



Article A Statistical Analysis of Commercial Articulated Industrial Robots and Cobots

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Abstract: This paper aims to elucidate the state-of-the-art, prevailing priorities, and the focus of the industry, and identify both limitations and potential gaps regarding industrial robots and collaborative robots (cobots). Additionally, it outlines the advantages and disadvantages of cobots compared to traditional industrial robots. Furthermore, three novel factors are introduced in this survey as metrics to evaluate the efficiency and performance of industrial robots and cobots. To achieve these purposes, a statistical analysis and review of commercial articulated industrial robots and cobots are conducted based on their documented specifications, such as maximum payload, weight, reach, repeatability, average maximum angular speed, and degrees of freedom (DOF). Additionally, the statistical distributions of the efficiency factors are investigated to develop a systematic method for robot selection. Finally, specifications exhibiting strong correlations are compared in pairs using regressions to find out trends and relations between them, within each company and across them all. The investigation of the distribution of specifications demonstrates that the focus of the industry and robot makers is mostly on articulated industrial robots and cobots with higher reach, lower payload capacity, lower weight, better repeatability, lower angular speed, and six degrees of freedom. The regressions reveal that the weight of robots increases exponentially as the reach increases, primarily due to the added weight and torque resulting from the extended reach. They also indicate that the angular speed of robots linearly decreases with increasing reach, as robot manufacturers intentionally reduce the angular speed through reductive gearboxes to compensate for the additional torque required as the reach extends. The trends obtained from the regressions explain the reasons behind these interrelationships, the design purpose of robot makers, and the limitations of industrial robots and cobots. Additionally, they help industries predict the dependent specifications of articulated robots based on the specifications they require. Moreover, an accompanying program has been developed and uploaded on to GitHub, taking the required specifications and returning a list of proper and efficient robots sourced from different companies according to the aforementioned selection method.

Keywords: statistical analysis; industrial robots; cobots; robot efficiency; robot selection

1. Introduction

1.1. Classifications

Robotics plays a pivotal role in automating industries. Due to the mass production of robots in recent years, there has been a significant increase in the adoption of industrial robotic systems. Robots can be classified based on their structure. There exist six categories of industrial robotic manipulators, categorised by their structural configurations [1]. Five of these fall under the serial classification, including articulated, SCARA, Cartesian, cylindrical, and spherical robots [1]. Additionally, robots of the delta category fall into the parallel classification [1]. Parallel robots offer higher acceleration, speed, stiffness, and payload/weight ratio with lower inertia; however, serial robots provide a higher



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). workspace/robot size ratio, as well as ease of calibration and dynamics modelling [2]. The position (angle) errors in serial robots add up together, whereas these errors average in parallel robots, which results in higher position accuracy. However, it is worth noting that the workspace of parallel robots is limited by the length of their shortest link. Articulated robots have been employed in the industry more than robots from other categories due to their human-arm resemblance, wider range of reach, and ease of installation. Consequently, this review specifically focuses on articulated industrial robots.

In terms of human-robot interactions, two types of robots emerge: industrial robots, also referred to as traditional industrial robots and cobots. Figure 1 illustrates different levels of interaction between a robot and a human. At the isolated level, the robot is situated in a cell—an isolated area—and usually has safety measures in place to turn off the robot if someone enters the cell. The coexistence level is when the robot and the human do not have a shared workspace, but the robot is not isolated. In the case of synchronised level, the robot and the human worker share a workspace, but they do not work at the same time. However, various sources provide slightly different definitions for cooperation and collaboration levels. In sources such as [3], cooperation is defined as the simultaneous sharing of workspace by the robot and human without sharing a task. On the other hand, collaboration occurs when they not only simultaneously share the workspace but also share a task in a way that an action of one participant immediately affects the other. Conversely, as outlined in references such as [4], both cooperation and collaboration levels can involve working in the same workspace at the same time and sharing a task. However, the distinctive characteristic that sets collaboration apart from cooperation is the direct physical interaction between the robot and the human.

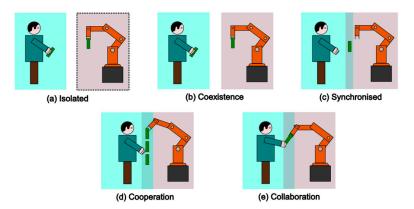


Figure 1. Different levels of human-robot interaction (regenerated from [4]).

Additionally, there are other papers like [5] which describe collaboration as the operation of a robot without a fence or physical barrier next to a person. Although this definition is followed by the market and considers broader robots as cobots, it may not be the most accurate and scientific definition. Nonetheless, the market definition is adopted for this statistical review on commercial articulated robots.

The market is increasingly paying more attention to cobots. According to the data shown in Figure 2, a total of 553,000 industrial robots and cobots were installed globally in 2022, in which cobots, as the necessary component of Industry 5.0, gained increased favourability. As it seems from this figure, more cobots were installed in industries in 2022 compared to previous years. Nevertheless, the majority of industrial robots installed in recent years are of the traditional type. It is noteworthy that the order in Figure 2 will remain the same if it is rearranged based on the cobot-to-traditional-robot ratio.

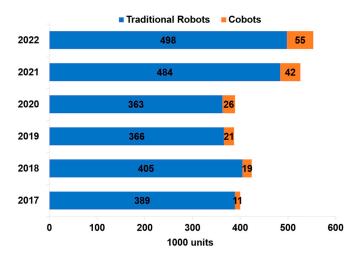


Figure 2. Annual installation of industrial cobots and traditional robots (added to the industry each year) (regenerated from [6]).

1.2. Previous Works, Innovations and Comparison

In order to find statistical and analytical papers reviewing industrial robots or cobots, the following Boolean strings were utilised in Google Scholar, which returned 45 results for industrial robots:

(intitle:review OR intitle:study OR intitle:survey) AND (intitle:statistical OR intitle:statistic OR intitle:analytical OR intitle:analysis) AND (intitle:robot OR intitle:robots OR intitle:robotic) AND (intitle:industry OR intitle:industrial OR intitle:industries).

The Boolean operator "intitle" was employed to just consider titles. This operator finds the exact word which follows it, thus, "intitle:robots" and "intitle:robot" find disparate results. Papers with review themes are expected to incorporate terms such as "review", "study", or "survey" in their title. Those with statistical or analytical themes should include the terms "statistical", "statistic", "analytical", or "analysis" in their title. In addition to the themes mentioned, the target papers should be about industrial robots. Therefore, the titles should contain the words "robot", "robots", or "robotic", in addition to the words "industry" or "industrial".

One result was found for cobots with the following string:

(intitle:review OR intitle:study OR intitle:survey) AND (intitle:statistical OR intitle:statistic OR intitle:analytical OR intitle:analysis) AND (intitle:cobot OR intitle:cobots OR intitle:cobots)

Also, the following Boolean string was obtained by removing the review part and ticking the option review articles in Google Scholar. The resulting Boolean string returned 12 papers for industrial robots:

(intitle:statistical OR intitle:statistic OR intitle:analytical OR intitle:analysis) AND (intitle:robot OR intitle:robots OR intitle:robotic) AND (intitle:industry OR intitle:industrial OR intitle:industries)

The following string returned one result for cobots:

(intitle:statistical OR intitle:statistic OR intitle:analytical OR intitle:analysis) AND (intitle:cobot OR intitle:cobots OR intitle:cobotic)

After careful consideration of the titles and abstracts of all these identified papers, it was perceived that none of them conducted a statistical or analytical review of industrial robots or collaborative robots. Within these results, the only paper with a close theme was [7], which conducted a statistical review of pneumatic industrial robotic grippers. This work investigated the distribution of the specifications of these grippers (such as maximum payload, weight, and reach), compared some of these specifications in pairs, and introduced a factor to assess their efficiency.

This paper considers the specifications of off-the-shelf industrial robots and cobots, including the maximum payload, weight, reach, repeatability, average maximum angular

speed (average of all joints), and DOF. Additionally, it presents three efficiency factors to measure the performance of industrial robots and cobots. Initially, the statistical distributions of these specifications and factors are discussed to identify the focal points of attention for both the industry and robot makers. Some of these specifications, which show a strong correlation, are compared in pairs to discern trends and relations to understand the design purpose of robot manufacturers, limitations, and the underlying reasons for these relations. Moreover, the specifications of industrial robots and cobots are comparatively analysed to elucidate the advantages and limitations of cobots and the potential replacement of industrial robots by cobots.

Furthermore, another aspect of this work is to help industries select a robot that suits their need. To find relevant papers studying the selection of industrial robots, the following Boolean string was deployed:

(intitle:industry OR intitle:industrial OR intitle:industries) AND (intitle:robot OR intitle:robotic OR intitle:robotics) AND (intitle:selection OR intitle:select OR intitle:choose OR intile:choosing)

This Boolean string yielded 81 results. Some of them employ multicriteria decisionmaking (MCDM) methods, fuzzy, or a combination of these techniques to devise a robot selection algorithm. For instance, ref. [8] used a VIKOR (MCDM) method, and ref. [9] deployed a Fuzzy Analytical Hierarchy Process (fuzzy + MCDM) for robot selection algorithms. Additionally, distance-based approaches have been proposed to develop a robot selection method. As an example, a robot selection method based on Mahalanobis distance was introduced in [10] with a database of 27 industrial robots and based on the idea of excluding outlier robots. However, none of these results specifically addressed the distribution of efficiency factors or any statistical feature of a sizable population of industrial robots. The distribution of a substantial population of these robots is of high importance because it reflects the state-of-the-art technology of industrial robots. In the current study, three factors are introduced to measure the efficiency and performance of a notable number of robots. Robots with higher efficiency exhibit greater energy efficiency and lower depreciation. Consequently, robots with lower efficiency can be excluded from the list of appropriate options. On the other hand, because of the competitive nature of the market, the technology, and consequently, the performance of a robot made by a leading company cannot surpass that of other leading companies by far. Therefore, it is more likely that a problem arises with a robot exhibiting a superior efficiency, called an outlier. These robots may be excellent ones that can appropriately fulfil all the reported maximum specifications concurrently in different conditions; however, the possibility of the failure to accomplish those maximum specifications at the same time is greater compared to other robots, and the documented data may be assessed in specific conditions. For instance, it may not be possible to obtain the reported repeatability of a robot while it is at its maximum reach and carrying the maximum payload, especially for outlier robots. The idea of setting aside outlier robots, as well as inefficient ones, has been put forward in [10] and is adopted in the current review.

The structure of this paper is as follows: Section 2 explains the sources of data and the methodology of data gathering. Section 3 presents the distribution of the specifications to identify the main requirements of the industry. Section 4 shows specifications with strong correlations to uncover trends and reasons behind the design choice of robot makers. Section 5 outlines the robot selection method based on the distribution of the proposed efficiency factors. Section 6 puts forward additional specifications for inclusion by robot manufacturers to be investigated in future works. Finally, the Section 7 remarks on the key findings of this survey.

2. Scope and Data Extraction

2.1. Target Robots and Cobots

As indicated previously, articulated robots are the predominant choice in the industry. Therefore, in this review, off-the-shelf (available in the market) articulated industrial robots and articulated industrial cobots are specifically investigated. Their catalogues on the official website of the manufacturers are considered to extract the payload capacity, weight, reach, repeatability, average maximum angular speed (AMAS), and DOF. These specifications are asserted in all catalogues; however, specifications such as maximum linear speed are not stated in all catalogues and, thus, are not taken into consideration in this work.

2.2. Target Robot Manufacturers

In this review, the "Big 4" companies in robotics, Fanuc, ABB, Kuka, and Yaskawa, which collectively represent more than approximately half of the global market share in industrial robots according to [11–13], are addressed. Figure 3 demonstrates the financial worldwide market share of each of these four leading companies in 2019 and outlines that they together held 56% of the market. Additionally, Universal Robots, which held 55% and 46% of the cobot market share in 2016 and 2017, respectively, [14] and reported sales revenue of 248 million USD in 2019 [15], is also included in this analysis.

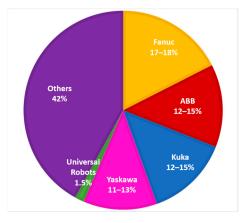


Figure 3. Financial market shares of the four leading companies in robotics in 2019. The figure is obtained based on the data provided by [13] and by adding the share of Universal Robots. The whole market capital was 19 billion USD.

This review investigates a total of 455 articulated industrial robots and cobots, which comprises 416 industrial robots and 39 cobots. The cobot-to-industrial-robot ratio in this review is 0.093, close to the 2022 sales ratio shown in Figure 2, which is 55,000 cobots over 498,000 industrial robots, or 0.110. Table 1 presents information on the quantity of industrial robots and cobots included in this survey, categorised by their respective manufacturers. It should be highlighted that the ratio of the number of the total robots exhibited in Table 1 for each company does not align with the percentages depicted in Figure 3. However, this disparity does not constitute any conflict because selling a greater number of robots by one company does not necessarily result in higher revenue compared to another company.

