

# Area Leakage Estimation in Water Distribution Systems: A Focus on Background Leakage <sup>†</sup>

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**Abstract:** Leakage is a major issue faced by utilities across the world. Background leaks constitute a large component, and their small size makes it challenging to localize. This paper presents a hydraulic model-based approach to localize background leaks. The proposed methodology clusters nodes into leak groups using node-weighted spectral clustering and estimates background leakage in each leak group using optimization. The algorithm successfully localized 113 out of 118 background leaks (no leak size >0.28% of the bulk supply) and estimated the leakage amount using simulated data.

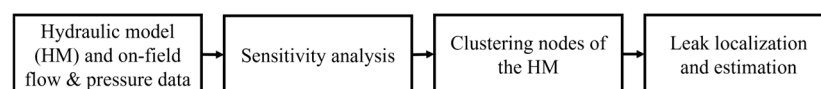
**Keywords:** background leaks; localization; node-weighted spectral clustering; sensitivity analysis

## 1. Introduction

Leak management is a major issue faced by water utilities across the world with water loss of up to 35% in developed [1] and more than 50% in developing nations [2]. Background leaks contribute to the major portion of these leaks and because of their small size, repairing them would be uneconomical. Hence pressure management can be considered an economical option for addressing background leaks [2] which requires an understanding of spatial distribution of leakage in the water distribution network (WDN). Since the background leaks and a single leak of the same leakage amount have different impacts on the pressure sensors due to the distribution of energy loss, this makes it much more challenging to localize background leaks. In the literature, numerous model-based and data-driven approaches were proposed by researchers focusing on leak localization using flow and pressure data [3,4]. But most of the methods in the literature, if not all, focus on large leaks or bursts, and background leakage has received limited attention. This paper presents a model-based approach for the localization and estimation of background leakage that uses on-field flow and pressure data.

## 2. Methodology

The framework of the proposed methodology is shown in Figure 1.



**Figure 1.** The framework of the proposed methodology.

### 2.1. Sensitivity Analysis

Sensitivity analysis is carried out to understand the sensitivity of nodal pressures to leaks in the WDN. For this, leaks ranging between 0.1 and 2% of bulk supply are simulated as pressure-dependent demands using emitters as shown in Equation (1)

$$Q_{leak_i} = K_i * P_i^n \quad (1)$$



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In Equation (1),  $Q_{leak_i}$ ,  $K_i$ ,  $P_i$  are the leakage simulated, emitter coefficient and pressure at node 'i', respectively. The value of emitter exponent 'n' is fixed as 1 [5] since background leaks are not necessarily circular. Leaks of varying sizes are simulated at nodes for computing pressure sensitivity for the unit emitter coefficient using Equation (2) with 'no-leak' scenario pressures as reference.

$$S = \begin{bmatrix} \frac{\Delta p_1}{K_1} & \dots & \frac{\Delta p_1}{K_n} \\ \vdots & \ddots & \vdots \\ \frac{\Delta p_n}{K_n} & \dots & \frac{\Delta p_n}{K_n} \end{bmatrix} \quad (2)$$

In Equation (2),  $\Delta p_n$  and  $K_n$  are the pressure change and emitter coefficient of node 'n', respectively. The sum of all columns in S results in a column matrix, where each row represents the sensitivity of a node for that scenario [6]. The sensitivity matrix S is constructed for different values of the emitter coefficient at each node, and the mean sensitivity for all scenarios is calculated and used as nodal weights for node-weighted spectral clustering in the later stage.

### 2.2. Clustering of Nodes

The clustering is performed to group all nodes into leak groups. The similarity of nodes is calculated using the calculated pressure sensitivity and connectivity of nodes [7] as shown in Equation (3) for clustering.

$$A_{ij} = \frac{\left(\frac{w_i}{d_i}\right) + \left(\frac{w_j}{d_j}\right)}{\max(w_i, w_j)} \text{ if } a_{ij} \neq 0 \text{ otherwise } A_{ij} = 0 \quad (3)$$

In Equation (3),  $A_{ij}$  is the similarity between nodes 'i' and 'j';  $w_i$  is the weight of node 'i', i.e., pressure sensitivity;  $d_i$  is the number of pipes incident at node 'i'.  $a_{ij}$  is 0 if nodes 'i' and 'j' are not connected and is 1 otherwise. Spectral clustering is performed using the Python package sci-kit-learn [8] to cluster nodes using the nodal similarities as inputs. The number of leak groups is fixed as the number of pressure sensors installed in the WDN.

