~583 cm<sup>-1</sup>, do not follow the same trend as the ceramic, meaning that not only the strain induced by oxygen vacancies can explain the evolution of these modes [32].

The displacement of Raman spectra may be caused by stresses/strains in different directions and individual stress tensors for a given data a reported by Atkinson et al. [33]. Therefore, as is suggested by Wolf et al. [34] that the interpretation of the Raman results needs the knowledge of the stress state in the studied material. Thus, combining Raman spectroscopy with other advanced techniques such as low-angle X-ray diffraction, neutron and cyclotron diffraction can give more information about the unknown stress states in the investigated material.

### 3.3. Dielectric, Leakage Current, and Ferroelectric Properties

Figure 6 shows the frequency dependence of the dielectric constant and dielectric loss tan  $\delta$  for BNT thin film annealed under an O<sub>2</sub> atmosphere. It is seen that the frequency dispersion of the dielectric constant is quite low, as the dielectric constant remains constant over a large frequency range, but its value is still very small compared to what is observed for the BNT thin film [35]. Interestingly, low dielectric loss is obtained, demonstrating the prepared thin film will tend to have a high breakdown voltage limit.



**Figure 6.** Frequency dependence of the dielectric constant and the dielectric loss tan  $\delta$  of the BNT thin film annealed under O<sub>2</sub> atmospheres.

Figure 7 shows the ferroelectric properties at room temperature for the investigated BNT thin film. The film exhibits a typical ferroelectric character with a hysteresis loop comparable to the reported literature [20,21]. Noting that for BNT ceramic a huge hysteresis loop is reported and was attributed to the contribution of leakage related to the BNT defect chemistry [29]. For the present films, the obtained *P*-*E* loop is recorded at a very high applied electric field.

Leakage current property is also investigated for the studied BNT film as illustrated in Figure 8. An asymmetric curve is observed because of the asymmetric metal work function of the top Au and bottom Pt electrodes [35]. It can be seen from the plots that the leakage current density of the BNT thin film is lower by several orders of magnitude compared with the ceramic or with some reported thin film data [16]. It is probably that Na-deficiency (Bi-excess depicted for EXD analysis) leads to the creation of a donor state,



which compensates oxygen vacancies and thus, contributes to the improvement of the electrical properties.

Figure 7. *P-E* hysteresis loop of BNT thin film prepared under O<sub>2</sub> atmosphere.



Figure 8. Room temperature *J*-*E* curve of a BNT thin film annealed under oxygen atmosphere.

It is worth noting that in the present work, BNT solution is prepared without any excess of the starting reagent to compensate the Bi and/or Na deficiency that could result from the volatility of  $Bi_2O_3$  and  $Na_2O$  during the synthesis process. The induced Bi/Na-vacancies are expected to be compensated by oxygen vacancies according to the following Equations (2) and (3) (Kröger-Vink notation):

$$2Na_{Na}^{x} + O_{O}^{x} \to 2V_{Na}^{\prime\prime} + V_{\ddot{o}} + Na_{2}O\uparrow,$$
<sup>(2)</sup>

$$2Bi_{Bi}^{x} + 3O_{O}^{x} \rightarrow 2V_{Bi}^{\prime\prime} + 3V_{\ddot{o}} + Bi_{2}O_{3}\uparrow,$$
(3)

Obviously, the presence of oxygen vacancies is expected to induce high dielectric loss in the material. However, the BNT-O<sub>2</sub> film show good dielectric properties with frequency stability of both the dielectric constant and the dielectric losses as well as good ferroelectricity compared to other atmospheres (see supplementary materials). Recall that in EDX the At% of Bismuth is very higher compared to the At% of Sodium, thus we surmise that the mass of  $Bi_2O_3$  is in excess compared to  $Na_2O$ . In this case, the excess will

compensate not only the volatility of  $Bi_2O_3$  but also that of  $Na_2O$ , and in this way, it limits the creation of oxygen vacancies according to Equation (4):

$$Bi_2O_3 + 2V'_{Na} + 3V_{\ddot{o}} \to 2Bi''_{Na} + 3O^x_{O},$$
 (4)