Table 1. The number of articulated industrial robots and cobots from the target robot manufacturers that were studied in this analysis. (The background colour is for better reading of the items).

Manufacturer	No. of IR	No. of Cobots	No. of Total Robots
Fanuc	90	11	101
ABB	97	8	105
Kuka	157	9	166
Yaskawa	72	6	78
Universal Robots	0	5	5
Total	416	39	455

In the section Appendix A, in Tables A1–A5, the model of the industrial robots and cobots of Fanuc, ABB, Kuka, Yaskawa, and Universal Robots considered in this analysis are presented.

2.3. Data Sources

In this survey, articulated industrial robots and cobots available on the official websites of these companies with catalogues presenting necessary specifications were considered. The datasheets for Fanuc robots were gathered from [16], ABB robots from [17], Yaskawa robots from [18], and Universal Robots from [19]. Regarding Kuka, robots listed in [20] were taken into account, and if their datasheets were not available in [20], they were obtained from [21].

It is important to indicate that each model of the robots available on the website of the manufacturers impacts the analysis equally (following the same strategy referenced in [7]) without considering the actual sales statistics for each robot since this information is not publicly accessible. However, this approach does not necessarily constitute a weakness in this survey because of the fact that popular products usually feature several editions and series and maintain a longer presence in product listings.

It must be acknowledged that the data analysis in this study relies solely on the details presented in the datasheets of the robots; however, these data points may contain some form of exaggerations, inaccuracies, or measurements conducted under specific conditions. Nonetheless, the data are mostly deemed trustworthy since well-known companies are generally inclined to safeguard their reputation. Consequently, a method is proposed in Section 5 to assist in removing possible outlying data for robot selection.

3. Data Distribution

3.1. Statistical Values of Specifications

To analyse the obtained data, it is essential to elucidate some statistical parameters and how their relative positions contribute to describing the data distribution. Mean and median are the two statistical parameters utilised to measure the tendency of data. Unlike the mean, the median is typically less affected by the outlier and extreme data points. In an asymmetric data set, the mean is not usually at the centre of the distribution; therefore, the median is often the preferred statistical parameter for identifying the central tendency [22].

From a statistical point of view, in a right-skewed distribution, the mean is often greater than the median, and the data is denser on the left side. Conversely, when the distribution is skewed to the left, the median is often greater than the mean, and the data is denser on the right side. The maximum, minimum, mean, and median (statistical values) of the specifications for the total of industrial robots and cobots are presented in Table 2. The specifications mentioned in Table 2 will be discussed further in the next subsections.

Data	Min.	Max.	Mean	Median	Count
Weight (kg)	7.0	12,500	1026.2	665.0	455
Payload capacity (kg)	0.5	2300	176.8	80.0	455
Reach (mm)	350.0	4683.0	2211.8	2403.0	455
A factor (mm)	7.4	1131.7	346.5	291.8	455
Repeatability (mm)	0.01	0.9	0.07	0.05	453
B factor	50.0	47,237.0	7240.2	6581.4	453
AMAS (°/s)	21.0	700.0	224.7	173.0	447
C factor (°/s)	25.4	12,541.4	1566.9	1174.1	445
DOF	3	15	6.0	6	455

Table 2. Ranges and statistical values of specifications and factors of articulated industrial robots and cobots. (The background colour is for better reading of the items).

According to Table 2, all the obtained specifications exhibit a right-skewed distribution, except for reach, which is skewed to the left. Regarding articulated robots, it can be inferred that companies prefer higher reach and better repeatability while showing a tendency

towards lower payload capacity, weight, and angular speed. One of the possible reasons for the choice of lower payload capacity could be the prevalence of small-sized parts in production lines that require manipulation. Additionally, opting for lower payload capacity results in a reduction in the weight of the robot and subsequently leads to a decrease in both depreciation and the cost of the robotic system.

Table 3 illustrates trends of the data for industrial robots, where all the specifications are skewed to the right, except for reach, which is left-skewed. The specification distributions of industrial robots mirror the same pattern seen in the dataset of the whole robots presented in Table 2.

Table 3. Ranges and statistical values of specifications and factors of articulated industrial robots. (the background colour is for better reading of the items).

Data	Min.	Max.	Mean	Median	Count
Weight (kg)	7.0	12,500.0	1116.3	995.0	416
Payload capacity (kg)	0.5	2300.0	192.2	110.0	416
Reach (mm)	350.0	4683.0	2311.4	2600.0	416
A factor (mm)	13.3	1131.7	355.0	307.2	416
Repeatability (mm)	0.01	0.9	0.07	0.05	414
B factor	50.0	47,237.0	7250.2	6576.8	414
AMAS (°/s)	21.0	700.0	226.5	173.0	414
C factor (°/s)	25.4	12,541.4	1593.8	1168.4	412
DOF	3	15	5.9	6.0	416

Table 4 presents the statistical values for industrial cobots, revealing trends which are consistent with industrial robots and the whole robots, except for reach, demonstrating a relatively symmetric distribution.

Table 4. Ranges and statistical values of specifications and factors of articulated industrial cobots.(the background colour is for better reading of the items).

Data	Min.	Max.	Mean	Median	Count
Weight (kg)	9.5	375.0	65.3	46.3	39
Payload capacity (kg)	0.5	50.0	12.2	10.0	39
Reach (mm)	500.0	1900.0	1149.4	1150.0	39
A factor (mm)	7.4	691.7	255.4	236.2	39
Repeatability (mm)	0.01	0.15	0.05	0.04	39
B factor	367.8	23,189.1	7134.5	6581.4	39
AMAS (°/s)	99.0	408.0	201.9	180.0	33
C factor (°/s)	100.8	2757.1	1231.1	1205.4	33
DOF	6	14	6.3	6	39

In the next subsections, the distribution of each specification is investigated in detail.

3.2. Distribution of Payload Capacity

The maximum payload a robot can carry occurs when its centre of mass is at the **0** position, which is considered the payload capacity of a robot in this work. As highlighted in Table 2, the mean payload capacity is approximately double the median value. Consistent with this, in Figure 4, the data exhibits a rightward skew. This information reveals that payload values are denser at the left. Additionally, the figure demonstrates two notably dense areas, one that centres around 10 kg (the focus of robots designed for manipulating lighter objects) and another one around 200 kg (the centre of robots designed for handling heavier objects).

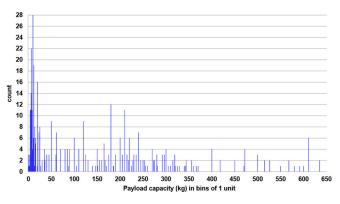


Figure 4. A bar chart histogram of the distribution of maximum payload for industrial robots and cobots in bins of 1 kg, up to 650 kg.

According to Figure 5, depicting the cumulative percentages of payload capacities, 40% and 70% of the industrial robots and cobots possess a payload capacity of less than 25 kg and 210 kg, respectively. These data collectively indicate that the prevalent emphasis of the industry and robot makers is on robots with lower payload capacities. This inclination could be attributed to the predominance of small-sized products made by industries. Therefore, robots employed for the handling and manipulation of these objects tend to provide lower payload capacities. Moreover, tools used in welding, painting, and assembly tasks typically have smaller dimensions, consequently resulting in a lower payload capacity in welding, painting, and assembling robots.

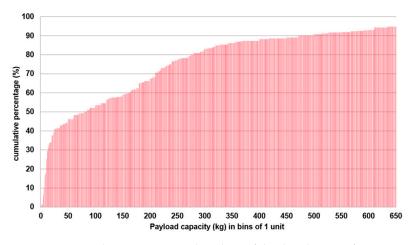


Figure 5. A cumulative percentage bar chart of the distribution of maximum payload for industrial robots and cobots in bins of 1 kg, up to 650 kg.

It should be noted that the manipulation of heavy objects, especially when the gripping point of the object is far from the centre of gravity, can be facilitated through the collaboration of multiple robots working together. This strategy may draw attention to robots with lower payload capacity and, consequently, lighter robots, especially in future applications. The idea of using multiple robots (a swarm of robots) for handling nonuniform loads has been investigated in [23]. Additionally, ref. [24] has surveyed dual arm manipulation. Furthermore, the Robotic Operating System (ROS and ROS2) has been paving the way for enabling the easy and efficient collaboration of robots working with each other.

Based on Table 3, illustrating the mean payload capacity of industrial robots is approximately twice the median value, and referring to Figure 6, where the data is skewed to the right, these observations together imply a higher concentration of payload values towards the left. Furthermore, Figure 6 exhibits two distinct denser areas—one around 10 kg (the preferred area for robots manipulating lighter objects) and another one around

200 kg (the preferred area for robots manipulating heavier loads). This pattern is in line with the results obtained for the mixed data of industrial robots and cobots.

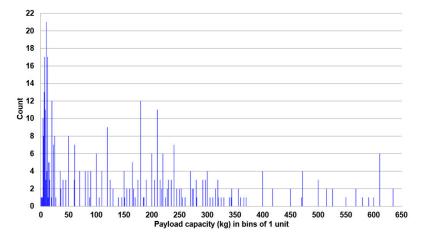


Figure 6. A bar chart histogram of the distribution of maximum payload for industrial robots in bins of 1 kg, up to 650 kg.

It is remarkable that, with reference to both Tables 3 and 4, the mean and median payload capacities of cobots are less than one-tenth of the average and median payload capacities of industrial robots. The median and mean payload capacities of cobots are approximately 10 kg, and, as illustrated by Figure 7, the concentration of payload capacity is centred around 10 kg, collectively suggesting a symmetric distribution of data. In light of these data and recognising that the maximum payload capacity of cobots is just 50 kg, it can be inferred that cobots are designed for handling lighter objects. However, through the implementation of more advanced sensors and cameras (for human–robot interactions), control and AI algorithms, and human awareness features, it will be possible to make cobots with heavier payload capacities work safely with humans, consequently filling this gap in the industry.

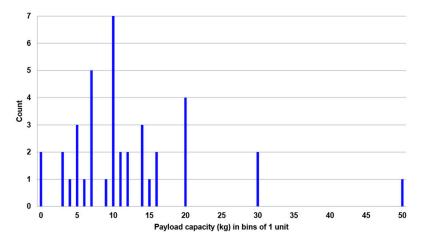


Figure 7. A bar chart histogram of the distribution of maximum payload for industrial cobots in bins of 1.

3.3. Weight Distribution

A right-skewed bar chart histogram illustrating the weight of the total of industrial robots and cobots is provided in Figure 8. Considering this histogram and referencing Table 2, which mentions the mean weight is 1.5 times the median value, it can be concluded that the weight distribution is more concentrated on the left side.

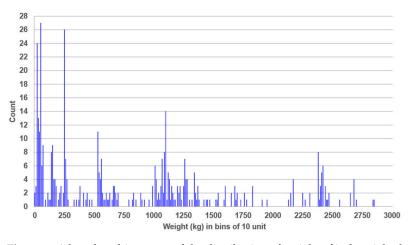


Figure 8. A bar chart histogram of the distribution of weight of industrial robots and cobots in bins of 10 kg, up to 3000 kg.

Three focal points around 50, 250, and 1100 kg can be observed for the weight of industrial robots and cobots in Figure 8. In addition, Figure 9 highlights a 20%, 40%, and 70% of industrial robots and cobots weigh relatively less than 50 kg (robots manipulating light objects), 250 kg (robots mostly handling medium objects), and 1100 kg (robots manipulating heavy objects), respectively. By taking all these data into account, it is suggested that the prime focus of the industry and robot makers is lighter robots.



Figure 9. A cumulative percentage bar chart of the distribution of weight of industrial robots and cobots in bins of 10 kg, up to 3000 kg.

One of the possible reasons for this trend is that the industry and industrial robot makers emphasise lower payload capacities, as elaborated in the previous subsection. Thus, there is a focus on designing lighter robots. Another rationale is that lighter robots enable easier transportation and installation. Moreover, lighter industrial robots and cobots often come with lower prices and maintenance costs. Additionally, the reduced weight of a robot typically results in less depreciation, higher speed, and lower cycle time. As indicated in the preceding subsection, the promotion of using multiple cooperating smaller robots, as opposed to a single larger one, may further increase the popularity of lighter robots in the future.

Some studies, including [25], have deployed different optimisation methods to design industrial robots with decreased weight to enhance their efficiency. Additionally, [25] reveals how adding some holes in the arms of robots can improve their strength through decreasing their weight and enhancing their stress distribution. Therefore, it can be inferred that a higher weight may not necessarily result in better strength, and vice versa. Given the information in Table 3, although the median weight of industrial robots is closer to the mean value compared to the combined total of industrial robots and cobots, the median is still 10% less than the mean. The data is also skewed to the right, based on Figure 10. Therefore, the data is denser on the left, which shows that lighter industrial robots are typically preferred in the industry. It is also notable that, according to Figure 10, three areas are denser: one centres around 50 kg (industrial robots manipulating delicate objects), the second around 250 kg (industrial robots typically handling medium objects), and the last around 1100 kg (industrial robots and cobots.