### 2.3. Leak Localization and Estimation

For leak localization, an optimization problem (Equation (4)) is solved with the emitter coefficient of each leak group as a decision variable, i.e., if there are leaks in a leak group that create a detectable pressure drop, the algorithm predicts all nodes in the leak group as leaky. A genetic algorithm is deployed to solve the optimization problem.

$$F = \sum_{i=1}^{N_{pressure}} w_i (P_i^{meas} - P_i^{sim})^2 + \sum_{j=1}^{N_{flow}} w_j (Q_j^{meas} - Q_j^{sim})^2 \quad (4)$$

In Equation (4),  $P_i^{meas}$  and  $P_i^{sim}$  are the measured and simulated pressures of node 'i', respectively;  $Q_j^{meas}$  and  $Q_j^{sim}$  are the measured and simulated flows in pipe 'j', respectively.

## 3. Case Study and Dataset

The proposed methodology is demonstrated on a renowned L-town network with 33 pressure sensors (Figure 2) [9]. For the leak dataset, 7.5% of the pipes are assumed to be leaky, and leaks are simulated using emitters at both the start and end nodes of the selected pipes. The emitter is fixed so that no leak is bigger than 0.3% of the bulk supply (Figure 2).

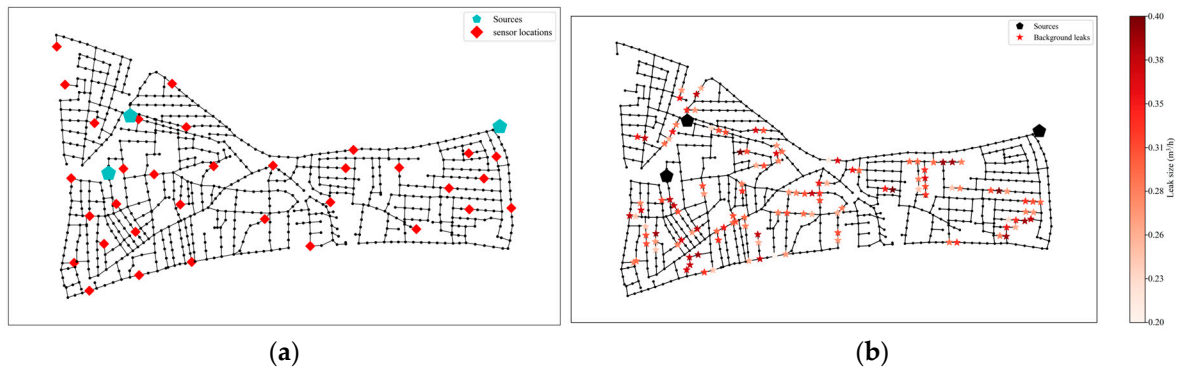


Figure 2. (a) L-town network; (b) simulated background leaks.

#### 4. Results

The contour map of nodal sensitivity values, clustering, and leak localization results are shown in Figure 3. To partially account for inaccuracies in the hydraulic model, the demands in the model are perturbed by 10% before use for leak localization. Nodes associated with different leak groups are represented by distinct colors in the corresponding Figure 3, with each leak group labeled at the top of its respective cluster.

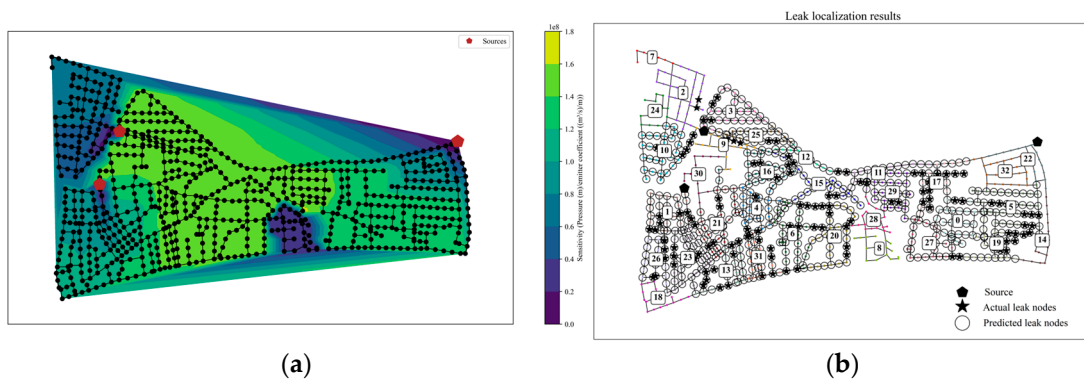


Figure 3. (a) Sensitivity analysis results; (b) clustering and leak localization.