# 3.4. Energy Storage Investigation

The energy storage density and the efficiency ( $\eta$ ) can be determined from the P-E hysteresis loop using Equations (5) and (6):

$$W_{rec} = \int_{Pr}^{Pm} EdP, \tag{5}$$

$$\eta = \frac{W_{rec}}{W_{rec} + W_{loss}} \times 100,\tag{6}$$

where *P* is the polarization, ( $W_{rec}$ ) is the recoverable energy density, *E* is the applied field, and ( $W_{loss}$ ) is the energy loss density as it shown from Figure 9a, given by Equation (7):

$$W_{loss} = W_{stored} - W_{rec} \tag{7}$$



**Figure 9.** (a). General ferroelectric hysteresis loop showing  $W_{rec}$  (green color) and  $W_{loss}$  (red color). (b). Evolution of the energy storage parameters versus field for BNT thin film.

The variation of the obtained energy density and efficiency as a function of applied field is presented in Figure 9b.

The investigated film shows an interesting high recovered energy density that exceeds 1 J/cm<sup>3</sup> and an efficiency of 50% under a low electric field *E* of only 630 kV/cm that demonstrates the better dielectric rigidity with a high breakdown electric field compared

with the BNT-based ceramics. Noting that the breakdown field is not achieved in our experience because of the device limitation. High recoverable energy density at high electric field has been reported for CSD thin films [20,22], thus, we expect an increase of the recovered energy with the applied electric field.

## 4. Conclusions

In summary, a lead-free polycrystalline thin film of Bi<sub>0.5</sub>Na<sub>0.5</sub>TiO<sub>3</sub> was prepared on a Pt/SiN substrate by the sol-gel method and annealed under an O<sub>2</sub> atmosphere. Both SEM and AFM images allowed the analysis of the film microstructure. EDX analysis showed that the investigated film is Na- deficient. Pure perovskite phase with *R3c* rhombohedral symmetry was evidenced by X-ray diffraction using grazing incidence method and it was corroborated by Raman investigation. Furthermore, dielectric, ferroelectric, and leakage current properties were investigated at room temperature and revealed that the BNT thin film showed good electrical properties with a high frequency stability of the dielectric constant, low dielectric losses, and good ferroelectric properties with well saturated hysteresis loop, along with low leakage current density. One defect mechanism was suggested where the Na- deficiency leads to the creation of a donor state, which compensates oxygen vacancies and reduces leakage current in the BNT thin film prepared under an oxygen atmosphere. The film also presents attractive electrostatic energy storage properties at a low-applied electric field, which significantly exceeds of the values reported for BNT-based ceramics.

**Supplementary Materials:** The following supporting information can be downloaded at: https: //www.mdpi.com/article/10.3390/qubs7030029/s1, Figure S1: SEM images showing the microstructure of BNT thin films annealed at 600 °C under different atmospheres (a) O2, (b) N2 and (c) Ar, (d) Example of cross-sectional image of the BNT thin film annealed under O2; Figure S2: EDX spectra with elemental composition of BNT thin films annealed under O2, N2, and Ar atmospheres; Figure S3: (a–c) AFM micrographs of the BNT thin films deposited by the Sol gel method on a Pt/SiN substrate under the atmospheres of oxygen, nitrogen and argon, respectively; and (d–f) the corresponding 3D AFM images, respectively; Figure S4: Room-temperature X-ray diffractogram of BNT thin films annealed under N2 and Ar atmospheres; Figure S5: Comparison of the room temperature Raman spectra of the BNT thin films annealed under different atmosphere. The spectrum of a BNT ceramic is given as reference; Figure S6: P-E hysteresis loop of BNT thin films prepared under Ar and N2 atmosphere, respectively.

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