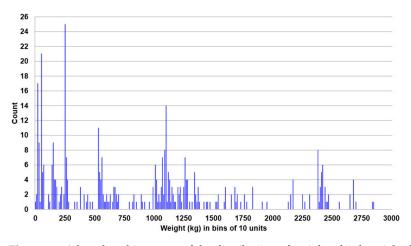


Figure 10. A bar chart histogram of the distribution of weight of industrial robots in bins of 10 kg, up to 3000 kg.

Interestingly, according to Tables 3 and 4, the mean and median weights of cobots are roughly one-twentieth of the mean and median weight of industrial robots, respectively. The median is 30% less than the mean weight of cobots, and Figure 11 exhibits a right-skewed distribution. Consequently, the data is more concentrated on the left. Furthermore, as depicted in Figure 11, the dense area of the weight distribution is around the median, which is 46 kg. By considering these data, it can be assumed that cobots are lighter in comparison to industrial robots because they handle lighter payloads, and they should be safe to work with people. As indicated in the previous subsection, the implementation of more precise sensors and advanced control and AI algorithms makes cobots handle heavier payloads more safely and cautiously alongside humans. This development may contribute to the creation of industrial cobots with higher payload capacity, and consequently, heavier weight will be available in the future.

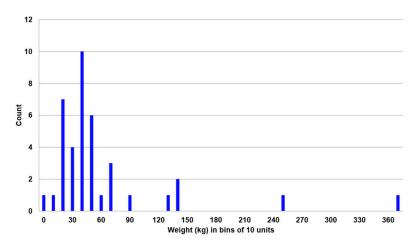


Figure 11. A bar chart histogram of the distribution of weight of industrial cobots in bins of 10 kg.

3.4. Distribution of Reach

Reach (stroke) for industrial robots and cobots is defined as the maximum distance between the centre of the wrist of the robot and the axis of the first joint, perpendicular to this axis.

Referencing Table 2, the median reach is approximately 9% greater than the mean (unlike other specifications) and, as illustrated in Figure 12, the data is relatively right-skewed. Consequently, the data is roughly denser on the right, in contrast to other specifications.

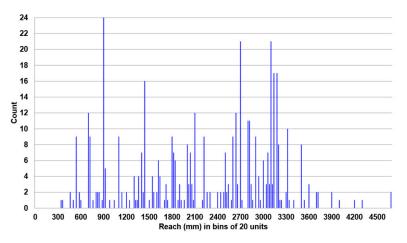


Figure 12. A bar chart histogram of the distribution of reach of industrial robots and cobots in bins of 20 mm.

In accordance with Figure 13, 70% of the robots exhibit a reach of higher than 1600 mm, and 30% surpass 3000 mm. Considering these observations collectively, it can be inferred that the industry and robot makers prefer higher reach over higher payload capacity.

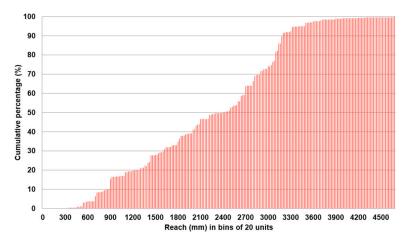


Figure 13. A cumulative percentage bar chart of the distribution of reach of industrial robots and cobots in bins of 20 mm.

This reveals that the applications of robots in the industry predominantly include manipulating smaller objects over extended distances, such as picking and placing, machine tending, arc welding, and painting.

Given the information in Table 3, the median reach of industrial robots exceeds the mean value by relatively 13%, and, based on Figure 14, the data is skewed to the left. Accordingly, the data is denser on the right, and it shows that the predominant focus of industrial robots is on achieving longer reach.

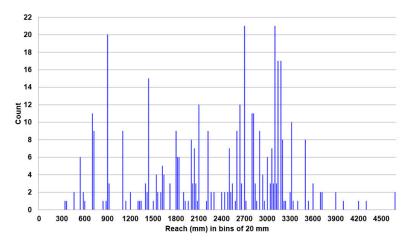


Figure 14. A bar chart histogram of the distribution of reach of industrial robots in bins of 20 mm.

According to Figure 15, the reach of cobots centres around 900 mm and 1400 mm, and the mean reach falls in the middle of them. It is notable that, according to Tables 3 and 4, the mean and median reach of cobots are roughly half of their counterparts in industrial robots. The maximum reach of industrial cobots is 1900 mm, which is even less than half of the maximum reach of industrial robots and reveals a noticeable gap. These data suggest that cobots have shorter reach in comparison to industrial robots, possibly to mitigate risks linked to heavier weight and longer reach during their collaboration with human workers. As mentioned in earlier subsections, by implementing more accurate sensors andenhanced control and AI algorithms, cobots can handle payloads to farther distances more safely and cautiously beside humans. This advancement can result in cobots with extended reach in the future.

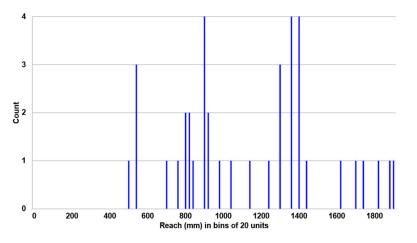


Figure 15. A bar chart histogram of the distribution of reach of industrial cobots in bins of 20 mm.

3.5. Distribution of the A Factor

In order to establish a metric for evaluating the efficiency of a wide range of industrial robots and cobots, the A factor is presented in this work. Its formula is indicated in Equation (1).

$$A_{factor} = \frac{(Payload) \ (Reach)}{Weight} \tag{1}$$

A similar factor has been proposed by [7] to assess the efficiency and performance of robotic grippers based on their force, stroke, and weight. This factor is deemed applicable to robots as well, consisting of two beneficial components: payload/weight ratio, where a higher value results in less depreciation and energy consumption (as the robot carries less weight to manipulate a payload), and reach. Furthermore, as reach increases, maintaining a high payload/weight ratio becomes more challenging; hence, robots with lower payload/weight can compensate for this by achieving a better reach, and vice versa. So, incorporating these three specifications into a single factor can be an appropriate measurement of the efficiency and performance of an industrial robot or cobot. However, the inclusion of more specifications, such as repeatability and maximum angular speed, can make the factor more comprehensive.

Table 2 indicates that the median of the A factor is 16% less than the mean, and as illustrated in Figure 16, the data is skewed to the right. Consequently, the distribution of this factor is denser on the left.

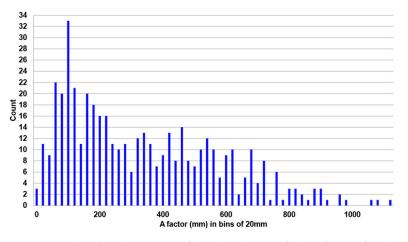


Figure 16. A bar chart histogram of the distribution of the A factor of industrial robots and cobots in bins of 20 mm.

According to Figure 17, characterised by a higher slope at the beginning and the data previously mentioned, the A factor for the majority of the robots is in the lower range. This can be attributed to the fact that maintaining the ratio of payload/weight, in addition to having high reach, is more challenging for heavier robots. Conversely, lighter robots struggle to have a high reach capacity. Furthermore, according to Figure 17, 40% of robots have an A factor of less than 200, although the maximum value of the A factor is 1131 (Kuka KR 800 R2800-2).

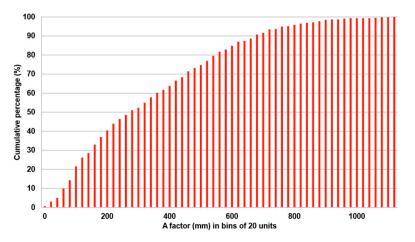


Figure 17. A cumulative percentage bar chart of the distribution of the A factor of industrial robots and cobots in bins of 20 mm.

The standard deviation of the A factor for the total of industrial robots and cobots (σ_A) is 240.8, and the mean (μ_A) is 346.5. In light of the characteristics of the A factor distribution discussed in this subsection, it can be assumed that robots with an A factor of less than $\mu_A - \sigma_A = 105.7$ can be categorised as inefficient robots based on this factor, while robots

with an A factor exceeding $\mu_A + 2 \sigma_A = 828.1$ can be classified as outlier robots. In addition, robots with an A factor falling within the range of $\mu_A - \sigma_A = 105.7$ and $\mu_A + 2 \sigma_A = 828.1$ can be labelled as efficient and appropriate industrial robots and cobots, according to this factor.

Generally, in normal distributions, the range between $\mu - \sigma$ and $\mu + \sigma$ is of high importance due to including more significant data and excluding extreme data. However, because of the right-skewed distribution of the A factor, the range is defined between $\mu - \sigma$ and $\mu + 2\sigma$. It is noteworthy that other robot selection methods mentioned in the Introduction section have some settings to be adjusted manually, which makes it reasonable to establish this range based on the observed distribution of the factor. Outlier robots are more likely to struggle to maintain all the maximum specifications at the same time. Since the technology level of the robots from these market-leading companies is the same, presenting a robot that outstandingly outperforms the other robots may be less probable. They could be well-designed robots capable of satisfying the maximum specifications simultaneously, but the likelihood is lower. Therefore, outlier robots can be set aside in robot selections, as well as less efficient robots. The idea of detecting and excluding outlier robots in robot selection has been presented in [10] for 27 robots.

Based on this factor, from the total of 455 industrial robots and cobots (416 industrial robots and 39 industrial cobots), 366 (332 industrial robots and 34 industrial cobots) are categorised as efficient, 73 (68 industrial robots and 5 industrial cobots) as inefficient, and 16 (16 industrial robots and 0 industrial cobots) as outliers.

Given the information presented in Table 3, the median of the A factor is 16% below the mean value in industrial robots, and as shown in Figure 18, the A factor of industrial robots is also right-skewed. Thus, the data is more concentrated on the left. As discussed previously, in accordance with the A factor, among the total of 416 industrial robots, 332 (80%) are classified as efficient, 68 (16%) as inefficient, and 16 (4%) as outliers.

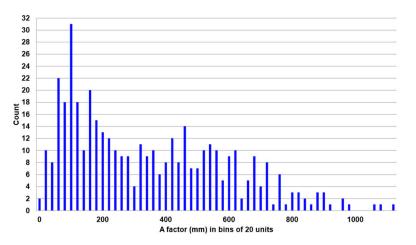


Figure 18. A bar chart histogram of the distribution of the A factor of industrial robots in bins of 20 mm.

Referring to Table 4, the mean of the A factor for industrial cobots is 8% less than the median. Figure 19 also illustrates a right-skewed data distribution; hence, both sources suggest the data is denser on the left, similar to industrial robots. Based on A factor investigated previously, among the total of 39 industrial robots, 34 (87%) are considered efficient, 5 (13%) are inefficient, and there were no outliers. These data underscore the close efficiency alignment between industrial cobots and robots, indicating that the A factor does not significantly differentiate between the two types.

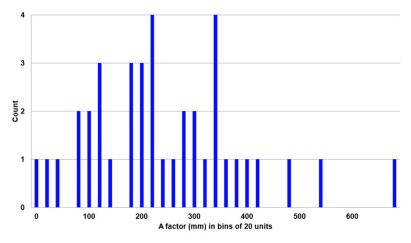


Figure 19. A bar chart histogram of the distribution of A factor of industrial cobots in bins of 20 mm.

3.6. Distribution of Repeatability

There are three key concepts regarding robotic precision and calibration: resolution, accuracy, and repeatability. Position resolution refers to the minimum movement a robot can perform [26]. ISO 9283 [27] defines position accuracy for manipulating robots as "the deviation between a command pose and the mean of the attained poses when approaching the command pose from the same direction". Additionally, it explains position repeatability as "the closeness of agreement between the attained poses after n repeat visits to the same command pose in the same direction". Repeatability is mostly emphasised and measured for industrial robots and cobots since they are typically required to do a task repeatedly. Generally, repeatability is affected by accuracy, and accuracy is influenced by resolution. It should be noted that orientation repeatability has not been mentioned on the datasheet of the target robots.

Given that Table 2 mentions the median repeatability is 28% below the mean value, and according to Figure 20, which demonstrates that the data is skewed to the right for industrial robots and cobots, it can be indicated that the data is more concentrated on the left. Moreover, Figure 20 reveals a notable focus on the repeatability of 0.05 mm.

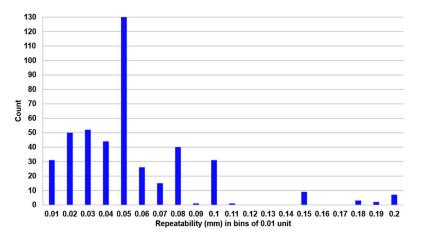


Figure 20. A bar chart histogram of the distribution of repeatability of industrial robots and cobots in bins of 0.01 mm, up to 0.2 mm.

Based on Figure 21, 70% of industrial robots and cobots have repeatability equal to or better than 0.05 mm. All these data collectively indicate that the industry prioritises robots exhibiting better repeatability. This may be attributed to the prevalent applications of industrial robots and cobots that are manipulating lighter and more delicate objects, requiring higher repeatability.