As shown in Figure 3, 113 out of the 118 leaks simulated are localized to their respective leak groups. Figure 4 shows the leak estimation error for each leak group.

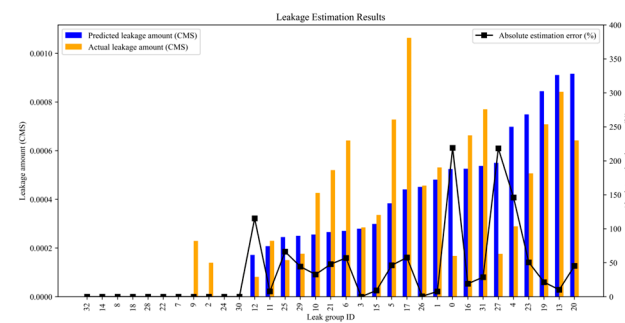


Figure 4. Leak estimation error.

In the majority of leak groups, the error estimate is between 2 and 50% of simulated leakage. But for groups 4, 27, and 0, leakage is overestimated due to neighboring high-leakage groups causing increased pressure drops, a drawback of the methodology. Despite higher errors in a few groups, the proposed methodology performed well for the majority of the leak groups and hence benefits water utilities and our understanding of spatial leakage distribution, aiding in supply and leakage management decisions.

## 5. Conclusions

A sensitivity analysis-based node-weighted spectral-clustering method is proposed for localizing leaks and estimating background leaks in water distribution networks. The approach clusters WDN nodes into leak groups and identifies leakage within each group by minimizing differences between simulated and observed flow/pressures. As demonstrated on the L-town network using simulated data, the algorithm successfully localized 113 out of the 118 leaks ranging from 0.14% to 0.28% of the bulk supply, aiding water utilities in improved decision-making for WDN operation and leakage management.

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**Conflicts of Interest:** The authors declare no conflicts of interest.

## References

1. Levinas, D.; Perelman, G.; Ostfeld, A. Water leak localization using high-resolution pressure sensors. *Water* **2021**, *13*, 591. [[CrossRef](#)]
2. Rajakumar, A.G.; Cornelio, A.A.; Mohan Kumar, M.S. Leak management in district metered areas with internal pressure reducing valves. *Urban Water J.* **2020**, *17*, 714–722. [[CrossRef](#)]
3. Wan, X.; Kuhanestani, P.K.; Farmani, R.; Keedwell, E. Literature review of data analytics for leak detection in water distribution networks: A focus on pressure and flow smart sensors. *J. Water Resour. Plan. Manag.* **2022**, *148*, 03122002. [[CrossRef](#)]
4. Romero-Ben, L.; Alves, D.; Blesa, J.; Cembrano, G.; Puig, V.; Duviella, E. Leak detection and localization in water distribution networks: Review and perspective. *Annu. Rev. Control* **2023**, *55*, 392–419. [[CrossRef](#)]
5. Greyvenstein, B.; Van Zyl, J.E. An experimental investigation into the pressure-leakage relationship of some failed water pipes. *J. Water Supply Res. Technol.—AQUA* **2007**, *56*, 117–124. [[CrossRef](#)]
6. Morosini, A.F.; Costanzo, F.; Veltri, P.; Savić, D. Identification of measurement points for calibration of water distribution network models. *Procedia Eng.* **2014**, *89*, 693–701. [[CrossRef](#)]
7. Fang, Q.; Zhao, H.; Xie, C.; Chen, T. A method for water supply network DMA partitioning planning based on improved spectral clustering. *Water Supply* **2023**, *23*, 3432–3452. [[CrossRef](#)]
8. Pedregosa, F.; Varoquaux, G.; Gramfort, A.; Michel, V.; Thirion, B.; Grisel, O.; Duchesnay, É. Scikit-learn: Machine learning in Python. *J. Mach. Learn. Res.* **2011**, *12*, 2825–2830.
9. Vrachimis, S.G.; Kyriakou, M.S. LeakDB: A benchmark dataset for leakage diagnosis in water distribution networks. *WDSA/CCWI Jt. Conf. Proc.* **2018**, *1*, 146–153.

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