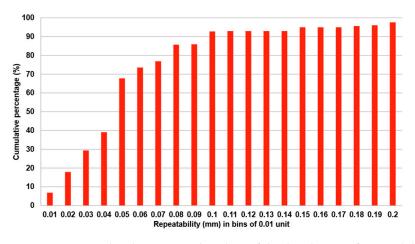


Figure 21. A cumulated percentage bar chart of the distribution of repeatability of industrial robots and cobots in bins of 0.01 mm, up to 0.2 mm.

As per Table 3, the median repeatability of industrial robots is 28% below the mean (like the mixed total of industrial robots and cobots). Additionally, as presented in Figure 22, the data is right-skewed; therefore, both sources indicate that the data is denser on the left. Furthermore, Figure 22 shows that the data is focused at 0.05 mm for industrial robots. Since, high repeatability is of high importance for industrial robots, especially the ones engaged in welding and machining tasks, which mostly include drilling, cutting, and milling.

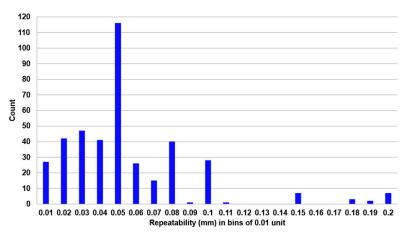


Figure 22. A bar chart histogram of the distribution of repeatability of industrial robots in bins of 0.01 mm, up to 0.2 mm.

Based on Table 4, the median repeatability for industrial cobots is 17% below their mean, and as shown in Figure 23, the data is skewed to the right. Consequently, it can be concluded that the data is more clustered on the left. The predominant value for repeatability of industrial cobots is 0.05 mm, mirroring industrial robots. The mean repeatability of cobots excels that of industrial robots. This can be ascribed to shorter reach, lighter weight, and lower payload capacity of industrial cobots compared to industrial robots, as discussed in the previous subsections. Therefore, it is easier for cobots to achieve better repeatability.

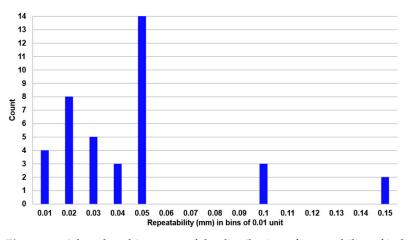


Figure 23. A bar chart histogram of the distribution of repeatability of industrial cobots in bins of 0.01 mm.

3.7. Distribution of B Factor

To devise a more comprehensive factor to assess the efficiency of a wide range of industrial robots and cobots, the B factor is introduced in this work. This factor not only incorporates repeatability but also payload capacity, weight and reach, considered in A factor. The formula for the B factor is exhibited in Equation (2).

$$B_{factor} = \frac{(Payload) (Reach)}{(Weight)(Repeatability)}$$
(2)

This factor includes three beneficial components, including payload/weight ratio, where a higher value leads to less depreciation and energy consumption, reach, as mentioned for the A factor, and repeatability. Furthermore, as reach increases, maintaining a high payload/weight ratio and repeatability typically becomes more difficult. Hence, robots with a lower payload/weight ratio or repeatability can compensate for this by achieving a better reach and vice versa. A good example of this is welding robots, whose payload/weight ratio is mostly lower than those of general industrial robots. These robots can offset this ratio by exhibiting better reach and repeatability. If a welding robot has a low B factor, a general robot satisfying the needed specifications and having a better B factor can replace it. Thus, including these four specifications into a single factor can be a suitable assessment of the efficiency and performance of an industrial robot or cobot. However, to create a more inclusive factor, more specifications, such as the average maximum angular speed, can be taken into account.

Referring to Table 2, the median of the B factor is 9% less than the mean, and as presented in Figure 24, the data distribution is skewed to the right. Therefore, both references propose that the data is more concentrated on the left. However, the B factor displays a more symmetric and less skewed distribution than the A factor (the median of the A factor is 16% more than its mean).

Based on Figure 25, which demonstrates initially a relatively continuous higher slope, 40% of robots have a B factor of less than 5200 even though the maximum value of the B factor is 47,237 (Fanuc LR Mate 200 iD 14L). According to all these indications, the B factor of most of the robots in the industry tends to be in the lower extreme. This may be ascribed to the challenge of maintaining repeatability as reach increases. The possible reason is that the reach multiplies by the angle error of motors and amplifies position errors. On the other hand, the focus of the industry is on robots with higher reach; hence, making robots more accurate is more challenging. Additionally, keeping all the elements of repeatability, reach, and payload/weight ratio is demanding.

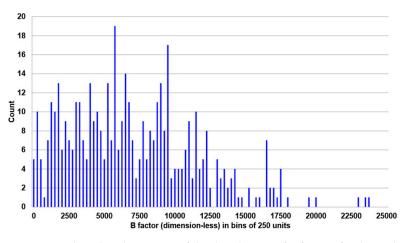
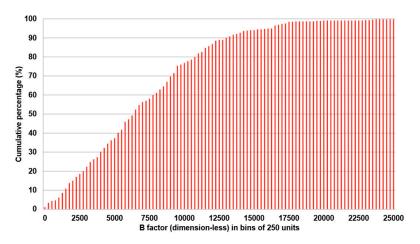
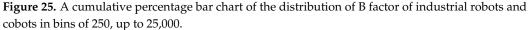


Figure 24. A bar chart histogram of the distribution of B factor of industrial robots and cobots in bins 250, up to 25,000.





The standard deviation of the B factor for the total of industrial robots and cobots (σ_B) is 4895.2, and the mean (μ_B) is 7250.2. By considering the characteristics of the B factor distribution investigated in this subsection, it is proposed that robots with a B factor of less than $\mu_B - \sigma_B = 2355.0$ can be labelled as inefficient robots considering this factor, while robots with a B factor exceeding $\mu_B + 2 \sigma_B = 17,040.6$ can be classified as outlier robots. In addition, robots with a B factor falling within the range of $\mu_B - \sigma_B = 2355.0$ and $\mu_B + 2 \sigma_B = 17,040.6$ can be labelled as efficient and appropriate industrial robots and cobots according to this factor.

Generally, in normal distributions, the interval between $\mu - \sigma$ and $\mu + \sigma$ is deemed an important span due to encompassing more significant data and excluding extraordinary values. However, since the distribution of the B factor is skewed to the right, the range is defined between $\mu - \sigma$ and $\mu + 2 \sigma$. It is noteworthy that other robot selection approaches indicated in the Introduction section require some manual adjustments, which makes it reasonable to establish this range based on the observed distribution of the factor.

Through considering this factor, from the total of 453 industrial robots and cobots, 368 (338 industrial robots and 30 industrial cobots) are labelled as efficient, 71 (65 industrial robots and 6 industrial cobots) as inefficient and 14 (11 industrial robots and 3 industrial cobots) as outliers. These numbers are relatively close to what A factor reports.

Table 3 shows that the median of the B factor of industrial robots is lower than the mean by 9%, and Figure 26 displays a right-skewed distribution for this factor. Consequently, the data is denser on the left, mirroring the combined total of industrial robots and cobots. As

investigated previously, based on the B factor, among the total of 414 industrial robots, 338 (82%) are classified as efficient, 65 (16%) are inefficient, and 11 (3%) are outliers.

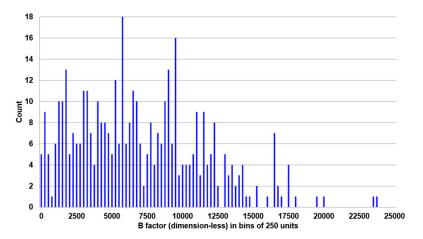
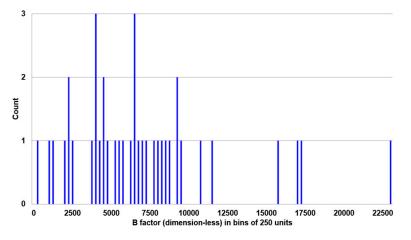
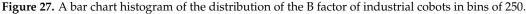


Figure 26. A bar chart histogram of the distribution of B factor of industrial robots in bins of 250 and up to 25,000.

As per Table 4, which shows that the median of the B factor for industrial cobots is approximately 8% below the median, and based on Figure 27, the data is skewed to the right. Therefore, based on both sources, the data is denser on the left, similar to industrial robots. As discussed earlier, by considering the B factor, out of the total of 39 industrial cobots, 30 (77%) are considered efficient, 6 (15%) are inefficient, and 3 (8%) are outliers. These percentages imply that the efficiency and performance of industrial cobots and robots are close to each other, and this factor is neutral in distinguishing between an industrial robot and a cobot.

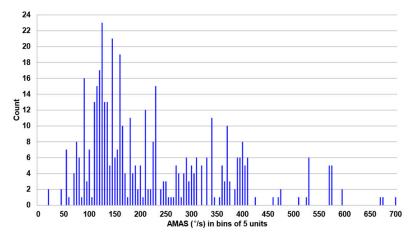




3.8. Distribution of Average Maximum Angular Speed (AMAS)

The angular speed of a robot is a key factor in its cycle time, which holds greater significance than the linear speed at its end. This is because the angular positions of joints (motors) at the beginning of each cycle (loop) are the same as those of the previous cycle; hence, a specific angular trajectory should be completed for each cycle. Consequently, angular speed directly results in a shorter cycle time. To determine the priority of the industry regarding the cycle time of articulated robots, some statistical analyses are conducted on the average maximum angular speed (AMAS) of robots, as well as other specifications.

Figure 28 demonstrates a right-skewed bar chart histogram of the AMAS for the mixed total of industrial robots and cobots. Observing this histogram and referencing Table 2, which highlights the median AMAS is less than the mean value by 23%, it can be concluded



that the AMAS distribution is more concentrated on the left side. Moreover, from Figure 28, the focal point of the industry and the centre of the dense area is around 150° /s.

Figure 28. A bar chart histogram of the distribution of the average maximum angular speed of industrial robots and cobots in bins of $5^{\circ}/s$.

According to Figure 29, showing the cumulative percentages of average maximum angular velocity, 40% of industrial robots and cobots exhibit an AMAS value less than 150°/s. All these data collectively indicate that the prominent focus of the industry and robot makers is on articulated robots with lower average maximum angular speed values. The reason lies in the use of gearboxes in articulated robots, which lower the speed to increase the torque and stability. Gearbox types in robotics applications are mostly planetary, cycloid, and harmonic, which offer gearbox ratios in the range of 1/4 to 1/200 [28]. Implementing more advanced motor technologies in the future holds the potential for motors with simultaneous high speed and torque. This advancement is expected to result in an increase in the maximum angular speed and a corresponding reduction in the cycle time of industrial robots and cobots. Another reason is that in applications where speed is pivotal, delta and SCARA industrial robots are usually preferred over articulated ones. Thus, high angular speed is not regarded as a priority for articulated industrial robots and cobots.

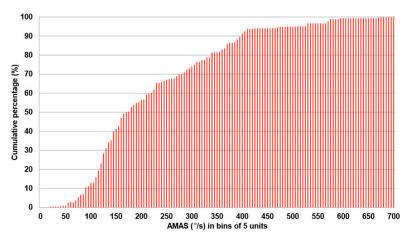
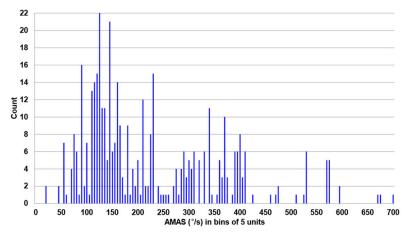


Figure 29. A cumulative percentage bar chart of the distribution of repeatability of industrial robots and cobots in bins of $5^{\circ}/s$.

Table 3 shows that the mean AMAS of industrial robots is roughly 24% less than the mean value, and Figure 30 exhibits that the distribution of the data is skewed to the right. Both sources indicate that the AMAS of industrial robots, along with the entire



robot dataset, are denser on the left. Furthermore, as depicted in Figure 30, the AMAS of industrial robots centres around 150° /s, like the whole robots.

Figure 30. A bar chart histogram of the distribution of the average maximum angular speed of industrial robots in bins of $5^{\circ}/s$.

It is noteworthy that based on information from Tables 3 and 4, the mean and median AMAS values of industrial robots are close to those of cobots. Additionally, information from Figures 30 and 31 indicate that thedata concentration around 150°/s is a common characteristic for both industrial cobots and robots. These results suggest that cobots may be capable of substituting industrial robots in tasks requiring average or low angular speed.

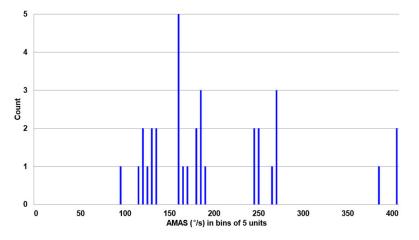


Figure 31. A bar chart histogram of the distribution of the average maximum angular speed of industrial cobots in bins of $5^{\circ}/s$.

3.9. Distribution of C Factor

To obtain a more inclusive factor to assess the efficiency and operation of a broad range of industrial robots and cobots, the C factor, as the improved version of the B factor, is proposed in this paper. This factor considers AMAS alongside the specifications of payload capacity, weight, reach, and repeatability investigated by the B factor. Equation (3) delineates the formulation of the C factor.

$$C_{factor} = \frac{(Payload) (Reach) (AMAS)}{1000 (Weight) (Repeatability)}$$
(3)

In Equation (3), AMAS stands for the average of maximum angular speed. This factor consists of three useful elements: payload/weight ratio (where a higher value results in reduced depreciation and enhanced energy efficiency), repeatability, and AMAS. Furthermore, as reach increases, achieving a high payload/weight ratio, repeatability, and

angular speed generally becomes more demanding. Consequently, robots with lower payload/weight ratios, repeatability, or angular speed can compensate for this disadvantage by demonstrating a better reach and vice versa.

Moreover, robots with lower reach, lower payload/weight ratio, or lower repeatability can make up for them by demonstrating higher angular speed (lower cycle time). An illustrative instance of this is fast pick-and-place articulated robots, which typically have a lower payload/weight ratio and reach compared to general industrial robots. These robots can offset these shortcomings by having better repeatability and angular speed. The application of robots is not considered in factors A, B, and C because a more efficient general robot can replace a lower-efficiency robot designed for specific tasks, such as painting, welding, or palletising. For example, if a palletising robot has a low C factor, a general-purpose robot that meets the required specifications and has a higher C factor can serve as an effective replacement. Hence, the inclusion of these five specifications into a factor can stand as a comprehensive evaluation of the efficiency and capability of industrial robots and cobots.

However, by investigating more specifications, such as cost, lifetime, and warranty, more comprehensive factors can be derived. However, these specifications are out of the scope of this paper and are usually not available in datasheets. Even determining the average maximum angular speed of robots poses challenges, as not all robots have datasheets specifying the maximum angular speed of their joints (in the datasheet of 8 out of 455 industrial robots and cobots of this project, the maximum angular speed of the joints has not been mentioned).

Given the data in Table 2, the median of the C factor is 25% below the mean value (more than what was calculated for the factors A and B), and according to the right-skewed distribution illustrated in Figure 32, the data points are denser at the left.

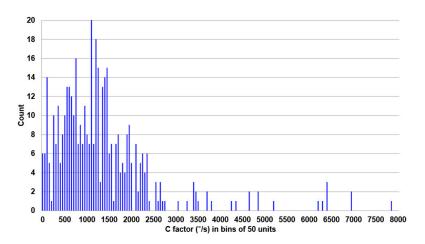


Figure 32. A bar chart histogram of the distribution of the C factor of industrial robots and cobots in bins of 50 deg/s, up to 8000.

According to Figure 33, 40% of robots have a C factor of less than 900, even though the maximum value of the C factor is 12,541.4 (Fanuc LR Mate 200 iD 7L). Given the information in Figure 33, which initially shows an approximately continuous steeper slope, and the previously mentioned data distributions, the C factor for most of the robots in the industry falls on the lower side. This is attributed to the increased difficulty in obtaining high angular speed as reach or payload capacity increases, primarily due to the added weight of links. Moreover, to have better repeatability, the control system of a robot must finely adjust its movements, particularly at critical points in its operation, such as when approaching the desired position. Therefore, having better repeatability may negatively affect maximum angular speed. Therefore, while the focus of the industry is on robots with higher reach and better repeatability, making articulated robots faster remains challenging.

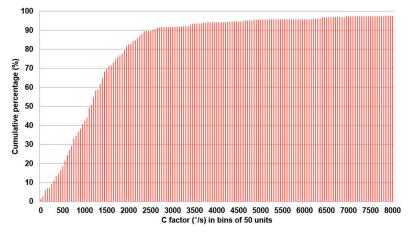


Figure 33. A cumulative percentage bar chart of the distribution of the C factor of industrial robots and cobots in bins of $50^{\circ}/s$, up to 8000.

The standard deviation of the C factor of the combined total of industrial robots and cobots (σ_C) is 1759.2, and the mean (μ_C) is 1566.9. Based on the distribution features of the C factor surveyed in this subsection, it is suggested that robots possessing a C factor of less than $\mu_C - 0.75 \sigma_C = 247.5$ can be classified as inefficient robots, while robots surpassing $\mu_C + 2.25 \sigma_C = 5525.1$ can be categorised as outlier robots, considering this factor. Furthermore, robots with a C factor within the range of $\mu_C - 0.75 \sigma_C = 247.5$ and $\mu_C + 2.25 \sigma_C = 5525.1$ are labelled as efficient and appropriate industrial robots and cobots in accordance with this factor.

Typically, in normal distributions, the range between $\mu - \sigma$ and $\mu + \sigma$ is highlighted as an important interval because of including more data of high importance and precluding extraordinary values. Nevertheless, due to the right-skewed distribution of the C factor, the range is specified between $\mu - 0.75\sigma$ and $\mu + 2.25\sigma$. Unlike the A and B factors, considering $\mu - \sigma$ as the lower bound is not suitable because it is negative; therefore, $\mu - 0.75\sigma$ is specified instead. To keep the range length at 3σ , similar to the A and B factors, the upper bound of the C factor is selected as $\mu + 2.25\sigma$.

According to this factor, out of the total of 445 industrial robots and cobots, 394 (362 industrial robots and 32 industrial cobots) are classified as efficient, 32 (31 industrial robots and 1 industrial cobot) as inefficient, and 19 (19 industrial robots and no industrial cobot) as outliers. The count of inefficient robots classified by this factor is fewer than those identified by the A and B factors; conversely, the number of outliers is higher than the A and B factors.

Referring to Table 3, the median of the C factor is 27% less than the mean value, and based on Figure 34, the C factor for industrial robots is skewed to the right. Consequently, the data for industrial robots is more concentrated on the left, as well, because of the existence of some outliers at the very right end. Based on what was previously discussed for the C factor, from the total of 412 industrial robots, 362 (88%) are categorised as efficient, 31 as inefficient (7%), and 19 (5%) as outliers.

Table 4 illustrates the median of the C factor for industrial cobots is roughly close to the mean value, and based on Figure 35, the data is not significantly skewed. According to the previous discussion, from the total of 33 industrial robots, 32 (97%) are considered efficient, 1 (3%) is inefficient, and none are identified as outliers. These percentages imply that, according to the C factor, the efficiency and performance of industrial cobots surpass industrial robots. Having no outliers improved the percentage of efficient industrial robots in comparison to industrial robots. One of the reasons is the maximum angular speed of industrial cobots is 400, and the one for industrial robots is 700, which is 75% higher and leads to an increased number of extreme data points.

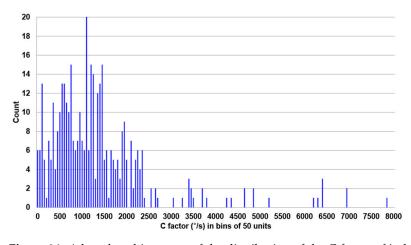


Figure 34. A bar chart histogram of the distribution of the C factor of industrial robots in bins of 50° /s, up to 8000.

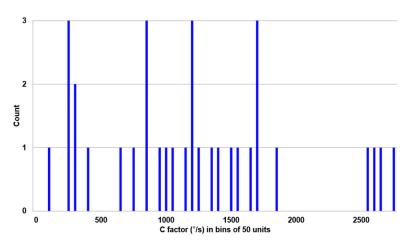


Figure 35. A bar chart histogram of the distribution of the C factor of industrial cobots in bins of $50^{\circ}/s$.

3.10. Distribution of Degrees of Freedom (DOF)

In light of Tables 2–4, the median and mean DOF of the whole of industrial robots and cobots are 6. As exhibited in Figure 36, the focal point of the DOF for industrial robots and cobots is 6.

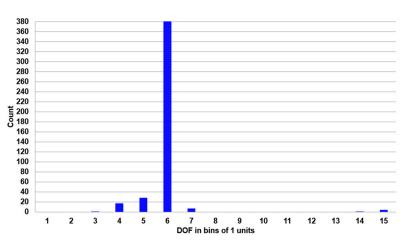


Figure 36. A bar chart histogram of the distribution of DOF of industrial robots and cobots in bins of 1.

According to Figure 37, around 88% of industrial robots and cobots feature six DOF. These data together show that the industry emphasises robots with six DOF. This is because robots predominantly manipulate objects possessing six degrees of freedom (three for position and three for orientation) in the 3D space. Robots with fewer than six DOF may face challenges to achieve desired positions and orientations. On the other hand, having a DOF of more than six results in extra costs and more complicated computations due to the existence of infinite configurations for the robot to get the object to a specific desired position and orientation. Moreover, there are instances of industrial robots and cobots with 14 and 15 degrees of freedom, which are robots with two arms.

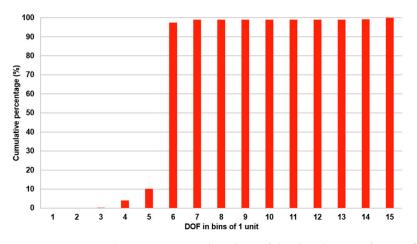


Figure 37. A cumulative percentage bar chart of the distribution of DOF of industrial robots and cobots in bins of 1 unit.

Given the information in Figure 38, 364 out of 455 (80%) industrial robots feature 6 degrees of freedom, which is the centre point of the DOF for the combined total of industrial robots and cobots, as well. There are some robots with a DOF of less than six that can be used in applications in which the orientation of the manipulated object around an axis is limited or constrained as these robots are under-actuated.

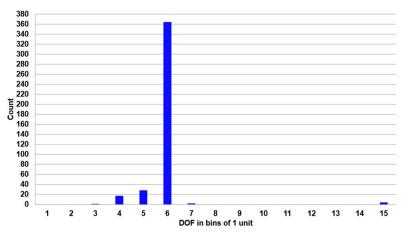


Figure 38. A bar chart histogram of the distribution of DOF of industrial robots in bins of 1.

According to Figure 39, 32 out of 38 (8%) industrial cobots have a DOF of six, which is the centrepiece of the DOF of industrial robots as well. Notably, there is no cobot with a DOF less than six among the data. This can be attributed to the design of cobots, intended for general applications where complete manipulation of objects is generally necessary. However, some industrial robots are specifically designed for niche applications, where having a DOF below six enables them to fulfil their duties and also makes them more affordable.

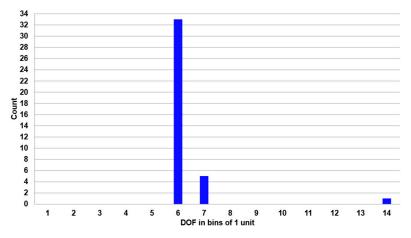


Figure 39. A bar chart histogram of the distribution of DOF of industrial cobots in bins of 1.

3.11. Data Resampling and Validation

For the statistical analysis of the A, B, and C factors, two distinct attributions stand out: (i) the sample data does not follow the normal distribution of traditional statistics, and (ii) data captured from companies ABB, Kuka, Fanuc, Yaskawa, and Universal Robots are representative of approximately 58% of the market share. Taking into account the sampling method, variability, and non-sampling errors, it is assumed that the large sample of this work accurately represents the population as a whole. Based on these two attributions, a bootstrapped method was performed to estimate the sampling distribution. With the software package Statistics101 [29], the original dataset was resampled 500,000 times with 455 (A factor), 453 (B factor), and 445 (C factor) observations in each run. A 95% bootstrapped confidence interval was applied to the sampling distribution of means for the A, B, and C factors, with the results being [324, 368], [6798, 7700], and [1409, 1736], respectively. Thus, there is a 95% confidence that each factor's population mean falls within the respective ranges. These ranges indicate that, with a 95% probability, the difference between the mean of the factors for this study and factors for the whole population is 11% or less, which is deemed an acceptable margin.

4. Data Comparison and Trends

To find trends and relations among the specifications to understand the limitations of articulated robots and the design purposes of the robot makers, as well as to predict robot specifications based on required ones, the linear regression method is utilised. The equations of this method have been obtained using the least square method to predict *Y*—as the dependent parameter—based on *X* for a given set of data plotted on an *X*-*Y* plane. According to this method, the regression line should pass through \overline{X} and \overline{Y} , representing the mean of data along the *X* and *Y* axes. The equation of the correlation coefficient for this line, which measures the strength of the linear relationship between two variables, is expressed in Equation (4) [30].

$$r = \frac{1}{N} \frac{\sum_{i=1}^{N} \left(X_i - \overline{X} \right) \left(Y_i - \overline{Y} \right)}{S_X S_Y} \tag{4}$$

In which N is the number of data points, S_X is the standard deviation of data along the X axis, and S_Y is the standard deviation along the Y axis. A correlation coefficient with a magnitude surpassing 0.7 shows a strong relation between the two variables [31] and may convey a meaningful message. Additionally, the slope of this line (m_{reg}) can be calculated according to Equation (5) [30].

1

$$n_{reg} = r \frac{S_Y}{S_X} \tag{5}$$

As mentioned previously, since the fittest regression line goes through \overline{X} and \overline{Y} , the value of intercept can consequently be calculated as Equation (6).

$$b_{reg} = \overline{Y} - m_{reg}\overline{X} \tag{6}$$

Now that the regression equations are prepared, they will be used to identify relations between specifications to find possible trends. In some cases, a mathematical function such as ln(x), e^x , \sqrt{x} can be applied to one or both axes to even discern a nonlinear relation in the data.

4.1. Reach vs. Weight

The equation of the regression line for all the robots, as depicted in Figure 40, to estimate weight based on reach is provided in Equation (7).

$$ln(weight) = 0.00151 \ reach + 2.7454 \tag{7}$$

It should be noted that in this equation, *reach* is in millimetres. The correlation coefficient for all the robots is 0.92, for Kuka is 0.93, for UR is 0.94, for ABB is 0.92, for Fanuc is 0.92, and for Yaskawa is 0.92. These correlations reveal a strong exponential relation between the *reach* and *weight* of articulated robots. It is noteworthy that *weight* (not its logarithm) and *reach* do not exhibit a stronger linear correlation, which is 0.68. However, a regression between *reach* and the \sqrt{weight} exhibits a strong correlation coefficient of 0.87, indicating a linear relation between *reach*² and *weight*. This further indicates a relation between *weight* and higher levels of *reach*.

The rationale behind this is that to increase the *reach* by x times, the length of each link should increase by x times, thereby increasing the *weight* by x times. Therefore, the torque on the robot increases by x^2 times. Furthermore, the two cross-sectional dimensions of the links should increase to endure under the added torque and *weight*, which leads to an increase in *weight* much more than x times. Moreover, the motors and power transmission systems should now apply a torque of more than x^2 times stronger. Consequently, the combination of motors and transmission systems should get much stronger and heavier. By considering these facts, if the *reach* increases, the *weight* increases at a higher rate. The same pattern has been observed in some natural phenomena. For example, ref. [32] has revealed a linear relation between *weight* and *length*³ in quadrupedal terrestrial tetrapods. Hence, industries should be aware that opting for a greater reach requires a much heavier robot, which leads to elevated energy consumption, costs, and transportation charges. It is notable that the companies demonstrate a close performance in terms of reach-to-ln(weight) ratio.

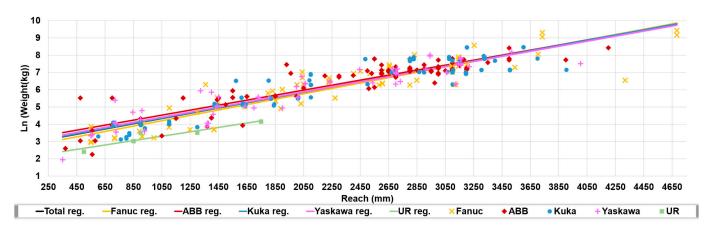


Figure 40. The distribution and regression of *reach* versus the natural logarithm of *weight* by manufacturer (reg. stands for regression).

4.2. Reach vs. AMAS

In the preceding subsection, it was noted that when *reach* increases by x times, motors and power transmission systems should apply at least x^2 times higher torque and links should endure this torque. In addition to reinforcing the motors, robot makers can also decrease the gearbox ratio to supply the extra torque which results in lower angular speed. Hence, a regression analysis between *reach* and average maximum angular speed (*AMAS*) is conducted to find a relation. The equation of the regression line for all the robots, presented in Figure 41, to estimate the average maximum angular speed based on *reach* is indicated in Equation (8).

$$AMAS = -0.106 Reach + 462.57$$
 (8)

The correlation coefficient for all the robots is -0.75, for Kuka is -0.79, for UR is -0.64, for ABB is -0.85, for Fanuc is -0.79, and for Yaskawa is -0.68. The correlation coefficients exhibit a strong negative linear relation between the average maximum angular speed and the *reach* of the robots.

The obtained results mention that robot makers partially compensate for the increased required torque caused by extended *reach* and subsequently increased weight by reducing the *AMAS*. They may compensate for the remaining torque by making motors stronger and heavier.

Given Equations (7) and (8), as *reach* affects weight exponentially and *AMAS* linearly, there exists an exponential relation between *AMAS* (as the X-axis due to be a desirable parameter) and ln(weight) as Y axis with a correlation coefficient of -0.78. However, this does not necessarily show a direct causation relation between them, as *reach* serves as a confounding factor here. For example, it cannot be inferred that to achieve a higher angular speed, robot makers necessarily decrease the *weight* exponentially. Because as discussed in the previous section, having high angular speed is not a top priority for articulated robots in the industry, and a dramatic decrease in weight results in a significant reduction in payload capacity due to the linear relation between payload capacity and weight, which will be presented in Equation (9).

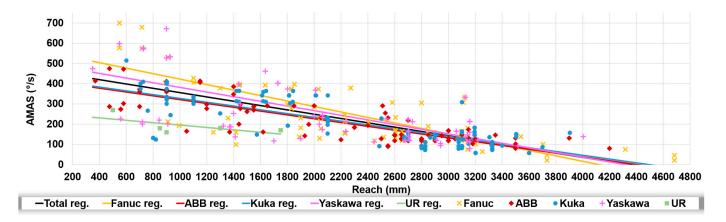


Figure 41. Distribution and regression of *weight* versus *AMAS* by the manufacturer (reg. stands for regression).

4.3. Payload vs. Weight

The equation of the regression line for all the robots, illustrated in Figures 42 and 43, to predict weight based on payload capacity is illustrated in Equation (9).

$$weight = 4.749 \ payload + 186.66 \tag{9}$$

The correlation coefficient for all the robots is 0.91, for Kuka is 0.94, for UR is 0.92, for ABB is 0.89, for Fanuc is 0.95, and for Yaskawa is 0.88. The correlations indicate a strong positive linear relation between the weight and *payload capacity* of the robots. The reason

for this could be that when the *payload* increases by x times, the torque only increases by x times, causing the links to get heavier linearly (not exponentially, as observed in the case of an increase in reach). Thereby, industries should be mindful that selecting a higher *payload capacity* requires a heavier robot, which leads to increased energy consumption, costs, and transportation charges. Additionally, it seems that increasing *payload capacity* is relatively easier for robot makers compared to increasing the reach. However, because of the needs of the industry, there is a prevalent preference for higher reach over higher *payload capacity*. It is noteworthy that Kuka exhibits the highest rate of *payload/weight*, which is 1/3.86 (the slope of its regression line), and Fanuc presents the lowest, which is 1/5.88. It is plausible that Fanuc was more cautious and prudent about reporting its *payload capacity*, or Kuka may really exhibit a remarkable payload-to-weight ratio.

Other pairs of specifications can be investigated. However, in this work, relations exhibiting correlation coefficients less than 0.7, even after applying mathematical transformations such as ln(x), e^x and \sqrt{x} , were disregarded. Some of these relations were between *reach* and *repeatability* (*reach* and *repeatability*: 0.27, *reach* and ln(repeatability): 0.57, *reach* and $\sqrt{repeatability}$: 0.42, *reach* and $e^{repeatability}$: 0.23, \sqrt{reach} and *repeatability*: 0.25), *repeatability* and *weight* (*repeatability* and *weight*: 0.32, *repeatability* and ln(weight): 0.29, *repeatability* and \sqrt{weight} : 0.33, and $e^{repeatability}$ and *weight*: 0.27).

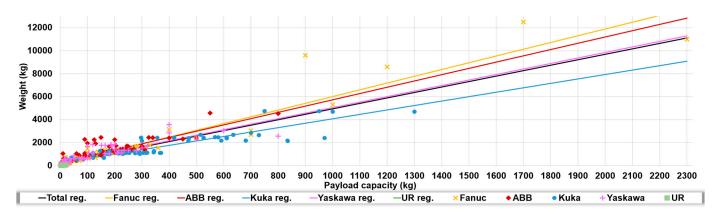


Figure 42. Distribution and regression of payload capacity versus weight by manufacturer (reg. stands for regression).

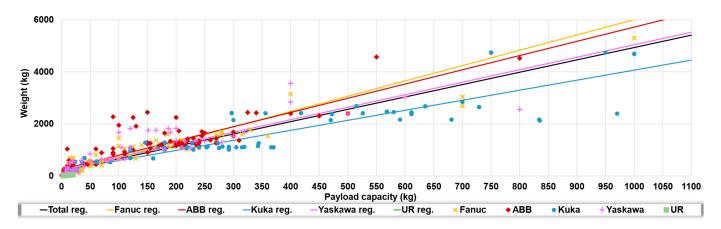


Figure 43. Distribution and regression of *payload capacity* versus *weight* by manufacturer for payload capacity up to 1100 kg (reg. stands for regression).

4.4. A, B and C Factors for Companies

In the previous section, the distribution of each factor was investigated. Now, the distribution of each factor for each company with respect to upper and lower selection bounds is considered.

Based on Figure 44, all the robots of Universal Robots fall within the efficient area based on the A factor. ABB does not have any outliers but exhibits the most inefficient ones (27), followed by Kuka (18), Yaskawa (17), and Fanuc (11), based on the number of inefficient ones identified by the A factor. Kuka has the most outliers (15), Yaskawa has just one outlier, and Fanuc, similar to ABB, has none. Kuka has the most efficient ones (133), and thereafter, Fanuc (90), ABB (78), and Yaskawa (60). Based on Figure 44 and these numbers, although the range of this factor for each company is different, a sensible number of their robots, 80%, lie within the efficient range considering this factor.

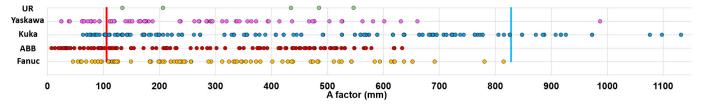


Figure 44. Distribution of the A factor by manufacturer with upper and lower efficiency bounds in red and blue, respectively.

Given Figure 45, like the A factor, all the robots of Universal Robots are within the efficient range based on the B factor. Fanuc has the most outliers (6), followed by Yaskawa (4), Kuka (2), and then ABB (2). Kuka has the most efficient ones (154) based on this factor, succeeded by Fanuc (80), ABB (73), and Yaskawa (56). ABB has the most inefficient ones (28), and then there are Yaskawa (18), Fanuc (15), and Kuka (10) based on the B factor. According to these numbers and Figure 45, although the range of this factor for each company varies, a significant number of their robots, 81%, fall within the efficient range according to this factor.

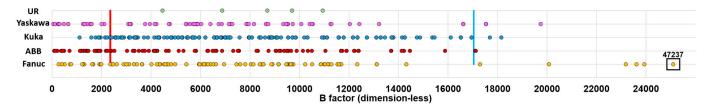


Figure 45. Distribution of the B factor by manufacturer with upper and lower efficiency bounds in red and blue, respectively.

Referring to Figures 46 and 47, akin to the A and B factors, all the robots of Universal Robots are in the efficient range considering the C factor. Kuka has the most efficient ones (166) with no outliers and no inefficient robots. Subsequently, there are ABB (92), Fanuc (70), and Yaskawa (61) based on this factor. Fanuc has the most inefficient ones (13), followed by ABB (10) and Yaskawa (9). Fanuc also has the most outliers (12), succeeded by Yaskawa (7) and ABB (none). According to these numbers and Figure 47, although the range of this factor for each company differs, a notable number of their robots, 88%, are labelled as efficient based on this factor.

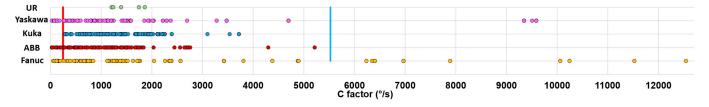


Figure 46. Distribution of the C factor by manufacturer with upper and lower efficiency bounds in red and blue, respectively.

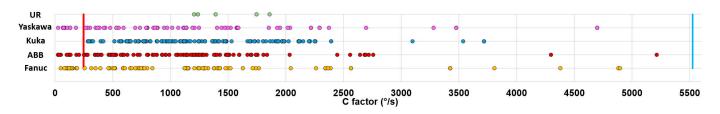


Figure 47. Distribution of the C factor by the manufacturer up to $5600 (^{\circ}/s)$ with upper and lower efficiency bounds in red and blue, respectively.

5. Robot Selection

In the earlier section, three factors were introduced, each categorising around 80–88% of robots as efficient. A proper method to select robots is to gather a list of robots labelled as efficient by all these three factors. This ensures that the opted robot is not identified as inefficient or an outlier by any of these factors. Moreover, individuals seeking to choose an industrial robot or cobot from other companies can calculate the score of the robot based on the A, B, and C factors to determine if it is classified as efficient or not. The range of efficient robots based on the A factor, as obtained in Section 3.5, is between 105.7 and 828.1. Based on the B factor, as calculated in Section 3.7, the range is between 2355.0 and 17,040.6. Finally, based on the C factor, as derived in Section 3.9, the range is between 247.5 and 5525.1.

From the total of 455 industrial robots and cobots, two of them were set aside due to unspecified repeatability in the datasheet, and eight were excluded due to a lack of angular speed information. Consequently, 445 (412 industrial robots and 33 industrial cobots) were examined for the final list of efficient robots. Within this group, 304 units (279 industrial robots and 25 industrial cobots), which account for 68%, were labelled as efficient based on these three factors. According to these numbers, 67% of industrial robots and 75% of industrial cobots were categorised as efficient. The slightly higher percentage for industrial cobots can be ascribed to their versatile design, tailored to cover a wider range of applications, which makes them more adaptable. These efficient robots were those that were not considered inefficient or outliers by any of these factors. The payload range of the efficient robots ranges between 3.0 and 1000.0 kg, weight spans from 11.2 to 5300 kg, reach falls between 500 and 4200 mm, repeatability is between 0.01 and 0.2, average maximum angular speed ranges between 58 and 577, and DOF is between four and seven inclusive. The obtained ranges mention that efficient robots can cover a wide spectrum of applications in the industry. They also note that the selection method is not focused on a specific robot size or type.

As the final step of the robot selection approach, the efficient robots with specifications falling within the desired specification ranges provided by an individual are demonstrated. If the number of output robots is more than one, they are ranked according to their C factor, which is the most comprehensive factor. The flow chart of the entire process of the robot selection method is depicted in Figure 48.

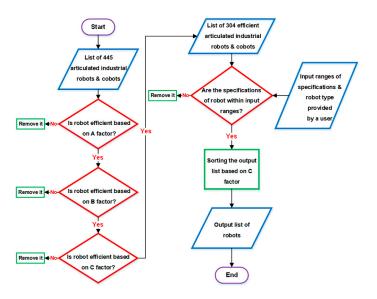


Figure 48. A flowchart of the robot selection method.

It is worth noting that the correlation between the factors does not result in identical outputs from each factor. Specifically, 62 robots are recognised as efficient by factor A but not by factors B or C; 64 robots are identified as efficient by factor B but not by factors A or C; and 90 robots are classified as efficient by factor C but not by factors A or B.

Following this robot selection method, a Python program has been developed and uploaded on GitHub (https://github.com/PeymanAmirii/Robot_Selection, accessed on 18 September 2024). This program takes a range of required specifications and robot types (industrial robot or cobot) and returns a list of efficient robots from the target companies (ABB, Kuka, Fanuc, Yaskawa, and Universal Robots), satisfying the inputs. This program provides users and industries with a tool to select an efficient robot with a proper performance which meets the needed input specifications.

6. Discussion

In this work, physical specifications were taken into account. However, there are other specifications that might significantly impact the selection of a robot and can contribute to devising more comprehensive selection factors. The most crucial one is the price of industrial robots and cobots. The consideration of the price of robots is out of the scope of this paper due to regional variations in price and cost of ownership. Additionally, price was not investigated in the selection algorithm because companies around the world operate with different ranges of budget. The algorithm provides a list of physically efficient robots for users, and then they can choose a robot that fits their budget from the sorted list. Additionally, if a robot is not physically efficient, it should be removed from the final list, regardless of its low price. However, it should be noted that cost may elucidate why some robots possess lower physical efficiency and can be investigated in future works.

Moreover, a useful physical specification to be considered is the footprint or the volume of a robot, especially when space constraints are a concern. While the footprint is commonly mentioned in the datasheets of robots, the volume of robots is rarely provided.

As stated earlier, in this analysis, the payload capacity of a robot is considered as the maximum payload a robot can carry when its centre of mass is at position **0**. However, the payload capacity diminishes as the robot's centre of mass moves farther from the **0**-position due to the additional torque, as shown in Figure 49 for a robot. To make the calculations more comprehensive, the mean of payload, when the centre of mass is at position **0** and the farthest position, can be taken into consideration as the overall payload capacity of a robot.

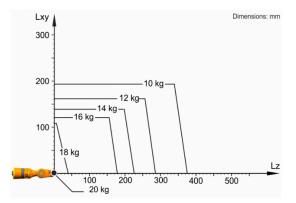


Figure 49. The payload capacity of the industrial robot Kuka KR 16 R1610-2 based on different positions of the centre of mass [33].

According to what was discussed before, repeatability, accuracy, and resolution are different but interconnected concepts. If robot manufacturers specify these three parameters, their mean can provide a more comprehensive measurement of the precision of robots for future studies. Additionally, orientation repeatability is another specification which is not available on the datasheets of robots. This metric is crucial in applications requiring precise angular positioning, such as painting, welding, and assembly.

For most of the robots, each joint has a limited angle range. This limits the reach volume of robots. To enhance the assessment of the reach of a robot, calculating the mean of the maximum reach length and the reach volume (if reported by manufacturers in their datasheets) can facilitate a more inclusive measure. The workspace of an industrial robot with a reported reach of 1.55 m is illustrated in Figure 50. It implies that the robot cannot reach all the points within a distance of 1.55 metres from its base; hence, considering the workspace volume in the measurements can be advantageous.

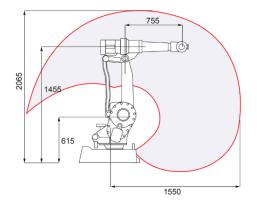


Figure 50. Workspace of the industrial robot ABB IRB 2400 with a reported reach of 1.55 m [34].

In this work, AMAS was employed to approximately reflect the cycle time of industrial robots and cobots. However, simulation software, such as RoboDK v5.8.0, can be utilised to compare the cycle times of different robots more accurately. This simulation software covers a wide range of industrial robots and cobots and provides software-in-the-loop simulation (SITL).

To enhance the robot selection method, other distance-based algorithms, such as K-Nearest Neighbours (KNN), can be deployed to choose a group of efficient robots based on their specifications or efficiency factors. For example, an average robot can be selected based on its specifications, then 60–70% of the closest robots to it can be recognised as efficient robots, and the rest as inefficient and outlier ones. Furthermore, as [35] highlights, any MCDM method is about how to combine several factors or criteria to create a single index for assessing suitability. Therefore, an MCDM method can be employed to obtain a final index from the proposed efficiency factors.

Establishing standard definitions for cobots and outlining safety guidelines for collaborative work with them are of high importance. Although ISO 10218 [36] indicates requirements and guidelines for safe design and provides protective measures and information regarding the use of industrial robots, there is a need for more accurate definitions and standards which are specifically tailored to cobots.

7. Conclusions

The investigation of the distribution of physical specifications revealed that the focus of the industry and robot makers is on articulated industrial robots and cobots characterised by higher reach, lower payload capacity, lower weight, better repeatability, lower angular speed, and six DOF. The possible reason is that prevalent applications in the industry involve manipulating and handling light objects over extended distances, which requires high precision (good repeatability). The decision to keep a lower angular speed aims to ensure higher torque and, consequently, higher sturdiness of articulated robots as their serial structure makes robustness challenging. Additionally, another rationale is that for high-speed applications, SCARA and Delta robots can be employed instead. Industrial robots and cobots with six DOF were preferred because of being fully actuated systems, which results in easier control algorithms and kinematic solutions.

Moreover, the specifications of industrial robots and cobots were also compared to highlight the advantages and disadvantages of industrial cobots over industrial robots. On average, industrial cobots are lighter and possess a lower payload capacity and reach (on average, one-tenth and half those of industrial robots, respectively) than industrial robots. However, their average angular speed (cycle time) is close to the average of industrial robots, and their repeatability is better than that of industrial robots.

Three factors were introduced to assess the efficiency and performance of industrial robots and cobots, intended to be used as standard measures in future works. The range of each efficiency factor varied for each company, but a considerable number of their robots fell into the efficient range based on each factor. A robot selection method based on these three factors was developed, which recognised 68% of the whole studied industrial robots and cobots as efficient and appropriate for industrial purposes and put aside inefficient and outlier robots. Outlier robots are those more likely to fail to properly satisfy all the reported specifications at the same time, as their specifications might have been measured under special conditions. The selected robots cover the range of payload capacity between 3.0 and 1000 kg and a reach range between 0.50 m and 4.20 m, suggesting that the selection method does not focus on a specific robot size. A Python code has been developed and uploaded on GitHub to provide a sorted list of efficient industrial robots and cobots, selected by the selection method, considering the input required specifications. This tool aims to assist industries in choosing articulated robots, meeting their specific needs. Although some robot makers provide some proprietary internal software to assist customers in finding their appropriate robots, the software just considers their own products and does not include those made by other manufacturers.

Pairs of specifications exhibiting a strong correlation coefficient were compared to understand the rationale behind the design choices of robot makers and to estimate their limitations. These comparisons express that the weight of robots increases exponentially as the reach increases, mostly due to the added weight and torque which result from the extended reach. The comparisons indicate that the angular speed of robots linearly decreases with respect to reach. This is ascribed to robot manufacturers intentionally reducing the angular speed through reductive gearboxes to partially make up for the additional torque required as the reach extends.

The weight of robots increases linearly with their payload capacity due to the linear increase in the required torque. Therefore, this implies that industries seeking a higher payload capacity should expect a proportional linear increase in the weight of their potential robot. Additionally, aiming for higher reach results in exponentially heavier robots. On

the other hand, no strong correlation was found between reach and repeatability or weight and repeatability.

Some useful information such as accuracy, resolution, and reach volume were suggested to be included in official datasheets of industrial robots and cobots to have a better understanding and more accurate criterion of their performance. Additionally, the need for establishing standard definitions and guidelines for cobots was outlined.

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Conflicts of Interest: The authors have no relevant financial or non-financial interests to disclose.

Appendix A

Table A1. A list of industrial robots and cobots from Fanuc that were investigated in this work (starred models are cobots).

LR Mate 200 iD 4SH	LR Mate 200 iD 4S	LR Mate 200 iD 4SC	LR Mate 200 iD 7H	LR Mate 200 iD 7C
LR Mate 200 iD 7WP	LR Mate 200 iD	LR Mate 200 iD 7L	LR Mate 200 iD 7LC	LR Mate 200 iD 14L
LR-10 iA 10	M-10 iD 8L	M-10 iD 10L	M-10 iD 12	M-10 iD 12 Dustproof
M-10 iD 12 Foodgrade	M-10 iD 16S	M-20 iD 12L	M-20 iB 25	M-20 iD 25
M-20 iD 25 Foodgrade	M-20 iB 25C	M-20 iB 35S	M-20 iD 35	M-410 iB 140H
M-410 iC 110	M-410 iC 185	M-410 iC 315	M-410 iC 500	M-410 iB 700
M-710 iC 12L	M-710 iC 20L	M-710 iC 20M	M-710 iC 45M	M-710 iC 50S
M-710 iC 50T	M-710 iC 50H	M-710 iC 50	M-710 iC 50E	M-710 iC 70T
M-710 iC 70	M-800 iA 60	M-900 iB 280	M-900 iB 280L	M-900 iB 330L
M-900 iB 360E	M-900 iB 400L	M-900 iB 700E	M-1000 iA	M-2000 iA 900L
M-2000 iA 1200	M-2000 iA 1700L	M-2000 iA 2300	R-1000 iA 80H	R-1000 iA 80F
R-1000 iA 100F	R-1000 iA 120F-7B	R-1000 iA 130F	R-2000 iC 100P	R-2000 iD 100FH
R-2000 iC 125L	R-2000 iC 165F	R-2000 iD 165FH	R-2000 iC 165R	R-2000 iC 190S
R-2000 iC 210F	R-2000 iD 210FH	R-2000 iC 210L	R-2000 iC 210WE	R-2000 iC 210R
R-2000 iC 220U	R-2000 iC 240F	R-2000 iC 270F	R-2000 iC 270R	ARC Mate 50 iD
ARC Mate 50 iD 7L	ARC Mate 100 iD 8L	ARC Mate 100 iD 10L	ARC Mate 100 iD 16S	ARC Mate 100 iD
ARC Mate 120 iD 12L	ARC Mate 120 iD 35	ARC Mate 120 iD	Paint Mate 200 iA 5L	P-40 iA
P-50 iB 10L	P-250 iB 15	P-350 iB 45	P-35 iA Opener	P-1000 iA
CR-4 iA *	CRX-5 iA *	CR-7 iA *	CR-7 iA L *	CRX-10 iA *
CRX-10 iA L *	CR-14 iA L *	CR-15 iA *	CRX-20 iA L *	CRX-25 iA *
CR-35 iB *				

IRB 1010-1.5/0.37	IRB 1090-3.5/0.58	IRB 1100-4/0.475	RB 1100-4/0.58	IRB 1200-7/0.7
IRB 1200-5/0.9	IRB 1200-7/0.7 Hygienic	IRB 1200-5/0.9 Hygienic	IRB 1300-11/0.9	IRB 1300-10/1.15
IRB 1300-7/1.4	IRB 1300-12/1.4	IRB 1410	IRB 1520ID	RB 1600-6/1.2
IRB 1600-6/1.45	IRB 1600-10/1.2	IRB 1600-10/1.45	IRB 1660ID-6/1.55	IRB 1660ID-4/1.55
IRB 2400/10	IRB 2400/16	IRB 2600-20/1.65	IRB 2600-12/1.65	IRB 2600-12/1.85
IRB 2600ID-15/1.85	IRB 2600ID-8/2.00	IRB 4400/60	IRB 4400/L10 IRB 460-110/2.4	
IRB 4600-60/2.05	IRB 4600-45/2.05	IRB 4600-40/2.55	IRB 4600-20/2.50 IRB 5710-110/2	
IRB 5710-90/2.7	IRB5710-90/2.3 LID	IRB 5710-70/2.7 LID	IRB 5720-180/2.6 IRB 5720-125/	
IRB 5720-155/2.6 LID	IRB 5720-90/3.0 LID	IRB 660-180/3.15	IRB 660-250/3.15	IRB 6620
IRB 6650S-90/3.9	IRB 6650S-125/3.5	IRB 6650S-200/3.0	IRB 6660-100/3.3	IRB 6660-130/3.1
IRB 6660-205/1.9	IRB 6700-200/2.60	IRB 6700-155/2.85	IRB 6700-235/2.65	IRB 6700-205/2.80
IRB 6700-175/3.05	IRB 6700-150/3.20	RB 6700-300/2.70	IRB 6700-245/3.00	IRB 6700Inv-300/2.60
IRB 6700Inv-245/2.90	IRB 6710-210/2.65	IRB 6710-200/2.95	IRB 6710-175/2.65 LID	IRB 6710-175/2.95 LID
IRB 6720-240/2.65	IRB 6720-210/2.8	IRB 6720-170/3.1	IRB 6720-215/2.5 LID	IRB 6720-215/2.65 LID
IRB 6720-200/2.8 LID	IRB 6720-150/3.1 LID	IRB 6730-270/2.7	IRB 6730-240/2.9	IRB 6730-210/3.1
IRB 6730-220/2.9 LID	IRB 6730-190/3.1 LID	IRB 6740-310/2.8	IRB 6740-260/3.0	IRB 6740-240/3.2
IRB 6740-270/2.8 LID	IRB 6740-230/3.0 LID	IRB 6740-220/3.2 LID	IRB 6790-235/2.65 IRB 6790-205/2	
IRB 760	IRB 760PT	IRB 7600-500/2.55	IRB 7600-400/2.55 IRB 7600-340/2	
IRB 7600-325/3.10	IRB 7600-150/3.50	IRB 8700-800/3.50	IRB 8700-550/4.20	IRB 52/1.2
IRB 52/1.45	IRB 5500-25	CRB 1300- 11/0.9 *	CRB 1300-10/1.15 *	CRB 1300-7/1.4 *
GoFa 5 *	GoFa 12 *	GoFa 10 *	IRB 14000-0.5/0.5 *	IRB 14050 *

Table A2. A list of industrial robots and cobots from ABB considered in this work (starred models are cobots).

Table A3. A list of industrial robots and cobots from Kuka considered in this work (starred models are cobots).

AGILUS KR 6 R700 CR	AGILUS KR 6 R700 HM SC	AGILUS KR 6 R700 WP	AGILUS KR 6 R700-2
AGILUS KR 6 R900 EX	AGILUS KR 6 R900 HM SC	AGILUS KR 6 R900 WP	AGILUS KR 6 R900-2
AGILUS KR 10 R1100 EX	AGILUS KR 10 R1100 HM SC	AGILUS KR 10 R1100 WP	AGILUS KR 10 R900 CR
AGILUS KR 10 R900 WP	AGILUS KR 10 R1100-2	AGILUS KR 10 R900-2	CYBERTECH nano KR 6 R1840 2
CYBERTECH nano KR 8 R1640-2	CYBERTECH nano KR 10 R1420	CYBERTECH nano KR 10 R1440-2	CYBERTECH nano KR 6 R1840-2 arc HW
CYBERTECH nano KR 8 R1440-2 arc HW	CYBERTECH nano KR 8 R1620 arc HW	CYBERTECH nano KR 8 R1640-2 arc HW	CYBERTECH KR 8 R2010-2
CYBERTECH KR 16 R1610-2	CYBERTECH KR 16 R2010-2	CYBERTECH KR 20 R1810 CR	CYBERTECH KR 20 R1810 F
CYBERTECH KR 20 R1810-2	CYBERTECH KR 20 R1820-2 E	CYBERTECH KR 20 R2010 KS F	CYBERTECH KR 22 R1610-2
IONTEC KR 20 R3100	IONTEC KR 30 R2100	IONTEC KR 50 R2100	IONTEC KR 50 R2100 HO
	AGILUS KR 6 R900 EX AGILUS KR 10 R1100 EX AGILUS KR 10 R900 WP CYBERTECH nano KR 8 R1640-2 CYBERTECH nano KR 8 R1440-2 arc HW CYBERTECH KR 16 R1610-2 CYBERTECH KR 20 R1810-2	AGILUS KR 6 R700 CRHM SCAGILUS KR 6 R900 EXAGILUS KR 6 R900 HM SCAGILUS KR 10 R1100 EXAGILUS KR 10 R1100 HM SCAGILUS KR 10 R900 WPAGILUS KR 10 R1100-2CYBERTECH nano KR 8 R1640-2CYBERTECH nano KR 10 R1420CYBERTECH nano KR 8 R1440-2 arc HWCYBERTECH nano KR 8 R1620 arc HWCYBERTECH KR 16 R1610-2CYBERTECH KR 16 R2010-2CYBERTECH KR 20 R1810-2CYBERTECH KR 20 R1820-2 E	AGILUS KR 6 R700 CRHM SCAGILUS KR 6 R700 WPAGILUS KR 6 R900 EXAGILUS KR 6 R900 HM SCAGILUS KR 6 R900 WPAGILUS KR 10 R1100 EXAGILUS KR 10 R1100 HM SCAGILUS KR 10 R1100 WPAGILUS KR 10 R900 WPAGILUS KR 10 R1100-2AGILUS KR 10 R900-2CYBERTECH nano KR 8 R1640-2CYBERTECH nano KR 8 R1640-2CYBERTECH nano KR 8 R1620 arc HWCYBERTECH Nano KR 8 R1640-2 arc HWCYBERTECH NANO KR 8 R1640-2 arc HWCYBERTECH NANO KR 8 R1640-2 arc HWCYBERTECH KR 16 R1610-2CYBERTECH KR 16 R2010-2CYBERTECH KR 20 R1810 CRCYBERTECH KR 20 R1810-2CYBERTECH KR 20 R1820-2 ECYBERTECH KR 20 R2010 KS F

	lable AS. Com.			
IONTEC KR 50 R2500 F	IONTEC KR 50 R2500 HO	IONTEC KR 50 R2500	IONTEC KR 70 R2100 F	IONTEC KR 70 R2100
KR 40 PA	QUANTEC KR 120	QUANTEC KR 120	QUANTEC KR 120	UANTEC KR 120
	R2700-2 F	R3100-2	R3100-2 F	R3900-2 K
QUANTEC KR 150	QUANTEC KR 150	QUANTEC KR 150	QUANTEC KR 150	QUANTECKR 180
R2700-2	R2700-2 F	R3100-2	R3100-2 F	R2900-2
QUANTEC KR 180	QUANTEC KR 180	QUANTEC KR 210	QUANTEC KR 210	QUANTEC KR 210
R2900-2 F	R3500-2 K	R2700-2	R2700-2 F	R3100-2 C
QUANTEC KR 210	QUANTEC KR 210	QUANTEC KR 240	QUANTEC KR 240 QUANTEC K	
R3100-2 F	R3300-2 K	R2900-2	R2900-2 C R2900-2	
QUANTEC KR 250	QUANTEC KR 250	QUANTEC KR 270	QUANTEC KR 300 QUANTEC nar	
R2700-2 C	R2700-2 F	R3100-2 K	R2700-2 F 120 R1800	
QUANTEC nano KR	QUANTEC nano KR	QUANTEC nano KR	QUANTEC nano KR QUANTEC nan	
120 R1800 C	120 R2100 F exclusive	160 R1570	160 R1570 C 180 R2100 F exc	
QUANTEC PA KR 120	QUANTEC PA KR 120	QUANTEC PA KR 120	QUANTEC PA KR 140	QUANTEC PA KR 180
R3200	R3200 arctic	R3200 HO	R3200-2	R3200
QUANTEC PA KR 180	QUANTEC PA KR 180	QUANTEC PA KR 180	0 QUANTEC PA KR 240 QUANTEC PA	
R3200 arctic	R3200 HO	R3200-2	R3200 R3200 arc	
QUANTEC PA KR 240	QUANTEC PA KR 240	360 FORTEC KR 240	360 FORTEC KR 240	360 FORTEC KR 240
R3200 HO	R3200-2	R3330	R3330 C	R3330 F
360 FORTEC KR 280	360 FORTEC KR 280	360 FORTEC KR R2830	360 FORTEC KR R2830	360 FORTEC KR R2830
R3080	R3080 F		C	C-F
360 FORTEC KR R2830	KR 470-2 PA	500 FORTEC KR 340	500 FORTEC KR 340	500 FORTEC KR 420
F		R3330	R3330 F	R3080
500 FORTEC KR 420	500 FORTEC KR 480	500 FORTEC KR 480	500 FORTEC KR 500	500 FORTEC KR R2830
R3080 F	R3330 MT	R3330 MT-F	R2830	C
500 FORTEC KR R2830	500 FORTEC KR R2830	500 FORTEC KR R2830	500 FORTEC KR R2830	600 FORTEC KR 420
C-F	F	MT	MT-F	R3330
600 FORTEC KR 420	600 FORTEC KR 510	600 FORTEC KR 510	600 FORTEC KR 600	600 FORTEC KR 600
R3330 F	R3080	R3080 F	R2830	R2830 F
KR 700 PA	KR 640 R2800-2	KR 800 R2800-2	KR 1000 L750 titan	KR 1000 L750 titan F
KR 1000 titan	KR 1000 titan F	KR 1000 1300 titan PA	KR 1000 1300 titan PA-F	AGILUS KR 6 R900-2 HO
AGILUS KR 10 R1100-2	CYBERTECH nano KR	IONTEC KR 30 R2100	IONTEC KR 50 R2100	IONTEC KR 50 R2500
HO	10 R1440-2 HO	CR lite	CR lite	CR lite
IONTEC KR 70 R2100	IONTEC KR 70 R2100	KR 1000 L950 titan PA	FORTEC ultra KR 480	FORTEC ultra KR 480
CR lite	HO		R3400-2	R3700-2
FORTEC ultra KR 560	FORTEC ultra KR 560	FORTEC ultra KR 640) KR 300-2 PA QUANTEC PA R3200-2 PA	
R3100-2	R3100-2 HI	R2800-2 HI		
QUANTEC PA KR 180	QUANTEC PA KR 240	QUANTEC KR 120	QUANTEC KR 120 QUANTEC K	
R3200-2 PA-HO	R3200-2 PA-HO	R2700-2 HO	R3500-2 P R3500-2 P	
QUANTEC KR 150	QUANTEC KR 180	QUANTEC KR 210	QUANTEC KR 240	QUANTEC KR 270
R3100-2 HO	R3500-2 K-F	R3300-2 K-F	R2900-2 HO	R3100-2 K-F
QUANTEC KR 300 R2700-2 C	QUANTEC KR 300 R2700-2 HC	LBR iisy 3 R760 *	LBR iisy 8 R930 *	LBR iisy 11 R1300 *
LBR iisy 15 R930 *	LBR iiwa 7 R800 *	LBR iiwa 7 R800 CR *	LBR iiwa 14 R820 *	LBR iiwa 14 R820 CR *
LBR iisy 6 R1300 *				

Table A3. Cont.

GP4	GP7	GP8	GP8L	GP12	GP20	GP20HL	GP25
GP25-12	GP35L	GP50	GP70L	GP88	GP110	GP180-120	GP180
GP215	GP215-200T	GP225	GP250	GP280	GP400	GP600	GP4 FGG
GP7 FGG	GP8 FGG	GP8 FGG HS	GP12 FGG	GP25 FGG	GP50 FGG	GP180 FGG	SIA5F
SIA10F	SIA20F	SDA5F	SDA10F	SDA20F	MotoMINI	MPK2F	MPK2F-5
MPX1150	MPX1950	MPO10	MPX3500	MPX2600	AR900	AR700	AR2010
AR3120	AR1730	PL80	PL190-100	PL190	PL320	PL500	PL800
SP235	SP80	SP100	SP165-105	SP150R	SP165	SP185R	SP210
CSDA10F	AR1440	GA50	GP120RL	GP165R	GP200R	GP300R	GP400R
HC10DTP Classic *	HC10DTP *	HC10DTFP *	HC20DTP *	HC20SDTP *	HC30PL *		

Table A4. A list of industrial robots and cobots from Yaskawa considered in this work (starred models are cobots).

Table A5. A list of industrial robots and cobots from Universal Robots considered in this work (starred models are cobots).

UR3e * UR5e * UR10e * UR16e * UR20 *

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